

## (CHAPTER-05) (Instrument Transformers)

→ Explain current transformer & potential transformer.

Definition of Instrument Transformer: →

Instrument transformers means current transformer and voltage transformer are used in electrical power system for stepping down currents and voltages of the system.

**Current Transformer: →**

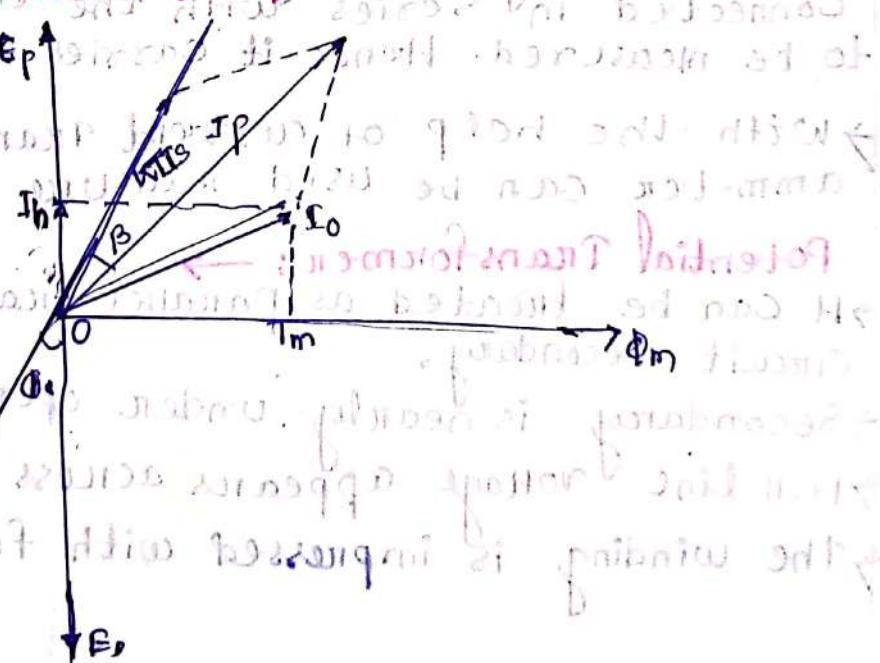
- It can be treated as series transformer under virtual short circuit conditions.
- Secondary must be always shorted.
- A small voltage exists across its terminals as connected in series.
- The winding carries full line current.
- The primary current and excitation varies over a wide range.
- The primary current is independent of the secondary circuit conditions.
- Needs only one bushing as the two ends of primary winding are brought out through the same insulator. Hence there is saving in cost.
- The secondary of a C.T. cannot be open circuited on any circumstance when it is under service.
- A current transformer may be considered as a series transformer.
- The primary winding of the current transformer is connected in series with the line carrying the current to be measured. Hence it carries of the full line current.
- With the help of current transformer, a 5A ammeter can be used measure a high current like 200A.

**Potential Transformer: →**

- It can be treated as parallel transformer under open circuit secondary.
- Secondary is nearly under open circuit conditions.
- Full line voltage appears across its terminals.
- The winding is impressed with full line voltage.

- The line voltage is almost constant hence exciting current and flux density varies over a limited range.
- The primary current depends on the secondary circuit conditions.
- Full line voltage appears across its terminals.
- The winding is impressed with full line voltage.
- The line voltage is almost constant hence exciting current and flux density varies over a limited range.
- The primary current depends on the secondary circuit conditions.
- Two bushings are required when neither side of the line is at ground potential.
- The secondary of a potential transformer can be open circuited without any damage being caused either to the operator or the transformer.
- Potential transformer may be considered as a parallel transformer.
- The primary winding is connected across the line of voltage to be measured. Hence the full line voltage is impressed across its terminals.
- With the help of potential transformer, a 120 V voltmeter can be used to measure very high voltages like 11 KV.

**Define Ratio error:**



- That primary Current  $I_p$  is not exactly equal to the secondary Current multiplied by turns ratio i.e.  $K_T I_S$
- This difference is due to the primary Current is contributed by the core excitation Current.
- The error in current transformer introduced due to this difference is called current error of current transformer.

The percentage current error =  $\frac{|I_p - K_T I_S|}{I_p} \times 100\%$ .

### Phase angle error : →

- Phase angle error is defined as the angular difference between the secondary current phasor reversed and the primary current phasor.
- If the reversed current phasor leads the primary current phasor then the phase angle error is defined as positive otherwise it is taken as negative.

### Graph

- The phase angle error is due to the no load current or exciting current. this is the angle by which the secondary current, when reversed, differs in phase from the primary current.
- In case of current Transformers, current ratio is more important, while phase angle error is of little importance. so long it is connected with an ammeter.

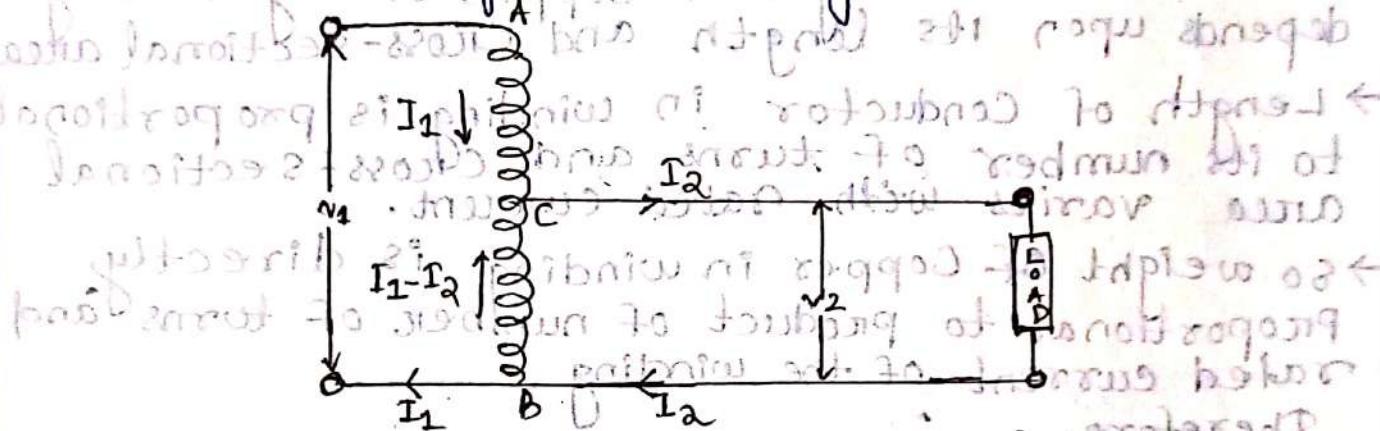
### Uses of Current Transformer : →

- Measuring such magnitude of current that the meter or instrument cannot conveniently be measured.
- Measure the current of another circuit.
- Worldwide to monitor high-voltage lines across national power grids.
- used to Reduce or multiply on alternating current.
- uses of ceramic Capacitors is as follows: M
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## Auto-Transformer (CHAPTER-4)

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- Autotransformer is a transformer having only one winding, a part of which acts as a primary and other as a secondary winding of the transformer are interrelated.
- Two winding transformer is a static machine which transfers electrical energy from one end to another without changing frequency.
- **Working Principle of single phase AutoTransformer**
- In an autotransformer, one single winding is used as primary winding as well as secondary winding.
- Two windings transformer two different windings are used for primary and secondary purpose.



Q. 1. (Diagram of) auto Transformer. →

- The winding AB of total turns  $N_1$  is considered as Primary winding.
- This winding is tapped from point C and position BC is considered as secondary.
- The number of turns in between points B and C is  $N_2$ .
- If voltage is applied across the winding in between (A & C), so voltage per turn in this winding is  $\frac{V_1}{N_1}$ .
- The voltage across the portion BC of the winding will be  $\frac{V_1}{N_1} \times N_2$ , and from the figure above, this voltage is  $V_2$ . Hence  $\frac{V_1}{N_1} \times N_2 = V_2$
- $\frac{V_2}{V_1} = \frac{N_2}{N_1}$  Constant  $= k$

- B portion is secondary winding.
- That value of constant ( $k$ ) is nothing but turns ratio or voltage ratio of that auto-transformer.
- When load is connected between secondary terminals i.e. between (B) and (C), load current  $I_2$  starts flowing.
- The current in the secondary winding or common winding is the difference of  $I_2$  and  $I_1$ .

### Comparison of Auto transformer with a two winding transformer (saving of copper)

- We know that weight of copper of any winding depends upon its length and cross-sectional area.
- Length of conductor in winding is proportional to its number of turns and cross-sectional area varies with rated current.

→ So weight of copper in winding is directly proportional to product of number of turns and rated current of the winding.

Therefore,

Weight of copper in the section AC

Proportional to

$$(N_1 - N_2) I_1$$

and similarly weight of copper in the section BC is proportional to

Hence,

Total weight of copper in the winding of auto transformer proportional to,

$$(N_1 - N_2) I_1 + N_2 (I_2 - I_1)$$

$$\Rightarrow N_1 I_1 - N_2 I_1 + N_2 I_2 - N_2 I_1$$

$$\Rightarrow N_1 I_1 + N_2 I_2 - 2N_2 I_1$$

$$\Rightarrow 2N_1 I_1 - 2N_2 I_1 \quad (\text{since } N_1 I_1 = N_2 I_2)$$

$$\Rightarrow 2(N_1 I_1 - N_2 I_1)$$

~~Proved that~~ → Proved that, the weight of copper in 2 winding transformer is proportional to  $N_1 I_1 \propto N_2 I_2$

$$\text{and of } W_t = 2(N_1 I_1 + N_2 I_2) \quad (\because N_1 I_1 = N_2 I_2)$$

$$\Rightarrow 2 N_2 I_2 = N_1 I_1 - N_2 I_2 \quad (\because N_1 I_1 = N_2 I_2)$$

$$\Rightarrow 2 N_1 I_1 = N_2 I_2 - N_2 I_2$$

$$\Rightarrow 2 N_1 I_1 = N_2 I_2 - N_2 I_2$$

$W_a$  &  $W_{tw}$  are weight of copper in auto transformer and two winding transformer respectively,

Hence  $\frac{W_a}{W_{tw}} = \frac{2(N_1 I_1 - N_2 I_2)}{2(N_1 I_1)}$

$$= \frac{N_1 I_1 - N_2 I_2}{N_1 I_1} = 1 - \frac{N_2 I_2}{N_1 I_1}$$

$$\Rightarrow 1 - \frac{N_2}{N_1} = 1 - K$$

$$\therefore W_a = W_{tw}(1 - K)$$

∴ Saving copper in auto transformer compared to two winding transformer,

$$\Rightarrow W_{tw} - W_a = K W_{tw}$$

### Advantages of using Auto Transformers:

→ The saving in cost of the material is of course not in the material is of course not in the same proportion.

→ The saving of cost is appreciable when the ratio of transformer is low, that is lower than 2.

→ Auto transformer is smaller in size and cheaper.

→ Auto transformer has higher efficiency than two winding transformer.

→ Loss ohmic loss and core loss due to reduction of transformer material.

→ Auto transformer has better voltage regulation as voltage drop in resistance and reactance of the single winding is less.

## Disadvantages of using Auto transformer:

- Electrical conductivity of the primary and secondary windings the lower voltage ckt is liable to be impressed upon by higher voltage.
- To avoid breakdown in the lower voltage circuit.
- The leakage flux between the primary and secondary windings is small and hence the impedance is low. This results into sever short ckt current under fault conditions.
- Common neutral in a star connected auto transformer it is not possible to earth neutral of one side only.
- Range of tapping is very large, the advantages gained in initial cost is lost to great extent.

## uses of Autotransformer:

- Compensating voltage drops by boosting supply voltage in distribution systems.
- Auto transformers with a number of tapping are used for starting induction and synchronous motors.
- Auto transformer is used as variac in laboratory or where continuous variable over broad ranges are required.

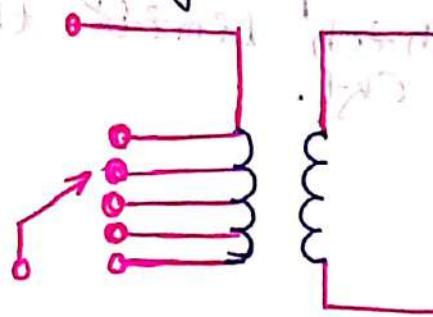
## Tap-changing Transformers:

- The change of voltage is affected by changing the numbers of turns of the transformer provided with taps.
- For sufficiently close control of voltage, taps are usually provided on the high voltage windings of the transformer.
- There are two types of tap-changing transformers:

1. off-load tap-changing transformer

2. on-load tap-changing transformer

**Off-Load tap-changing Transformer:** → The transformer is disconnected from the main supply when the tap setting is to be changed. The tap setting is usually done manually.



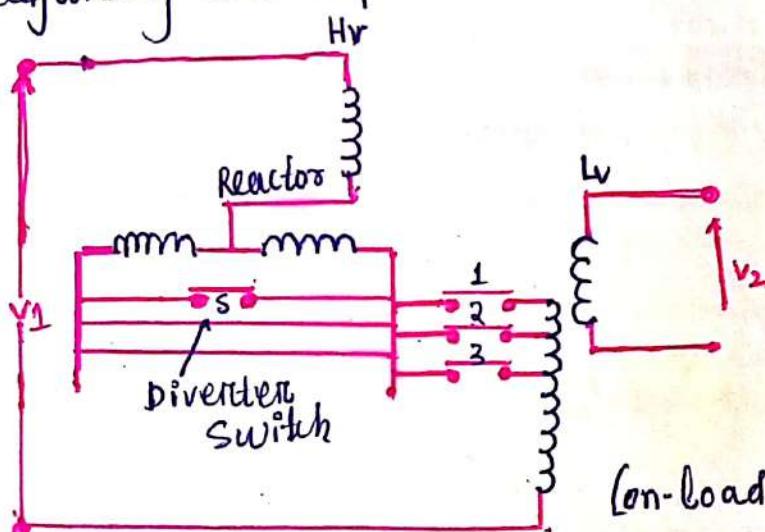
**On-Load tap-changing Transformer:** →

→ On-Load tap changing transformers are used. Such a transformer is known as a tap-changing under load transformer.

→ While tapping, two essential conditions are to be fulfilled.

1. The load ckt should not be broken to avoid arcing and prevent the damage of contacts.

2. No parts of the windings should be short circuited while adjusting the tap.



(on-load tap changing using a reactor)

R → Center tapped reactor.

S → Divertor switch

1, 2, 3 → Selector switch.

→ The transformer is in operation with switches 1 and S closed. To change to tap 2, switch S is opened, and 2 is closed, switch 1 is then opened, and S closed to complete the tap change.

- It is to be noted that the diverter switch operates on load, and no current flows in the selector switches during tap changing.
- During the tap change, only half of the reactance which limits the current is connected in the Ckt.



## Practical Transformer on Load

Two cases :> (i) When such a transformer is assumed to have no winding resistance and leakage flux

(ii) When the transformer has winding resistance and leakage flux.

(i) No winding resistance and leakage flux.

→ Practical transformer with the assumption that resistances and leakage reactances of the winding are negligible.

Assumption,  $v_2 = E_2$  and  $v_1 = E_1$

Let us take the usual case of inductive load which causes the secondary current  $I_2$  to lag the secondary voltage  $v_2$  by  $\phi_2$

→ The total primary current  $i_1$  must meet two requirements

(a) It must supply the no-load current  $I_0$  to meet the iron losses in the transformer and to provide flux in the core.

(b) It must supply a current  $I_2'$  in counteract the demagnetizing effect of secondary current  $I_2$ .

The magnitude of  $I_2'$  will be such that

$$N_1 I_2 = N_2 I_2'$$

$$I_2' = \frac{N_2}{N_1} I_2 = K I_2$$

### Phasor diagram →

$E_1, E_2 \rightarrow$  lag behind the mutual flux  $\Phi$  by  $90^\circ$ .

$I_2' \& I_2 \rightarrow$  primary & secondary current

$I_2 = K I_2'$  and it antiphase with  
 $E_2, I_0 \rightarrow$  No load Current of the  
transformer.

The value  $K$  is assumed to be unity  
So that,

Primary phasors = Secondary phasors.

Primary Power factor =  $\cos \phi_1$

Secondary " " =  $\cos \phi_2$

Primary input power =  $V_1 I_1 \cos \phi_1$

Secondary output power =  $V_2 I_2 \cos \phi_2$

(ii) Transformed with resistance and leakage reactance  
→ It must supply the no-load current  $I_0$  to meet the iron losses in the transformer and to provide flux in the core.

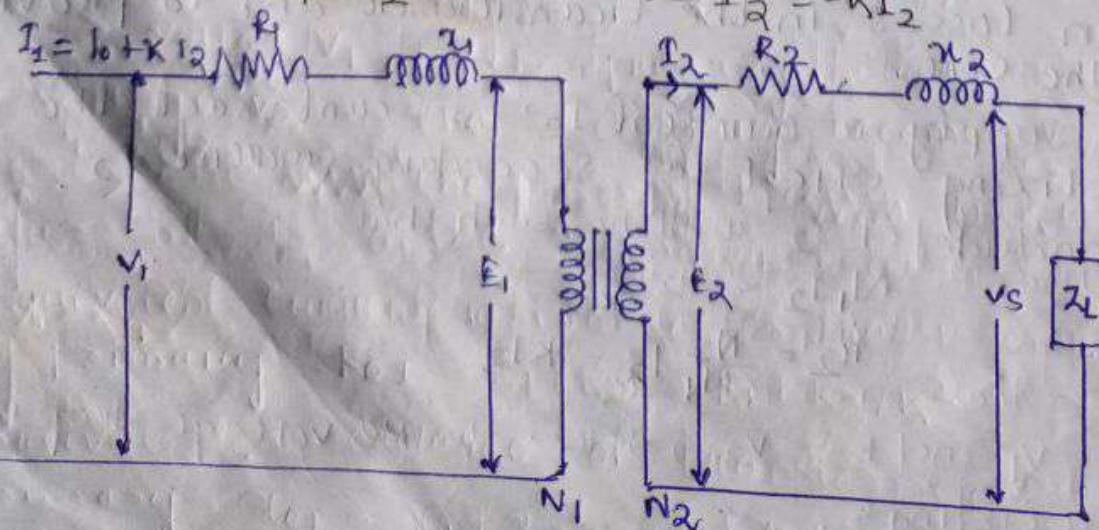
→ Supply current  $I_2'$  to the demagnetising effect of  
secondary Current  $I_2'$ . The magnitude of  $I_2'$  will be

$$N_1 I_2' = N_2 I_2$$

$$I_2' = \frac{N_2}{N_1} I_2 = K I_2$$

The total primary current  $I_1$  will be the  
phasor sum of  $I_2'$  and  $I_0$  i.e.

$$I_1 = I_2' + I_0 \text{ where } I_2' = -K I_2$$



$$v_1 = -E_1 + I_1(R_1 + jX_1) \quad \text{where } I_1 = I_0 + (kI_2)$$

$$= -E_1 + I_1 Z_1$$

$$v_2 = E_2 - I_2(R_2 + jX_2)$$

$$= E_2 - I_2 Z_2$$

Phasor diagram:-

Both  $E_1$  &  $E_2$  lag the mutual flux  $\phi$  by  $90^\circ$

$I_2'$  &  $I_2$  → primary & secondary current.

$I_2' = kI_2$  and is opposite to  $I_2$ .  
Also  $I_0$  is the no-load current of the transformer.

$\Rightarrow I_2$  &  $I_0$  gives the total primary current  $I_1$ .

→ Load power factor  $= \cos \phi_2$

→ Primary power factor  $= \cos \phi_1$

→ Input power to transformer ( $P_1$ )  
 $= V_1 I_1 \cos \phi_1$

→ Output power/ $\phi$  of transformer ( $P_2$ )  $= V_2 I_2 \cos \phi_2$

### Impedance Ratio

Consider a transformer having secondary impedance  $Z_2$

$$Z_2 = \frac{V_2}{I_2}$$

$$\Rightarrow Z_1 = \frac{V_1}{I_1}$$

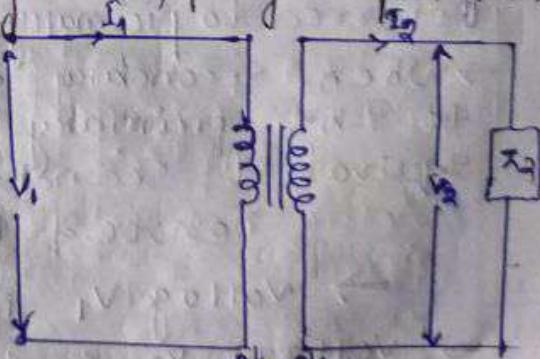
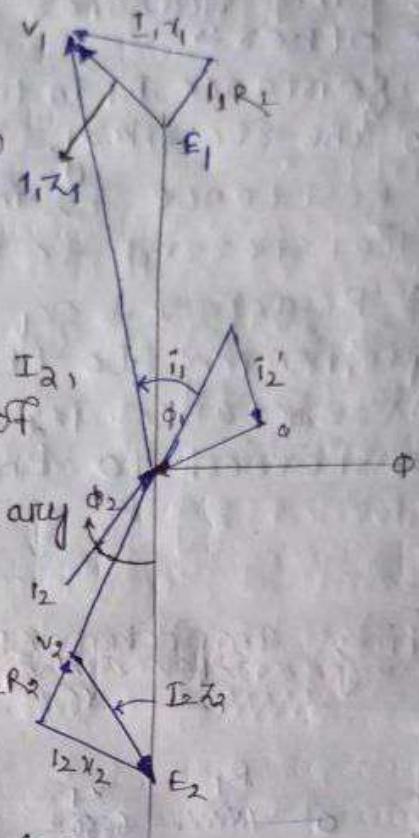
$$\frac{Z_2}{Z_1} = \cancel{\left( \frac{V_2}{V_1} \right)} \times \left( \frac{I_1}{I_2} \right)$$

$$\frac{Z_2}{Z_1} = k^2$$

The impedance ratio ( $Z_2/Z_1$ ) is equal to the square of voltage transformation ratio.

→ Impedance  $Z_2$  in secondary becomes  $Z_2/k^2$  when transferred to primary.

→ Impedance  $Z_1$  in primary becomes  $k^2 Z_2$  when transferred to the secondary.



Similarly,  $\frac{R_2}{R_1} = k^2$

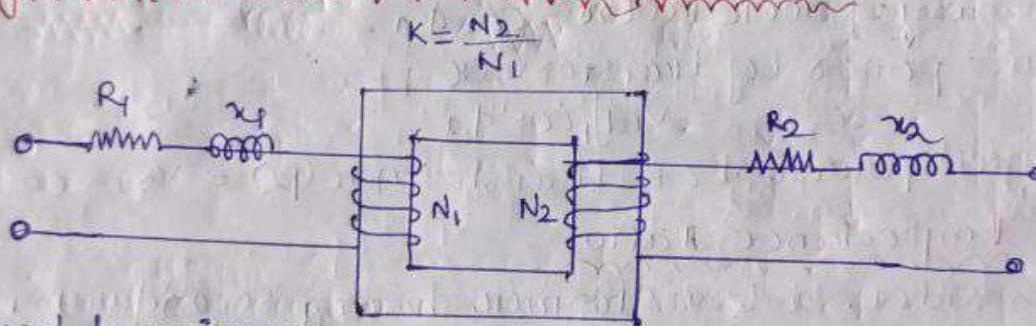
$$\frac{x_2}{x_1} = k^2$$

We can transfer the parameters from one winding to the other:

- (i) A Resistance  $R_1$  in the primary becomes  $k^2 R_1$  when transferred to the secondary.
- (ii) A Resistance  $R_2$  in the secondary becomes  $R_2/k^2$  when transferred to the primary.
- (iii) A Reactance  $x_1$  in the primary becomes  $k^2 x_1$  when transferred to the secondary.
- (iv) A reactance  $x_2$  in the secondary becomes  $x_2/k^2$  when transferred to the primary.

~~Ques~~

### Shifting Impedances in a Transformer: →



Referred to primary: →

→ When Secondary resistance or reactance is transferred to the primary, it is divided by  $k^2$ . It is then called equivalent Secondary reactance.  
denoted by  $R_2'$  or  $x_2'$

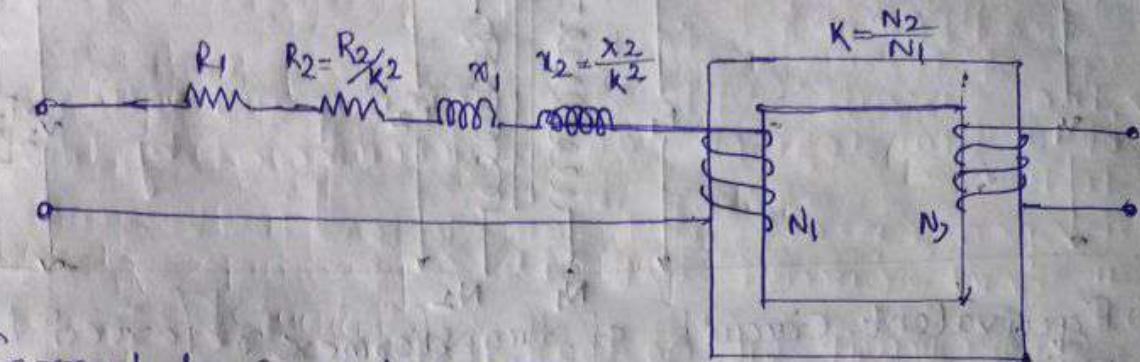
- Voltage  $V_1$  in the primary becomes  $kV_1$  in the secondary
- Voltage  $v_2$  in the secondary becomes  $v_2/k$  in the primary
- Current  $I_1$  in the primary becomes  $I_1/k$  in the secondary
- Current  $I_2$  in the secondary becomes  $kI_2$  in the primary

Equivalent ~~current~~ resistance of transformer referred to primary  $R_{01} = R_1 + R_2' = R_1 + R_2/k^2$

Equivalent reactance of transformer referred to Primary  $x_{01} = x_1 + x_2' = x_1 + x_2/k^2$

Equivalent impedance of transformer referred to ~~primary~~ secondary

$$Z_{02} = \sqrt{R_{02}^2 + X_{02}^2}$$



Referred to secondary: →

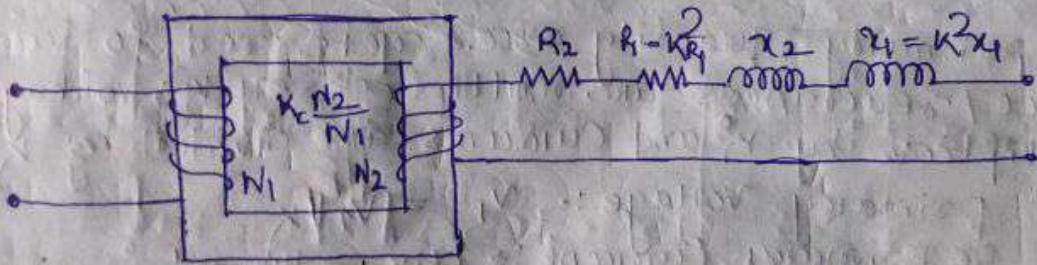
→ When Primary resistance or reactance is transferred to the secondary, it is multiplied by  $K^2$ . It is called equivalent primary resistance or reactance.

→ It is denoted by  $R'_1$  or  $x'_1$

→ Equivalent resistance of transformer referred to secondary:  $R'_{02} = R_2 + R'_1 = R_2 + K^2 R_1$

→ Equivalent reactance of transformer referred to secondary:  $X'_{02} = X_2 + X'_1 = X_2 + K^2 X_1$

→ Equivalent impedance of transformer referred to secondary:  $Z'_{02} = \sqrt{R'_{02}^2 + X'_{02}^2}$

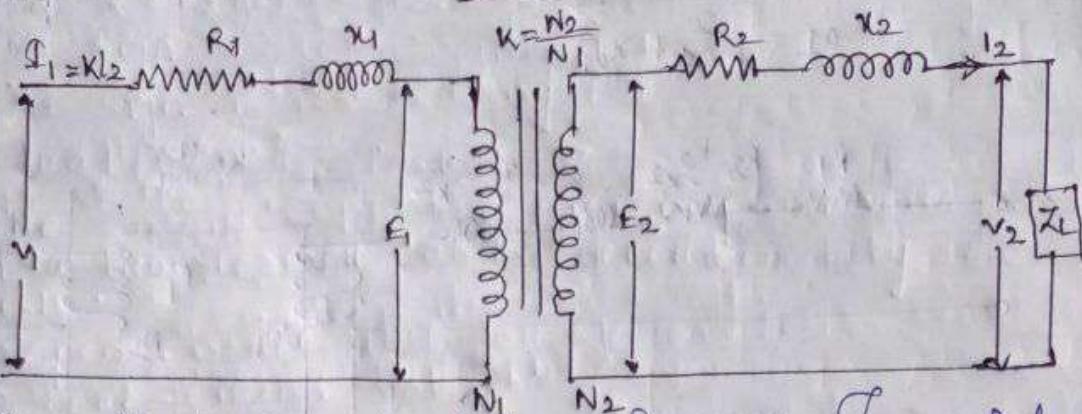


Approximate Equivalent circuit of a Transformer: →

→ The no-load current  $I_0$  in a transformer is only 1-3% of the rated primary current and may be neglected without any serious error.

→ This is an approximate representation because no-load current has been neglected.

### Ideal Transformer



(i) Equivalent circuit of transformer referred to Primary  $\rightarrow$

$\rightarrow$  When secondary quantities are referred to primary resistances/reactances are divided by  $K^2$ , voltage are divided by  $K$  and currents are multiplied by  $K$ .

$$\text{Actual Secondary Voltage } V_2 = K V_2'$$

$$\text{Actual Secondary Current } I_2 = I_2' / K$$

$$I_1 = I_2 = K I_2'$$

$$R_1' = R_1 / K^2$$

$$X_1' = X_1 / K^2$$

$$I_2' = K I_2$$

$$V_2' = \frac{V_2}{K}$$

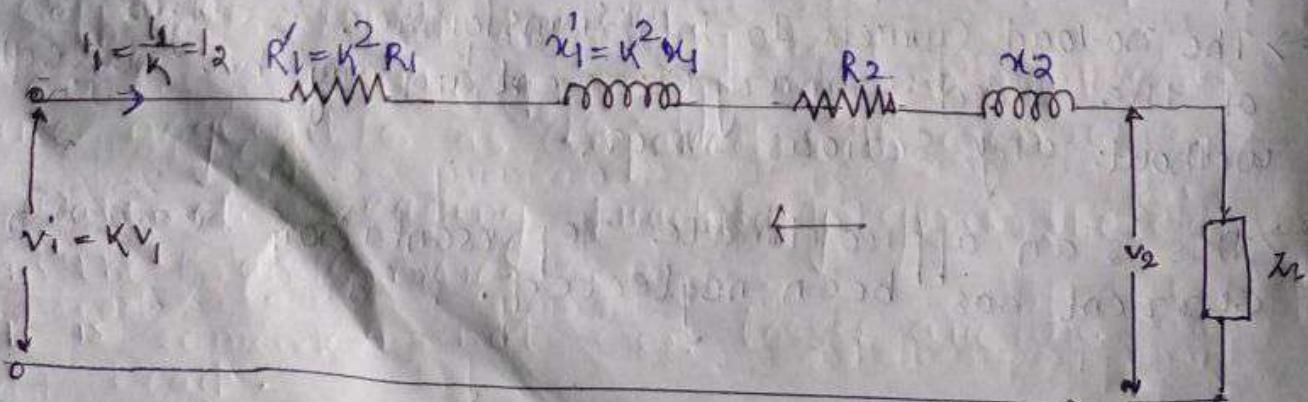
$$Z_L' = \frac{Z_L}{K^2}$$

(ii) Equivalent circuit of transformer referred to Secondary

$\rightarrow$  When primary quantity are referred to Secondary resistance/reactances are multiplied by  $K^2$ , voltage are multiplied by  $K$  and currents are divided by  $K$ .

$$\text{Actual Primary Voltage: } V_1 = V_1' / K$$

$$\text{Actual Primary Current: } I_1 = K I_1'$$



Approximate Voltage Drop in a Transformer: →

→ The approximate equivalent circuit of transformer referred to secondary.

→ No-load, secondary voltage is  $KV_1$ , when a load having a lagging Powerfactor P.f  $\cos\phi_2$  is applied.

→ The secondary carries a current  $I_2$  and voltage drops occur in  $(R_2 + K^2 R_1)$  and  $(x_2 + K^2 x_1)$

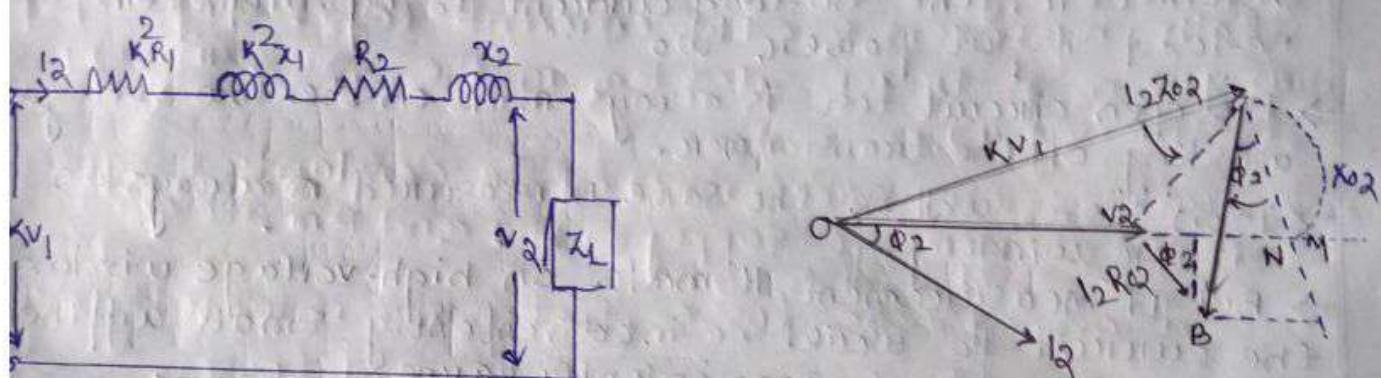
The secondary voltage falls from  $KV_1$  to  $V_2$

$$V_2 = KV_1 - I_2 (R_2 + K^2 R_1) + j (x_2 + K^2 x_1)$$

$$= KV_1 - I_2 (R_{02} + j x_{02})$$

$$= KV_1 - I_2 Z_{02}$$

$$= KV_1 + V_2 = I_2 Z_{02} \quad (\text{Drop in secondary voltage})$$



Approximate drop in secondary voltage.

$$= AN = AD + DN$$

$$= AD + BL$$

$$= I_2 R_{02} \cos\phi_2 + I_2 x_{02} \sin\phi_2$$

for a load having a leading P.f  $\cos\phi_2$

$$\text{Approximate voltage drop} = I_2 R_{02} \cos\phi_2 - I_2 x_{02} \sin\phi_2$$

**Voltage Regulation:** →

The voltage regulation of a transformer is the arithmetic difference between the no-load secondary voltage ( $0V_2$ ) and the secondary voltage  $V_2$  on load expressed as percentage of no load voltage.

$$\% \text{age voltage regulation} = \frac{0V_2 - V_2}{0V_2} \times 100$$

$$0V_2 = \text{No-load secondary voltage} = KV_1$$

$$V_2 = \text{Secondary voltage on load.}$$

$$0V_2 - V_2 = I_2 R_{02} \cos \phi_2 + I_2 X_{02} \sin \phi_2$$

+ve sign is for lagging P.F

-ve sign is for leading P.F

### Transformer Tests :→

→ The circuit constants, efficiency and voltage regulation of a transformer can be determined by two simple tests.

- (i) open-circuit test or No-load test.
- (ii) short-circuit test

### Open-circuit or No load Test :→

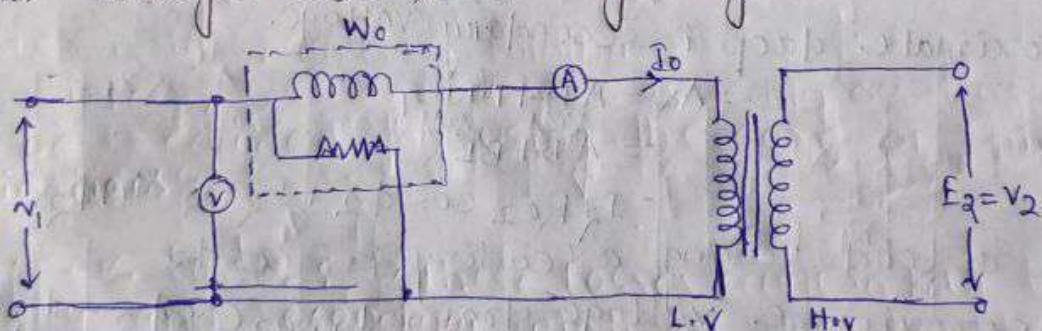
→ In this test, the rated voltage is applied to the primary while the secondary is left open-circuited.

→ The applied primary voltage  $V_1$  is measured by the voltmeter, the no-load current  $I_0$  by ammeter and no-load input power  $W_0$ .

→ The open circuit test is always made on the low-voltage winding of the transformer.

→ Iron losses will be the same if measured ~~is~~ always on either winding.

→ But if measurement is made on high-voltage winding the current  $I_0$  would be inconveniently small and the applied voltage inconveniently large.



→ Wattmeter will record the iron losses and small copper loss in the primary.

→ Cu losses in the primary under no load condition are negligible as compared with iron losses.

→ Wattmeter reading practically gives the iron loss in the transformer.

→ It is reminded that iron losses are the same at all loads.

Iron losses.  $P_1$  = wattmeter reading into  
 No load current  $I_0$  = Ammeter reading =  $I_0$   
 Applied voltage  $V_1$  = Voltmeter reading =  $V_1$   
 Input power  $W_0 = V_1 I_0 \cos \phi_0$

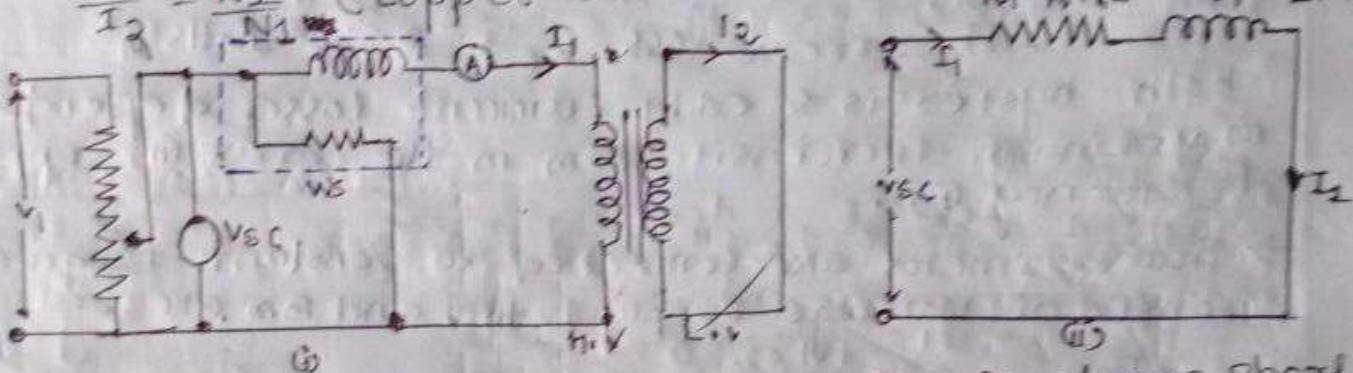
$$\text{No-load p.f. } \cos \phi_0 = \frac{W_0}{V_1 I_0} \approx 1$$

$$I_w = I_0 \cos \phi_0, I_m = I_0 \sin \phi_0$$

(i) Short-circuit or Impedance test: →

→ The secondary is short-circuited by a thick conductor and variable low voltage is applied to the primary.  
→ The low input voltage is gradually raised till at voltage  $V_{SC}$  full load current  $I_1$  flows in the primary.

$$\frac{I_1}{I_2} = \frac{N_2}{N_1} \quad (\text{Copper loss is the same as that on full load})$$



→ Short-circuit test: → low voltage winding is always short-circuited and measurements are made on the high voltage winding.

→ If measurements are made on the low-voltage winding the voltage will be inconveniently low.

full load cu loss.  $P_C$  = wattmeter reading =  $W_S$ .

Applied voltage = voltmeter reading =  $V_{SC}$

Primary Current = Ammeter reading =  $I_1$

$$P_C = I_1^2 R_{11} + I_1^2 R_2' = I_1^2 R_{02}$$

$$R_{02} = P_C / I_1^2$$

Real impedance referred to primary  $\bar{Z}_{01} = V_{SC}/I_1$

Total leakage reactance referred to primary

$$X_{01} = \sqrt{\bar{Z}_{01}^2 - R_{02}^2}$$

$$\text{short-crt p.f. } \cos \phi_S = P_C / V_{SC} I_1$$

Short-crt test gives full-load cu loss,  $R_{01}, X_{01}$   
Short-crt test will give full-load cu loss.

## Losses in a Transformer :

The power losses in a transformer are 2 types

1. Core or Iron Losses

2. Copper Losses.

These losses appear in the form of heat and produce (i) an increase in temperature

(ii) a drop in efficiency.

1) Core or Iron Losses : ( $P_I$ ) →

These consist of hysteresis and eddy current losses and occur in transformer core due to the alternating flux.

$$\text{Hysteresis loss} = K_h f B_m^{1.6} \text{ watts/m}^3$$

$$\text{Eddy Current loss} = K_e f^2 B_m^2 t^2 \text{ watts/m}^3$$

Both hysteresis & eddy current losses depend upon (i) maximum flux density  $B_m$  in the core & (ii) supply frequency ( $f$ ).

→ Transformers are connected to constant frequency, Constant voltage supply both  $f$  and  $B_m$  are constant.

Iron or core losses,  $P_I = \text{Hysteresis loss} + \text{eddy current loss}$   
= constant losses.

→ Hysteresis loss can be minimised by using steel of high silicon content whereas eddy current loss can be reduced by using the core of thin laminations.

2) Copper Losses : → These losses occur in both the primary and secondary windings due to their ohmic resistance.

→ These can be determined by short-circuit test

$$\text{Total cu losses} = P_C = I_1^2 R_1 + I_2^2 R_2$$

$$= I_1^2 R_{01} + I_2^2 R_{02} \quad (\text{variable losses})$$

→ It is clear that copper losses vary as the square of load current.

Total losses in a transformer =  $P_{it} + P_C$   
 = Constant losses + Variable losses  
 In transformers, copper losses account for about 90% of the total losses.

Efficiency of a Transformer : →

The efficiency of a transformer is defined as the ratio of output power to input power (watt or kW)

$$\text{Efficiency} = \frac{\text{O/P Power}}{\text{I/P Power}}$$

Efficiency can be determined by directly loading the transformer and measuring input & output power.  
 Method : Since efficiency of a transformer is very high considerate even 1% error in each wattmeter may give ridiculous results.

Since the test is performed with transformer on load, considerable amount of power is wasted for large transformer. → The cost of power alone would be considerable.

It is generally difficult to have a device that is capable of absorbing all of the output power.

The test gives no information about the proportion of various losses.

Open circuit & short circuit tests are carried out to find the efficiency.

$$\text{Efficiency} = \frac{\text{Output}}{\text{Input}} = \frac{\text{Output}}{\text{Output} + \text{Losses}}$$

Efficiency from Transformer test : →

$$\text{F.L. Iron loss} = P_{it} \text{ (open-circut)}$$

$$\text{F.L. C.U. loss} = P_C \text{ (short-circut)}$$

$$\text{Total F.L. losses} = P_{it} + P_C$$

Find full load efficiency of the transformer at any p.f without actually loading the transformer.

$$\text{F.L. efficiency } \eta_{fl} = \frac{\text{full-load VA} \times \text{p.f}}{(\text{full-load VA} \times \text{p.f}) + P_{it} + P_C}$$

$$\eta_R = \frac{(\alpha \times \text{full load VA}) \times \text{p.f}}{(\alpha \times \text{full load VA} \times \text{p.f}) + P_{it} + \alpha^2 P_C}$$

Condition for maximum efficiency  $\rightarrow$

$$\text{Output power} = V_2 I_2 \cos \phi_2$$

If  $R_{02}$  is the total resistance of the transformer referred to secondary,

$$\text{Total Cu Loss, } P_C = I_2^2 R_{02}$$

$$\text{Total loss} = P_t + P_C$$

$$\therefore \text{Transformer efficiency } \eta = \frac{V_2 I_2 \cos \phi_2}{V_2 I_2 \cos \phi_2 + P_t + I_2^2 R_{02}}$$

$$= \frac{V_2 I_2 \cos \phi_2}{V_2 \cos \phi_2 + P_t / I_2 + I_2 R_{02}}$$

$\rightarrow$  for normal transformer  $V_2$  is constant.

$\rightarrow$  for a load of given  $P_t$ , efficiency depends upon load current.

$\Rightarrow$

$$\frac{d\eta}{dI_2} = 0$$

$$\text{or } \frac{d}{dI_2} (V_2 \cos \phi_2 + P_t / I_2 + I_2 R_{02}) = 0$$

$$\text{or } 0 - \frac{P_t}{I_2^2} + R_{02} = 0$$

$$P_t = I_2^2 R_{02}$$

Iron losses = copper losses

$\rightarrow$  Hence efficiency of transformer will be maximum when copper losses are equal to constant iron loss.

$$I_2 = \sqrt{\frac{P_t}{R_{02}}}$$

$\rightarrow$  in a transformer, iron losses are constant whereas copper losses are variable.

$\rightarrow$  load current should be that total cu losses equal to iron losses.

$$1.9 \times 10^{-3} \times 100 \times 100 = 1.9 \times 10^{-3} \times 100 \times 100$$
$$1.9 \times 10^{-3} \times 100 \times 100 = 1.9 \times 10^{-3} \times 100 \times 100$$
$$1.9 \times 10^{-3} \times 100 \times 100 = 1.9 \times 10^{-3} \times 100 \times 100$$

Output KVA Corresponding to maximum efficiency :-

$P_C$  = Copper Losses at full-load kVA

$P_i$  = Iron Losses

$\chi$  = Fraction of full-load kVA at which efficiency is maximum

$$= \chi^2 P_C \quad (\rightarrow \text{Total Cu loss})$$

$$\chi^2 P_C = P_i$$

$$\chi = \sqrt{\frac{P_i}{P_C}} = \sqrt{\frac{\text{Iron loss}}{\text{f.l. Cu loss}}}$$

∴ Output KVA corresponding to maximum efficiency

$$= \chi \times \text{full load kVA}$$

$$= \text{full load kVA} \times \sqrt{\frac{\text{Iron loss}}{\text{f.l. Cu loss}}}$$

All day (or energy) efficiency :-

Commercial efficiency =  $\frac{\text{output power}}{\text{input power}}$

→ The performance of such transformers is judged on the basis of energy consumption during the whole day. This is known as all-day or energy efficiency.

→ The ratio of output in kWh to the input in kWh of a transformer over a 24-hour period is known as all-day efficiency.

$$\eta_{\text{all-day}} = \frac{\text{kWh output in 24 hours}}{\text{kWh input in 24 hours}}$$

→ All day efficiency is of special importance for those transformers whose primaries are never open-circuited but the secondaries carry little or no load much of the time during the day.

Construction of a Transformer :-

→ (i) The core is made of silicon steel which has low hysteresis loss and high permeability.

→ further core is laminated in order to reduce eddy current loss, iron losses and no-load

→ Current.

(ii) Instead of placing primary on one limb and secondary on the other.

→ This ensures tight coupling between the two windings, consequently leakage magnetic flux is considerably reduced.

(iii) The winding resistance  $R_1$  and  $R_2$  are minimised to reduce  $I^2R$  loss and resulting rise in temp and to ensure high efficiency.

Cooling of Transformers : →

→ Heat is produced in a transformer by the iron loss in the core and  $I^2R$  loss in the windings.

(i) In small transformers, natural air cooling is employed i.e. the heat produced is carried away by the surrounding air.

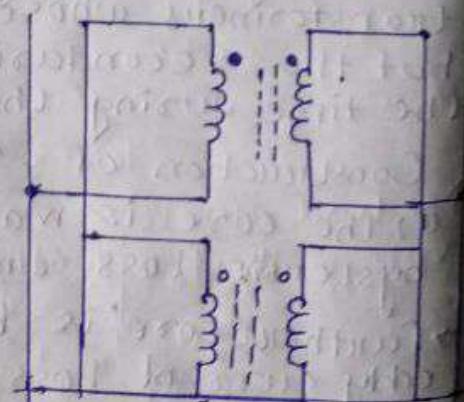
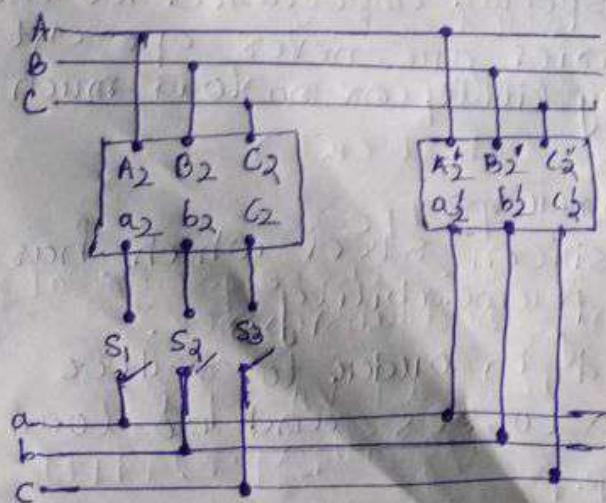
(ii) Medium size power or distribution transformers are generally cooled by housing them in tank filled with oil.

\* The oil serves a double purpose, carrying the heat from the windings to the surface of the tank and insulating the primary from the secondary.

(iii) For Large transformers, external radiators are added to increase the cooling surface of the oil filled tank.

\* The air circulates around the transformer and moves through the radiators where the heat is released to surrounding air.

What is parallel operation of Transformers ?



Why parallel operation of transformer is required?

→ It is economical to install numbers of smaller rated transformers in parallel than installing a bigger rated electrical power transformer.

Advantages :-

1. To maximize electrical power system efficiency generally electrical power transformer gives the maximum efficiency at full load.

→ If we run numbers of transformers in parallel, we can switch on only those transformers which will give the total demand by running nearer to its full rating for that time.

→ When load increases, we can switch none by one other transformer connected in parallel to fulfill the total demand.

→ In this way we can run the system with maximum efficiency.

2. To maximize electrical power system availability

→ If numbers of transformers run in parallel, we can shutdown any one of them for maintenance purpose.

→ Other parallel transformers in system will serve the load without total interruption of power.

3. To maximize power system reliability

→ If any one of the transformers run in parallel, is tripped due to fault of other parallel transformers in the system will share the load, hence power supply may not be interrupted if the shared loads do not make other transformers over loaded.

4. To maximize electrical power system flexibility

→ There is always a chance of increasing or decreasing future demand of power system.

→ It is predicted that power demand will be increased in future.

→ It is not economical from business point of view to install a bigger rated single transformer by forecasting the increased future demand as it is unnecessary investment of money.

→ Again if future demand is decreased transformers running in parallel can be removed from system to balance the capital investment and its return.

Conditions for parallel operation of Transformers: →

When two or more transformers run in parallel, they must satisfy the following Conditions for satisfactory performance.

These are the conditions for parallel operation of transformers.

1. Same voltage ratio of transformer.
2. Same percentage impedance
3. Same polarity
4. Same phase sequence,

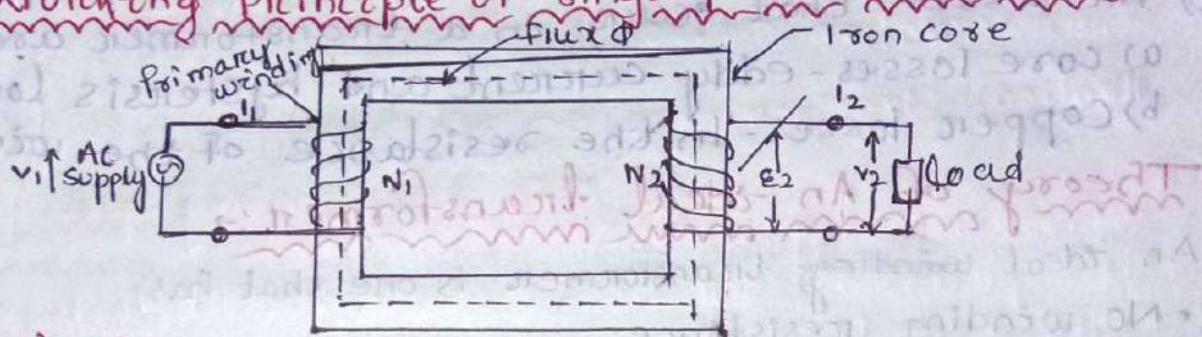
### (CHAPTER-3) (Single phase Transformer)

**Transformer** → The transformer is a static device which transfer electric power from one circuit to another circuit without any change in frequency.

Transformers are performed the following imp tasks :-

- \* To step up the voltage for transmission and other purpose.
- \* To step down the voltage for distribution purpose in Rectifiers and other electronic equipment.

#### Working Principle of single phase Transformer



#### Working :-

When an alternating voltage  $v_1$  is applied to the primary, an alternating flux  $\phi$  is set up in the core.

→ This alternating flux links both the windings and induces emfs  $E_1$  &  $E_2$  in them according to faraday's law of electromagnetic induction.

→ The emf  $E_1$  is termed as primary emf and emf  $E_2$  is termed as secondary emf.

$$E_1 = -N_1 \frac{d\phi}{dt}$$

$$E_2 = -N_2 \frac{d\phi}{dt}$$

$$\frac{E_2}{E_1} = \frac{+N_2 \frac{d\phi}{dt}}{+N_1 \frac{d\phi}{dt}} = \frac{N_2}{N_1}$$

→ that magnitudes of  $E_2$  and  $E_1$  depends upon the number of turns of the secondary and primary respectively.

→ A step-down transformer, if load is connected across the secondary winding, the secondary emf  $E_2$  will cause a current  $I_2$  to flow through the load.

→ A transformer enables us to transfer ac power from one circuit to another with a change in voltage level.

- Properties of Transformer
- (i) The transformer action is based on the laws of electromagnetic induction.
  - (ii) There is no electrical connection between the primary and secondary.
  - (iii) The a.c power is transferred from primary to secondary through magnetic flux.
  - (iv) There is no change in frequency i.e. output power has the same frequency as the input power.
  - (v) The losses that occur in a transformer are.
    - a) core losses - eddy current and hysteresis losses.
    - b) copper losses - In the resistance of the winding.

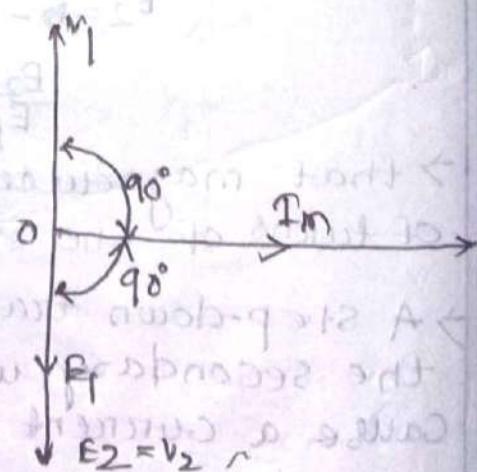
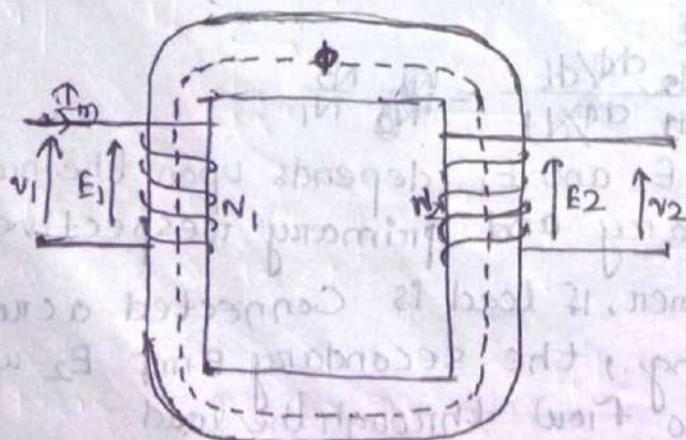
### Theory of An ideal transformer :-

An ideal ~~winding~~ transformer is one that has

- 1. No winding resistance
- 2. No leakage flux (i.e. the same flux links both the windings)
- 3. No iron losses (i.e. Eddy Current and hysteresis losses) in the core.

→ Practical transformers have properties that approach very close to an ideal transformer.

Consider, the ideal transformer on no load i.e. secondary is open-circuited.



- When the alternating voltage  $v_1$  is applied to the primary, it draws a small magnetic current  $I_m$  which lags behind the applied voltage by  $90^\circ$ .
- The alternating current  $I_m$  produces an alternating flux  $\phi$  which is proportional to and in phase with it.
- The alternating flux  $\phi$  links both the windings and induces e.m.f  $E_1$  in the primary and e.m.f  $E_2$  in the secondary.
- Both  $E_1$  and  $E_2$  lag behind flux  $\phi$  by  $90^\circ$ .
- In a pure inductive circuit, current lags behind the voltage by  $90^\circ$ .
- There are no iron losses, flux  $\phi$  is in phase with  $I_m$ .

### E.m.f Equation of a Transformer

Consider than an alternating voltage  $v_1$  of frequency  $f$  is applied.

(i) The sinusoidal flux  $\phi$  produced by the primary can be represented as

$$\phi = \phi_m \sin \omega t$$

The instantaneous e.m.f  $e_1$  induced in the primary.

$$E_{m1} = 2\pi f N_1 \phi_m$$

The r.m.s value of the primary e.m.f is

$$E_1 = \frac{E_{m1}}{\sqrt{2}} = \frac{2\pi f N_1 \phi_m}{\sqrt{2}}$$

$$E_1 = 4.44 f N_1 \phi_m$$

$$E_2 = 4.44 f N_2 \phi_m$$

$$E_1 = v_1 \text{ and } E_2 = v_2 \quad (\text{an ideal transformer})$$

### Voltage Transformation Ratio ( $k$ )

$$(i) \text{ Induced E.M.F} = \frac{E_2}{E_1} = \frac{v_2}{v_1} = \frac{N_2}{N_1} = k$$

the 'constant  $k$ ' is called voltage transformation ratio.

$$K=5 \quad (\text{i.e. } N_2/N_1=5) \text{ then } E_2 = 5E_1$$

for an ideal transformer:-

$$(i) E_1 = v_1 \text{ and } E_2 = v_2, \text{ there is no voltage drop in the windings.}$$

$$\frac{E_2}{E_1} = \frac{V_2}{V_1} = \frac{N_2}{N_1} = K$$

(ii) There are no losses,

therefore, volt-amperes input to the primary are equal to the output volt-amperes i.e.

$$V_1 I_1 = V_2 I_2 \quad \frac{V_2}{V_1} = \frac{I_1}{I_2} = K$$

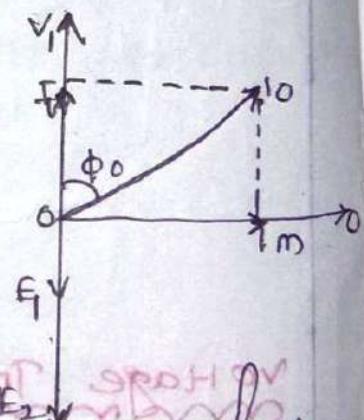
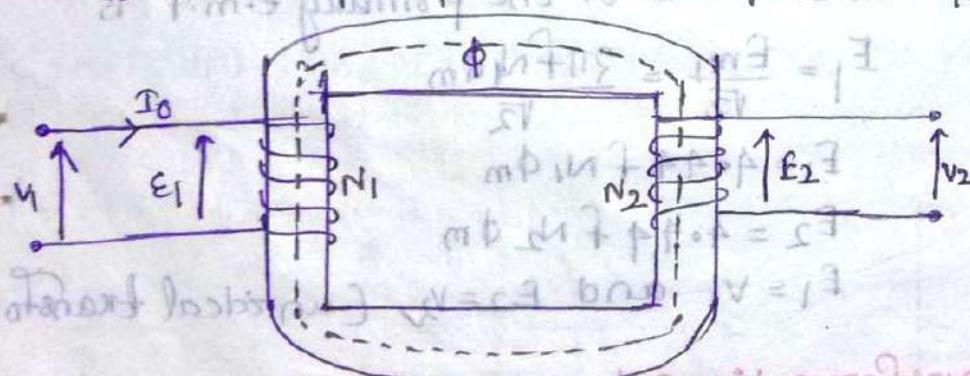
$$\frac{I_2}{I_1} = \frac{V_1}{V_2} = \frac{1}{K}$$

Hence, currents are in the inverse ratio of voltage transformation ratio.

### Practical Transformer on No load :

- Transformer on no load i.e. Secondary open circuit as shown in fig
- The primary will draw a small current  $I_0$  to supply
  - (i) the iron losses
  - (ii) a very small amount of copper loss in the primary
- Hence the primary no load current  $I_0$  is not  $90^\circ$  behind the applied voltage  $V_1$  but lags it by an angle  $\phi_0 < 90^\circ$

No load input power,  $W_0 = V_1 I_0 \cos \phi_0$



The no-load primary current  $I_0$  can be resolved into two rectangular components viz.

- (i) The component  $I_W$  in phase with the applied voltage  $V_1$ . This is known as active or working or iron loss component and supplies the iron loss and a very small Primary Copperloss

get n.g. expression on  $I_W = I_0 \cos \phi_0$

(ii) The Component  $I_m$  lagging behind  $V_1$  by  $90^\circ$  and is known as magnetising component. It is this component which produces the Mutual Flux  $\phi$  in the core.

$$I_m = I_0 \sin \phi$$

$I_a$  is phasor sum of  $I_m$  and  $I_w$

No Load P.F.  $I_0 = \sqrt{I_m^2 + I_w^2}$

No Load input power  $\rightarrow W_0 = I_0^2 R_{\text{iron}}$

### Practical Transformer on Load

Two cases :> (i) When such a transformer is assumed to have no winding resistance and leakage flux

(ii) When the transformer has winding resistance and leakage flux.

(i) No winding resistance and leakage flux.

→ Practical transformer with the assumption that resistances and leakage reactances of the winding are negligible.

Assumption,  $V_2 = E_2$  and  $V_1 = E_1$

Let us take the usual case of inductive load which causes the secondary current  $I_2$  to lag the secondary voltage  $V_2$  by  $\phi_2$ .

→ The total primary current  $I_1$  must meet two requirements

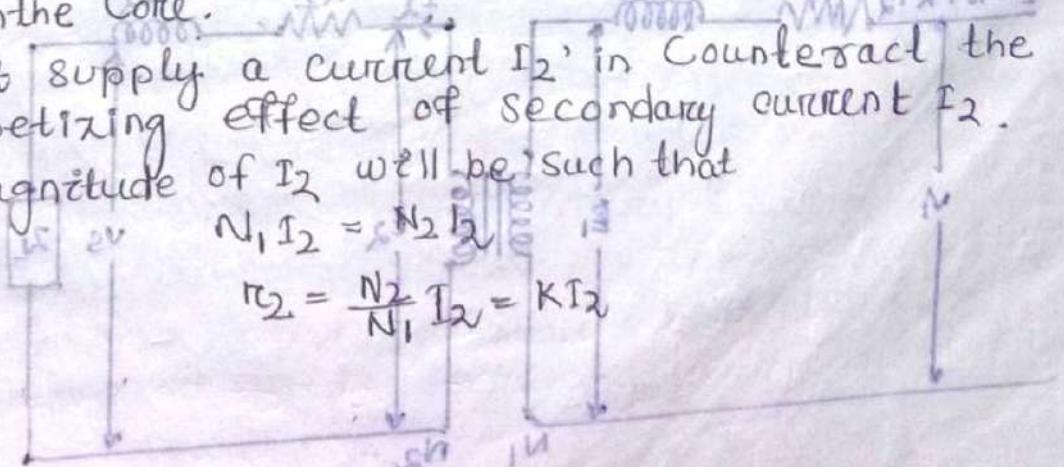
(a) It must supply the no load current  $I_0$  to meet the iron losses in the transformer and to provide flux in the core.

(b) It must supply a current  $I_2'$  in counteract the demagnetizing effect of secondary current  $I_2$ .

The magnitude of  $I_2'$  will be such that

$$N_1 I_2' = N_2 I_2$$

$$I_2' = \frac{N_2}{N_1} I_2 = K I_2$$



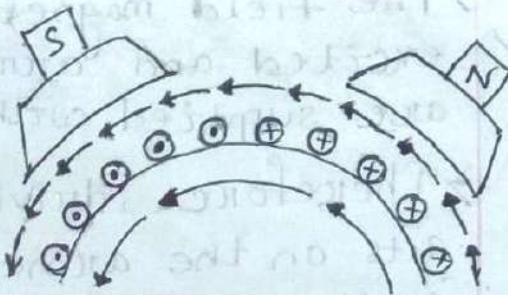
Defination

- A DC motor is an electrical machine that converts electrical energy into mechanical energy.
- Special applications such as in steel mills, mines and electric trains It is advantages to convert alternating current into Direct current in order to use DC Motor.
- The reasons is that speed/torque characteristics of dc motors are much more superior to that ac motor.
- D.C Motors are three types :-
  1. series-wound D.C Motor
  2. shunt-wound D.C Motor.
  3. compound-wound D.C Motor.

Working Principle of D.C Motor

- Operation of DC motor based on the principle when a current carrying conductor is placed in a magnetic field, the conductor experience a mechanical force.
- Direction of force the D.C motor working in Fleming's left hand rule.
- Fleming's left hand rule :- When a current-carrying conductor is placed in an magnetic field, the conductor experience a force perpendicular to both the field and to the direction of the current flow.
- If the fore finger indicates the direction of the magnetic field.
- The middle finger indicates the direction of the current and the thumb represents the direction of the motion.

- When the terminals of the motor are connected to an external source of dc supply.
1. The field magnets are excited developing alternate N and S pole.
  2. The armature conductors carry currents. All conductors under N-pole carry current in one direction while all conductors under S-pole carry currents in the opposite direction.
- Suppose the conductors under N-pole carry currents into the plane of the paper and those under S-pole carry currents out of the plane of the paper.
- Since each armature conductor is carrying current and is placed in the magnetic field, a mechanical force acts on it.
- That force on each conductor is tending to rotate the armature anticlockwise direction.
- All these forces add together to produce a torque which sets the armature rotating.
- When the conductor moves from one side of a brush to the other, the current in that conductor is reversed and at the same time it comes the influence of next pole which is opposite polarity.
- Consequently, the direction of force on the conductor remains the same.



### Back or counter E.M.F

- The armature conductors move through the magnetic field and hence e.m.f is induced in them as in a generator. The induced emf acts in a opposite direction to the applied voltage ( $V$ ) and is known as back or counter e.m.f. ( $E_b$ ).
- The back e.m.f 
$$E_b = \frac{P\phi ZN}{60A}$$

P - Number of poles,  $\phi$  - flux per pole

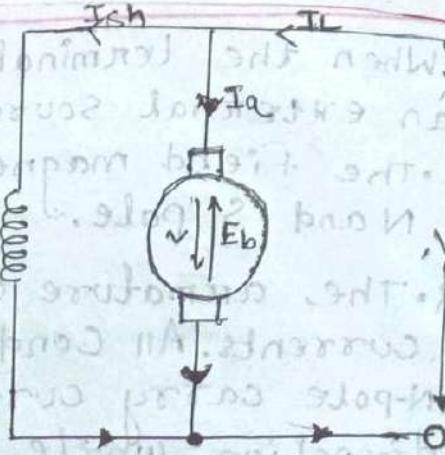
N - Speed,  $Z$  - Total number of conductors in the armature

→ Consider a shunt wound motor when dc voltage  $v$  is applied across the motor terminals.

→ The field magnets are excited and armature conductors are supplied with current  $I_a$ .

→ Therefore, driving torque acts on the armature which begins to rotate.

As the armature rotates, back emf  $E_b$  is induced which opposes the applied voltage  $v$ .



→ The applied Voltage  $v$  has to force current through the armature against the back emf.

→ The electric work done in overcoming and causing the current to flow again  $E_b$  is converted into mechanical energy developed in a d.c. motor.

→ Therefore, that energy conversion in a d.c. motor is only possible due to the production of back emf ( $E_b$ ).

$$\text{Net voltage across armature circuit} = v - E_b$$

$R_a$  is the armature circuit resistance,

then  $I_a = \frac{v - E_b}{R_a}$

where,  $I_a$  = Armature current

$v$  = applied voltage

$E_b$  = back emf

$R_a$  = Resistance of Armature

Since,  $v$  and  $R_a$  are usually fixed.

$E_b$  will determine the current drawn by the motor.

→ If the speed of the motor is high, the back emf  $E_b = (P \varphi Z N / 60 A)$  is large.

## Significance of Back emf

The presence of back e.m.f makes the dc motor a self-regulating machine.

It makes the motor to draw small armature current as it develops the torque required by the load.

$$\text{Armature current} - I_a = \frac{V - E_b}{R_a}$$

When the motor is running at no-load, small torque is required by the motor to overcome friction and windage losses. Therefore, a small current is drawn by the motor armature and the back emf is almost equal to the supply voltage.

If the motor is suddenly loaded, the load torque becomes greater than the armature torque and the motor starts to slow down.

As Motor speed decreases, back emf decreases and therefore, armature current starts increasing.

Armature torque increases and at some point it becomes equal to the load torque.

At that moment, motor stops slowing down and keeps running at this new speed.

If the load on the motor is decreased, the driving torque is momentarily in excess of the requirement so that armature is accelerated.

The armature speed increases; the back emf  $E_b$  also increases and causes the armature current to decrease.

The motor will stop accelerating will start rotating uniformly at this new slightly increased speed.

Therefore the back emf of dc motor regulates the flow of armature current i.e. automatically change the armature current to need the load requirement.

## Voltage Equation of D.C Motor.

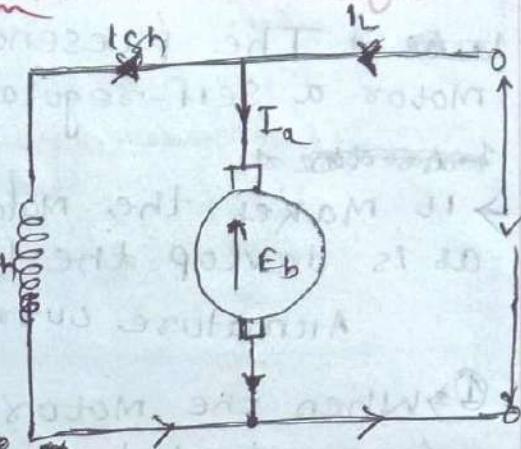
Let In a dc. motor

$V$  = applied voltage

$E_b$  - Back e.m.f

$R_a$  - Armature resistance

$I_a$  - Armature current



Since back emf ( $E_b$ ) acts in opposition to the applied voltage

(V)

→ the net voltage across the armature circuit is  $V - E_b$ .

$$\text{Armature current } (I_a) = \frac{V - E_b}{R_a}$$

$$\text{Voltage equation of DC Motor} \boxed{V = E_b + I_a R_a}$$

## Power Equation of DC Motor

→ Multiplied current in voltage equation.

$$V I_a = E_b I_a + I_a^2 R_a \quad (\because P = VI)$$

$$\boxed{\Rightarrow V I_a = E_b I_a + I_a^2 R_a}$$

this is power equation of DC Motor.

Where  $V I_a$  = electric power supplied to armature

$E_b I_a$  = power developed by armature (Armature Input)

$I_a^2 R_a$  = electric power wasted in armature (Armature output)

$P_{aRa}$  = electric power wasted in armature (Armature cu loss)

The efficiency of the motor is the ratio of the useful power output to the total input power. i.e., Efficiency =  $\frac{\text{useful power}}{\text{total input power}}$

## Condition for Maximum Power

The Mechanical power developed by the motor is

$$P_m = E_b I_a$$

$$\text{Now } P_m = V I_a - I_a^2 R_a$$

Since  $V$  and  $R_a$  fixed,

Power developed by the motor depends upon armature current, for maximum power  $dP_m/dI_a$  should be zero

$$\text{t.e., } \frac{dP_m}{dI_a} = 0$$

$$\Rightarrow V - 2I_a R_a = 0$$

$$\Rightarrow V = 2I_a R_a \Rightarrow I_a R_a = \frac{V}{2}$$

then, voltage eqn of DC motor =  $V = E_b + I_a R_a$

$$V = E_b + \frac{V}{2}$$

$$E_b = \frac{V}{2}$$

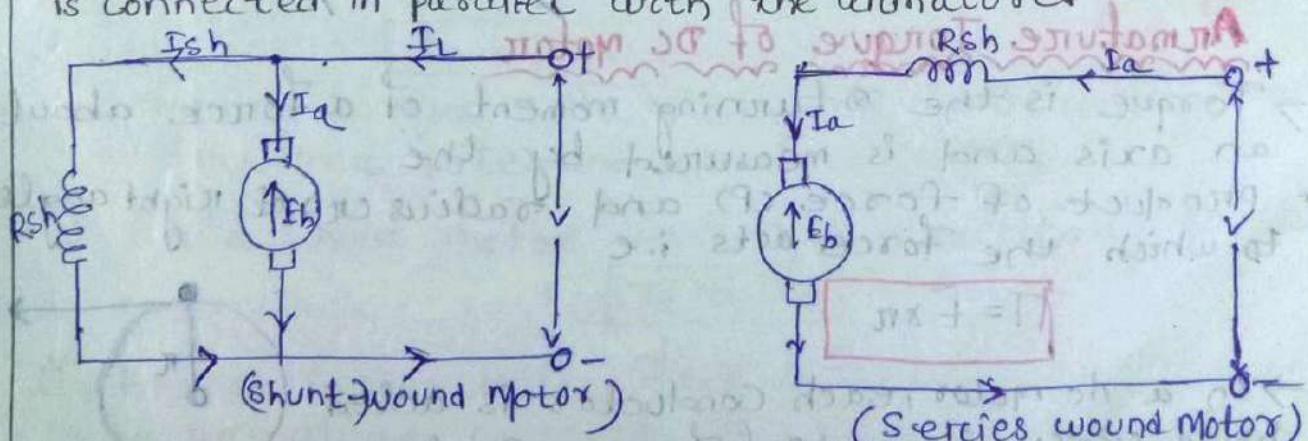
Hence mechanical power developed by the motor is maximum when back e.m.f is equal to half the applied voltage.

## Types of D.C. Motor

These are three types to

### (i) Shunt-wound Motor

→ ~~homothetic~~ Shunt-wound motor in which the field winding is connected in parallel with the armature.



### Series-wound Motor

→ Series wound motor in which the field winding is connected in series with the armature.

### (iii) Compound Wound Motor

→ Compound wound Motors has two field windings.

1. one connected parallel with armature

2. other connected series with armature

Compound wond motor are 2 types connection.

1. Short-shunt Connection.

2. Long-shunt Connection.

#### Short-shunt Connection

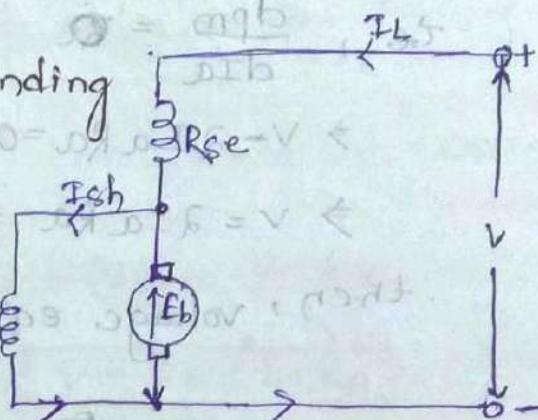
→ When the shunt field winding

is directly connected

across the armature

terminals.. is called

Short-shunt Connection.



#### Long-shunt connection

→ When the shunt field

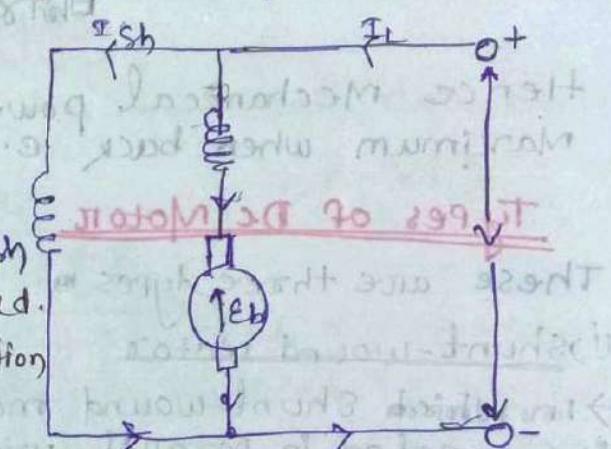
winding is so connected

that it shunts the

series combination of

armature and series field.

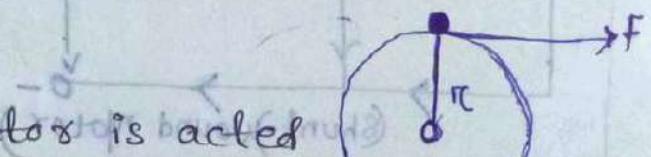
is called long-shunt connection



#### Armature Torque of DC motor

→ Torque is the turning moment of a force about an axis and is measured by the product of force ( $F$ ) and radius ( $r$ ) at right angle to which the force acts i.e

$$T = F \times r$$



→ In a dc motor, each conductor is acted

by a circumferential force ( $F$ ) at a

distance  $r$ , the radius of the armature.

→ The sum of the torques due to all armature conductors is known as gross or armature torque ( $T_a$ )

Let in a d.c. motor.  $r$  = average radius of armature.

$l$  = Effective length of each conductor

$Z$  = Total Number of armature Conductors

$A$  = Number of parallel path.

$i$  = Current in each Conductor =  $I_a/A$

$B$  = average flux density in  $\text{wb/m}^2$

$\phi$  = flux per pole  $\text{wb}$

$P$  = Number of poles.

Force on each conductor,  $F = BiL$  newtons.

Torque due to one conductor =  $F \times r$  newton.metre

Total armature torque,  $T_a = Z F r$  newton-metre.

Now  $i = I_a/A$ ,  $B = \phi/a$  where  $a$  is the  $\pi$ -sectional area

of flux path/pole at radius.

$$a = \frac{2\pi r l}{P}$$

$$T_a = Z \times \left(\frac{\phi}{a}\right) \times \left(\frac{I_a}{A}\right) \times l \times r$$

$$= Z \times \frac{\phi}{\frac{2\pi r l}{P}} \times \frac{I_a}{A} \times l \times r$$

$$= \frac{Z \phi I_a P}{2\pi A}$$

$$T_a = 0.157 Z \phi I_a (P/A) \text{ Newton-met}$$

Since  $Z$ ,  $P$  and  $A$  are fixed for a given machine

$$T_a \propto \phi I_a$$

Hence torque in a d.c. motor is directly proportional to flux per pole and armature current.

(i) For a shunt motor, flux  $\phi$  is practically constant

$$T_a \propto I_a$$

(ii) For a series motor, flux  $\phi$  is directly proportional to armature current  $I_a$  provided magnetic saturation does not take place.

$$T_a \propto I_a^2$$

$$E_b = \frac{P\phi Z N}{60 A}$$

$$\frac{P\phi Z N}{A} = \frac{60 \times E_b}{N}$$

for eq (i), we get the expression of  $T_a$  as

$$T_a = 0.159 \times \left( \frac{60 \times E_b}{N} \right) \times I_a$$

$$T_a = 9.55 \times \frac{E_b I_a}{N} \text{ N-m}$$

### Shaft Torque

→ The torque which is available at the motor shaft for doing useful work is known as shaft torque.

Shaft torque  $T_{sh}$  is somewhat less than the total armature torque  $T_a$ . The difference  $T_a - T_{sh}$  is known as lost torque.

$$T_{sh} = 9.55 \times \frac{\text{output}}{N} \text{ N-m}$$

Lost torque =  $9.55 \times$  iron and friction loss

### Speed of a D.C. Motor

$$E_b = V - I_a R_a \quad (i)$$

$$E_b = P\phi Z N / 60 A \quad (ii)$$

$$\frac{P\phi Z N}{60 A} = V - I_a R_a$$

$$N = \frac{(V - I_a R_a)}{\Phi} \cdot \frac{60 A}{P Z}$$

$$N = K \frac{(V - I_a R_a)}{\Phi} \quad \text{where } K = \frac{60 A}{P Z}$$

$$V - I_a R_a = E_b$$

$$N = K \frac{E_b}{\Phi}$$

$$N \propto \frac{E_b}{\Phi}$$

Therefore in a d.c. motor speed is directly proportional to back emf  $E_b$  and inversely proportional to flux per pole  $\Phi$ .

## Speed Relations

If a d.c motor has initial values of speed, flux per pole and back emf. as  $N_1, \phi_1$  and  $E_1$

$$N_1 \propto \frac{E_{b1}}{\phi_1} \text{ and } N_2 \propto \frac{E_{b2}}{\phi_2}$$

$$\frac{N_1}{N_2} = \frac{E_{b1}}{E_{b2}} \times \frac{\phi_2}{\phi_1}$$

(i) For a shunt motor flux practically remains constant so that  $\phi_1 = \phi_2$

$$\frac{N_1}{N_2} = \frac{E_{b1}}{E_{b2}}$$

(ii) For a series motor  $\phi \propto I_a$  prior to saturation

$$\boxed{\frac{N_1}{N_2} = \frac{E_{b1}}{E_{b2}} \times \frac{I_{a2}}{I_{a1}}}$$

$I_{a1}$  = Initial armature current

$I_{a2}$  = Final armature current

## Speed Regulation

→ The speed regulation of a motor is the change in speed from full-load to no-load

$$\therefore \text{speed regulation} = \boxed{\frac{N_{o-L} \text{ speed} - F.L \text{ speed}}{F.L \text{ speed}} \times 100}$$

$$= \frac{N_o - N}{N} \times 100$$

$N_o$  = No load speed

$N_f$  = full load speed.

$\Delta V = \text{in parallel load}$

$\Delta V = \text{in series load}$

$\Delta V = \text{in shunt load}$

## Losses in a D.C motor

practical losses

The losses occurring in a d.c motor are the same as in d.c generator.

- (i) Copper losses
- (ii) Mechanical losses
- (iii) Iron losses.

As in a generator these losses cause.

1. an increase of temperature.
2. Reduction in efficiency of the D.C Motor.

## Efficiency of D.C Motor

A dc generator, the efficiency of a d.c motor is the ratio of output power to the input power.

$$\text{Efficiency, } \eta = \frac{\text{Output}}{\text{Input}} \times 100$$

$$= \frac{\text{Output}}{\text{Output + losses}} \times 100$$

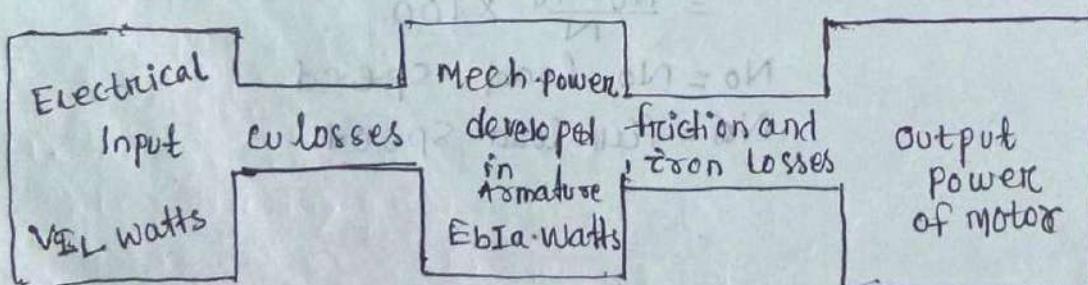
for a generator, the efficiency of a d.c motor will be maximum when:

variable losses = constant losses.

## Power stages

A - B = Copper losses

B - C = Iron and friction losses



overall efficiency  $\eta_c = C/A$

Electrical efficiency  $\eta_e = B/A$

Mechanical efficiency  $\eta_m = C/B$

## D.C Motor Characteristics

→ The performance of a d.c motor can be judged from its characteristic curves known as motor characteristics.

D.C motor characteristics is three types : →

### 1. Torque and Armature Current characteristic →

→ The curve between armature torque & armature current  $I_a$  of a dc motor. It is also known as electrical characteristic of the motor.

### 2. Speed and armature current characteristic : →

→ If the curve between speed ( $N$ ) and armature Current  $I_a$  of a d.c motor.

→ It is very important characteristic.

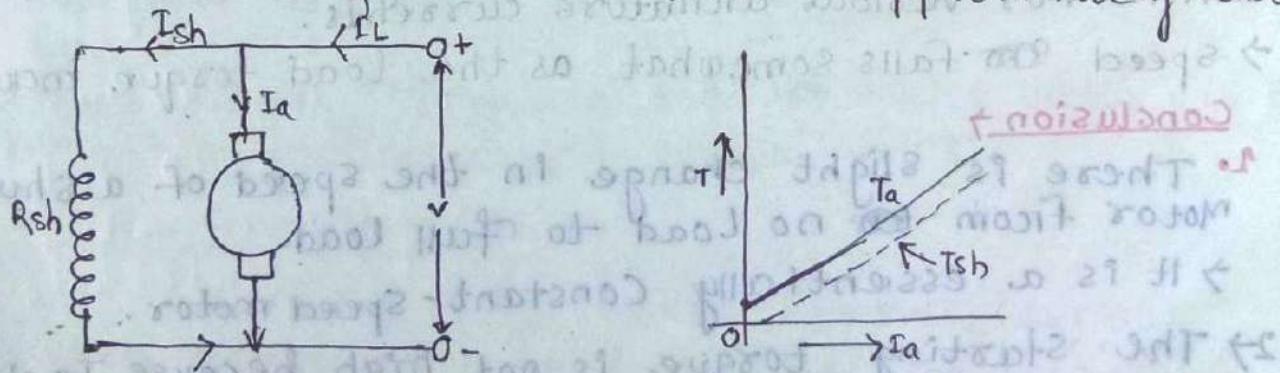
### 3. Speed and torque characteristic : →

→ It is the curve between Speed ( $N$ ) and armature torque  $T_a$  of a d.c motor. It is also known as mechanical characteristic.

## Characteristics of D.c shunt Motors

→ The Connection of a d.c motor. The field current  $I_{sh}$  is constant since the field winding is directly connected to the supply voltage  $V$ . is to be constant.

→ The ~~shaft~~ flux in a Shunt Motor is -approximately constant.



(i)  $T_a/I_a$  characteristic :.  $T_a \propto I_a$

→ Motor for is operating from a constant supply voltage. flux  $\phi$  is constant.

→  $T_a/I_a$  characteristic is a straight line passing through the origin.

→ Shaft torque is less than  $T_a$ -(as dotted line)

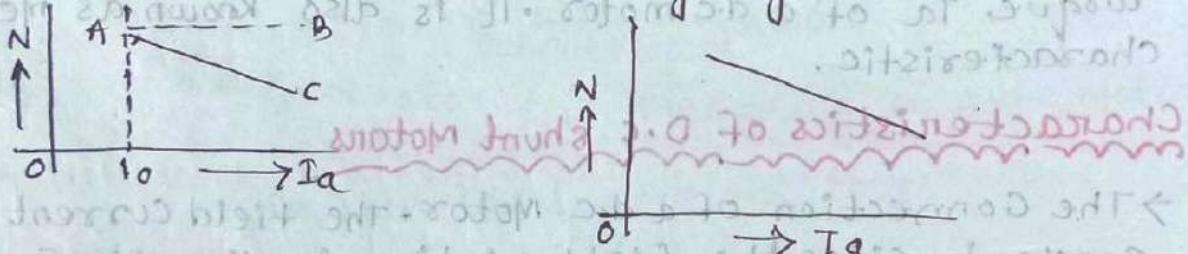
- Shunt Motor should not be started on heavy load.
- The curve that a very large current is required to start a heavy load.

### (ii) N/I<sub>a</sub> characteristic →

← The speed N of a Motor is given by

$$N \propto \frac{E_b}{a}$$

- The flux ( $\phi$ ) and back emf ( $E_b$ ) in a shunt motor are almost constant under normal condition.
- Speed of a shunt motor will remain constant as the armature current varies.
- When load is increased,  $E_b$  &  $\phi$  decrease due to the armature resistance drop and armature reaction respectively.
- $E_b$  decreases slightly more than  $\phi$  so that the speed of the motor decreases slightly with load.



### (iii) N/T<sub>a</sub> characteristic →

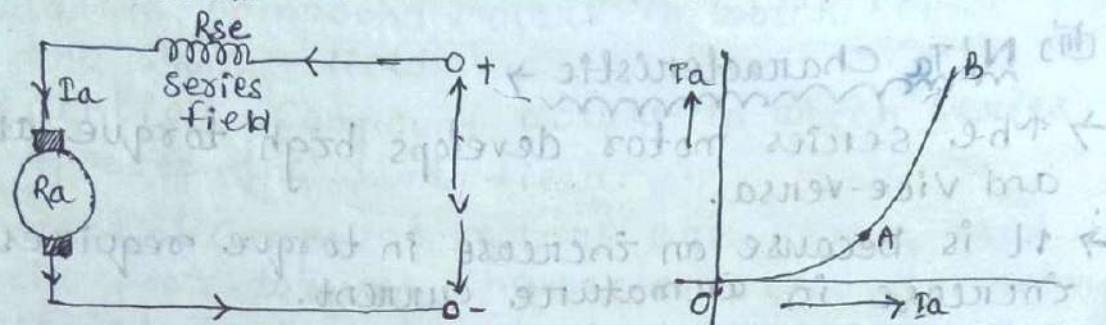
- This curve is obtained by plotting the values of N and  $T_a$  for various armature currents.
- Speed falls somewhat as the load torque increases.

#### Conclusion ↴

1. There is slight change in the speed of a shunt motor from no load to full load.  
→ It is an essentially Constant-Speed motor.
2. The starting torque is not high because  $T_a \propto I_a$ .

## Characteristics of D.C Series Motors. :-

- The connection of a d.c series motor. If the mechanical load on the motor increase, the armature current also increases.
- The flux in a series motor increase with the increase in armature Current and vice-versa.



### (i) \$T\_a/I\_a\$ characteristic :-

We know  $T_a \propto I_a$   
magnetic saturation -  $\phi \propto I_a$  so that  $T_a \propto I_a^2$   
After magnetic saturation  $\phi$  is constant so that  $T_a \propto I_a$

- Thus upto magnetic saturation, the armature torque is directly proportional to the square of armature current. If \$I\_a\$ is doubled, \$T\_a\$ is almost quadrupled.
- \$T\_a/I\_a\$ curve upto magnetic saturation is a parabola.
- After magnetic saturation from, torque is directly proportional to the armature current.
- Therefore \$T\_a/I\_a\$ curve after magnetic saturation is a straight line.
- The starting Torque of a dc series motor will be very high as compared to a shunt motor.

### (ii) \$N/I\_a\$ characteristic →

speed \$N \propto \frac{E\_b}{\phi}\$ where \$E\_b = V - I\_a(R\_a + R\_{sh})\$

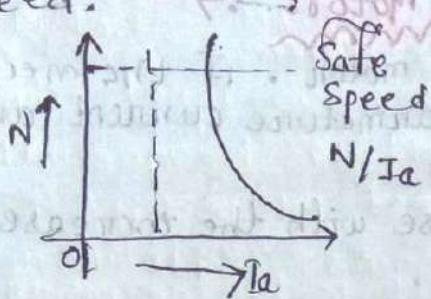
- When armature current increases, the back emf (\$E\_b\$) decreases due to \$I\_a(R\_a + R\_{sh})\$ drop while flux \$\phi\$ increases.

→ \$N \propto \frac{1}{\phi}\$  
\$\propto \frac{1}{I\_a}\$ upto magnetic saturation.

- upto magnetic saturation, the \$N/I\_a\$ curve follows the hyperbolic path.

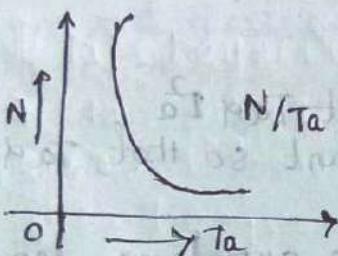
- After saturation, the flux becomes constant and so does the

Speed.



### (iii) $N/I_a$ Characteristic

- The series motor develops high torque at low speed and vice-versa.
- It is because an increase in torque requires an increase in armature current.



### Conclusion

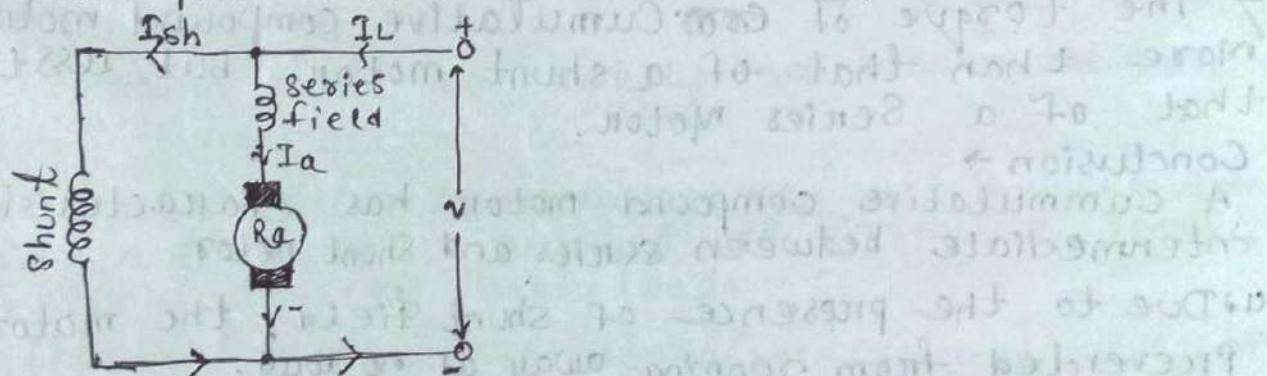
- (i) It has a high starting torque because initially  $T_a \propto I_a^2$ .
- (ii) It is variable speed motor.
- (iii) Thus if the load decreases, its speed is automatically raised and vice-versa.
- (iv) At no load, the armature current is very small and so is the flux.
- (v) The speed rises to an excessive high value.
- (vi) This is dangerous for the machine which may be destroyed due to centrifugal forces.
- (vii) A series motor should never be started on no load.  
→ However, to start a series motor, mechanical load is first put and then the motor is started.

### Compound Motors :-

- A compound motor has both series field and shunt field.
- The shunt field is always stronger than the series field.
- Compound are two types :-
- (i) Cumulative - compound motors in which series field aids the shunt field.
- (ii) Differential - compound motors in which series field opposes the shunt field.
- Differential - compound motors are rarely used due to their poor torque characteristics at heavy loads.
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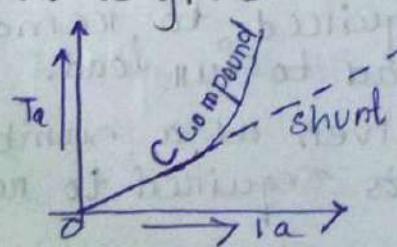
### Characteristics of cumulative compound motors :-

- Each pole carries a series as well as shunt field winding.



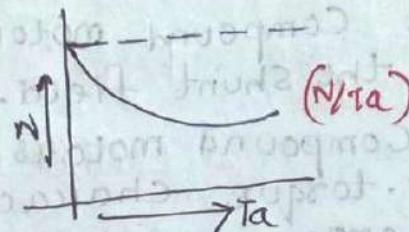
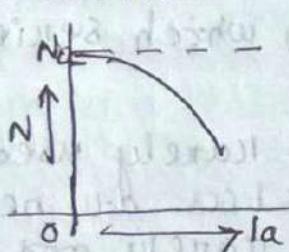
#### (i) $T_a/I_a$ Characteristic :-

- As the load increases, the series field increases but shunt field strength remains constant.
- Total flux increased and hence the armature torque.
- It may be noted that torque of a cumulative compound motor is greater than that of shunt motor for a given armature current due to series field.



(ii)  $N/I_a$  characteristic:

- The load increases, the flux per pole also increases.
- The speed of the motor falls as the load increases.
- It may be noted that torque of Cumulative-compound motor is greater than that of Shunt motor for a given armature current due to series.



(iii)  $N/T_a$  characteristic:

→  $N/T_a$  characteristic of a Cumulative Compound Motor.

→ The torque of Cumulative compound motor is more than that of a shunt motor but less than that of a Series Motor.

Conclusion →

A cumulative compound motor has characteristics intermediate between series and shunt motor.

i) Due to the presence of shunt field, the motor is prevented from running away at no load.

ii) Due to the presence of series field, the starting torque is increased.

→ Application of D.C Motor

Shunt motor → App characteristics of a shunt motor reveal that it is an approximately constant speed motor.

→ used : i) Where the speed is required to remain almost constant from no load to full load.

ii) Where the load has to be driven at a number of speeds and any one of which is required to remain nearly constant.

Industrial use : Laths, drills, boring mills, shapers, spinning and weaving machine.

(ii) Series Motor :

- It is variable speed motor.
- Speed is low at high torque and vice-versa.
- However at light or no load, the motor tends to attain dangerously high speed.
- The motor has a high starting torque.

- Used →
- (i) Where large starting torque is required in elevators and electric traction.
  - (ii) Where the load is subjected to heavy fluctuations and the speed is automatically required to reduce at high torques and vice-versa.

Industrial use :

Electric traction, cranes, elevators, air compressors, vacuum cleaners, hair dryers, sewing machines.

(iii) Compound Motors :

- Compound motors are rarely used because of their poor torque characteristics.
- Cumulative-Compound motors are used where a fairly constant speed is required with irregular loads or suddenly applied heavy loads.

Industrial use : presses, shears, reciprocating machines.

Speed control of D.C. Motors :

The speed of a d.c. motor is given by

$$N \propto \frac{E_b}{\phi}$$

$$N = K \frac{(V - I_a R)}{\phi} \text{ r.p.m}$$

$R = R_a$  (for shunt motor)

$R_a + R_{se}$  (for series motor)

Two main methods of controlling the speed of a d.c. motor are:

(i) By varying the flux per pole ( $\phi$ ). This is known as Flux Control method.

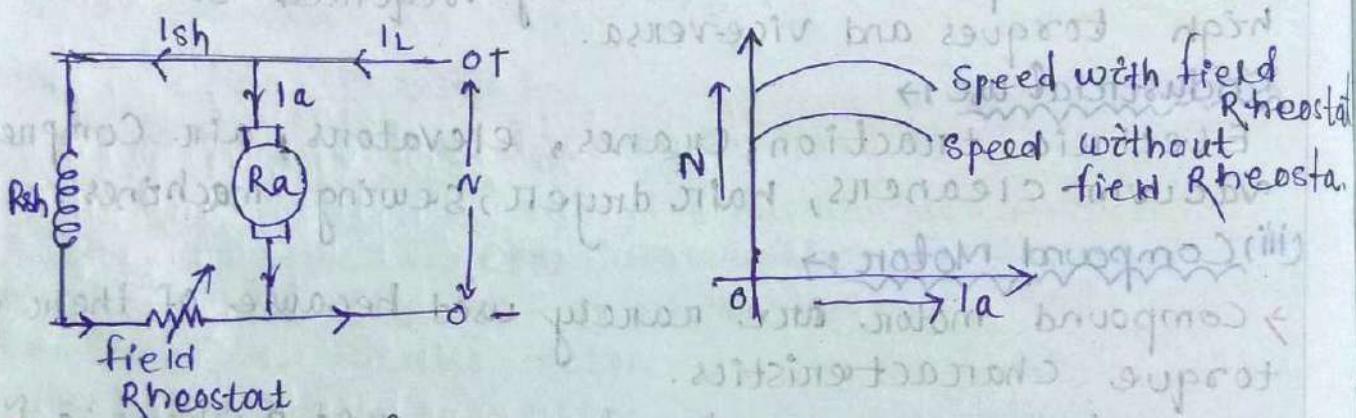
(ii) By varying the resistance in the armature circuit. This is known as armature control method.

## Speed Control of D.C Shunt Motors :

- The speed of a shunt motor can be changed by
  - flux control method.
  - Armature control method.

### Flux-Control Method:

- It is based on the fact that by varying the flux  $\Phi$ , the motor speed ( $N \propto \frac{1}{\Phi}$ ) can be changed and hence that name flux control method.
- In this method, a variable resistance known as shunt field rheostat.



- The shunt field rheostat reduces the shunt field current  $I_{sh}$  and flux  $\Phi$ .
- Therefore, we can only raise the speed of the motor above the normal speed.
- Generally this method permits to increase the speed in the ratio  $3 : 1$ .

### Advantages:

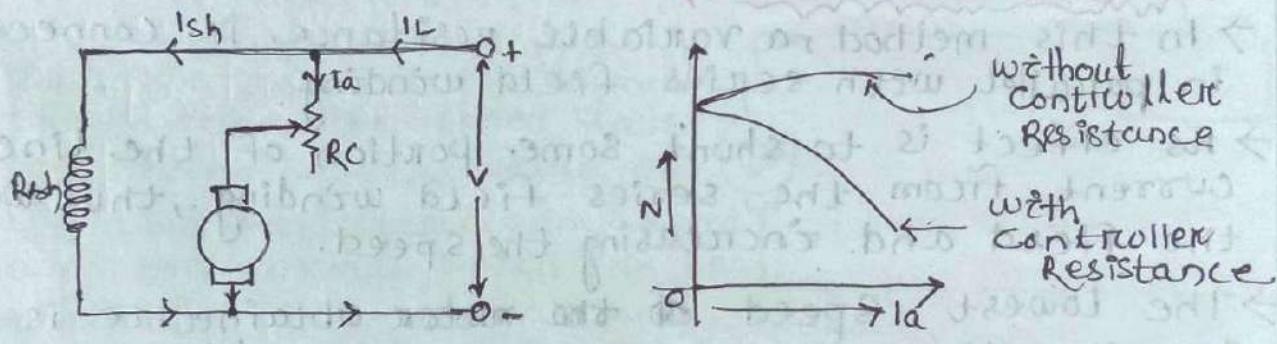
- This is an easy and convenient method.
- It is an inexpensive method since very little power is wasted in the shunt field rheostat due to relatively small value of  $I_{sh}$ .
- The speed control exercised by this method is independent of load on the machine.

### Disadvantages :

- (i) only speeds higher than the normal speed can be obtained since the total field circuit resistance cannot be reduced below  $R_{sh}$  - the shunt field winding resistance.
- (ii) There is a limit to the maximum speed obtainable by this method.

### Armature Control Method :

- This method is based on the fact that by varying the voltage available across the armature.
- The back e.m.f. and hence the speed of the motor can be changed.
- This is done by inserting a variable resistance  $R_C$  in series with the armature.



$$N \propto V - I_a(R_a + R_C)$$

$R_C$  = Controller resistance.

- Due to voltage drop in the controller resistance, the back emf is decreased. Since  $N \propto E_b$ , the speed of the motor is reduced.
- The highest speed obtainable is that corresponding to  $R_C = 0$ .. (Normal Speed)
- This method can only provide speeds below the normal speed.

### Disadvantages :

- A large amount of power is wasted in the controller resistance since it carries full armature current  $I_a$ .
- The output and efficiency of the motor are reduced.
- This method results in poor speed regulation.

→ The speed varies widely with load since the speed depends upon the voltage drop.

### Speed Control of DC

→ This method is seldom used to control the speed of shunt motors.

### Speed Control of D.C Series Motors →

→ The speed control of dc series motors can be obtained by (i) flux control method. (ii) armature-resistance control method.

#### (i) Flux Control Method →

→ This method, flux produced by the series motor is varied and hence the speed.

The variation of flux can be achieved - 2 ways

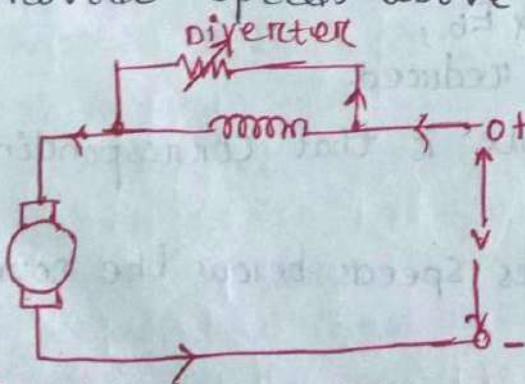
#### 1. Field Diverters →

→ In this method, a variable resistance is connected in parallel with series field winding.

→ Its effect is to shunt some portion of the line current from the series field winding, thus weakening the field and increasing the speed.

→ The lowest speed obtainable is that corresponding to zero current is the diverter.

→ The lowest speed obtainable is the normal speed of the motor, consequently, this method can only provide speeds above the normal speed.



#### 2. Armature diverters →

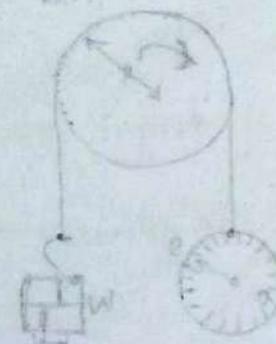
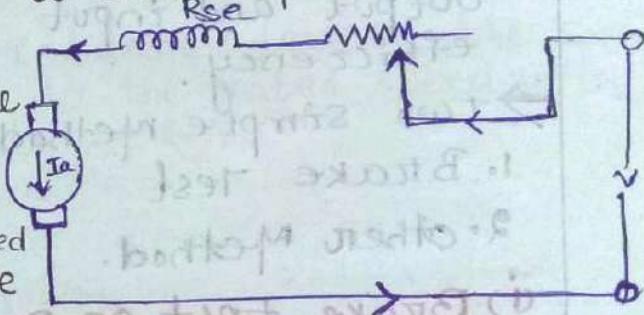
→ A variable resistance is connected in parallel with the armature.

→ The diverter shunts some of the line current, thus reducing the armature current.

- If  $I_a$  is decreased, the flux  $\phi$  must increase.
  - Since  $N \propto 1/\phi$ , the motor speed is decreased by adjusting the armature diverter.
  - Any speed lower than the normal speed can be obtained.
- Tapped-field Control:
- The flux is reduced by decreasing the number of turns of the series field winding.
  - Full turns of the field winding, the motor runs at normal speed and as the field turns are cut-out, speeds higher than normal speed are achieved.

(ii) Armature-resistance control:

- In this method, a variable resistance is directly connected in series with the supply to the complete motor.
- This reduces the voltage available across the armature and hence the speed falls.
- By changing the value of variable resistance, any speed below the normal speed can be obtained.
- This is the most common method employed to control the speed of D.C. series motors.



Calculation of Efficiency when the machine is generating on Load.

$$\text{Power input} = VI$$

Armature copper loss,

$$P_{cu} = I_2 R_a = (I + I_{sh})^2 R_a$$

Constant losses

$$W_C = VIO - (I_0 - I_{sh})^2 R_a$$

$$\text{Total losses} = P_{cu} + W_C$$

∴ Efficiency of the generator.

$$\eta = \frac{\text{Output}}{\text{Input}} = \frac{\text{Input} - \text{Losses}}{\text{Input}} = \frac{VI - (P_{cu} + W_C)}{VI}$$

Efficiency By Direct Loading method:

→ In this method, the DC machine is loaded and output and input are measured to find the efficiency.

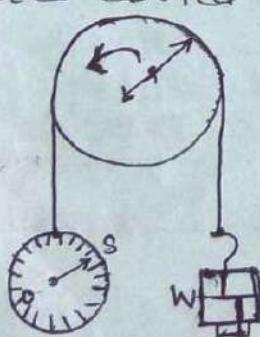
→ two simple methods can be used.

1. Brake Test

2. Other Method.

(i) Brake test on DC Machines.

→ In this brake test on DC machines a brake is applied to a water-cooled pulley mounted on the motor shaft.



→ One end of the rope is fixed to the floor via a spring balance and a known mass is suspended at the other end.

→ If the spring balance reading is kg-wt and the suspended mass has a weight of W kg-wt

Net pull on the rope = (W - s)

$$\text{kg-wt} = (W - s) * 9.81 \text{ Newtons}$$

If r is the radius of the pulley in meters, then the shaft torque  $T_{sh}$  developed by the motor is

$$T_{sh} = (W - s) * 9.81 * r \text{ N-m}$$

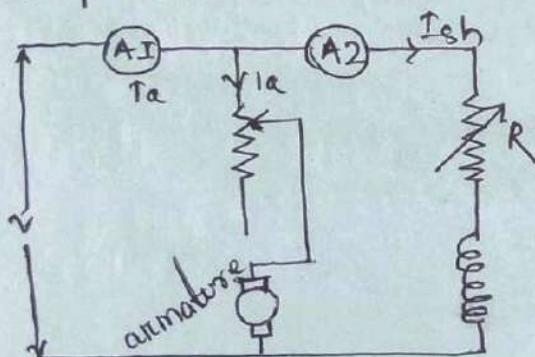
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If the speed of the pulley is N r.p.m then,

$$\begin{aligned}\text{output power} &= 2 \cdot 3 \cdot 14 N T_{sh} / 60 \\ &= 3.14 N \times (W-S) 9.81 \times H\end{aligned}$$

### Swinburne's Test method :-

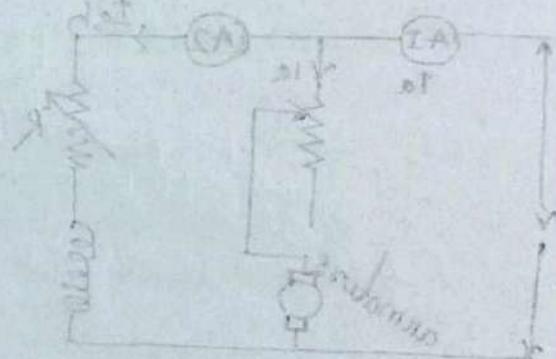
- This method is an indirect method of testing a DC machine.
- Swinburne's Test is the most commonly used and simplest method of testing of shunt and compound wound DC machines.
- In this test the efficiency of the machine at any load is pre-determined.
- In this method of testing no load losses are measured separately and eventually we can determine the efficiency.
- The Ckt connection for swinburne's test is the speed of the machine is adjusted to the rated speed with the help of the shunt regulator R.



- The Swinburne's test no load power input is only required to supply the losses.
- The losses occur in the machine mainly are:-
  1. Iron losses in the core
  2. Friction and windings losses
  3. Armature Copper loss.
- No load mechanical output of the machine is zero in Swinburne's test, the no load input power is only used to supply the losses.

## Disadvantages of swinburne's Test

1. Iron loss is neglected through there is change in iron loss from no load to full load due to armature reaction.
2. We cannot be sure about the satisfactory commutation on loaded condition because the test is done on no-load.
3. We can't measure the temperature rise when the machine is loaded. power losses can vary with the temperature.
4. In DC series motors, the swinburne's cannot be done to find its efficiency as it is a no load test.



## CHAPTER-01

# D.C. GENERATOR

### 1.1. Operating Principle of generator.

An electric generator is a machine that converts mechanical energy into electrical energy.

- Whenever flux is cut by a conductor, an emf is induced which will cause a current to flow if the conductor circuit is closed.
- The direction of induced emf. is given by 'Fleming's right hand rule'.
- Essential components of a generator are,  
(i) a magnetic field.  
(ii) Conductor or a group of conductors.  
(iii) Motion of conductor with respect to magnetic field.

Fleming's right hand rule :-

- Stretch the thumb, fore-finger and middle finger and middle fingers of your right hand so that they are at right angles to each other.
- If the fore-finger points in the direction of field, thumb in the direction of motion of the conductor, then middle finger will point in the direction of induced emf.

### 1.2 Construction of D.C. generator :-

- The d.c. generator and d.c. motor have the same general construction.

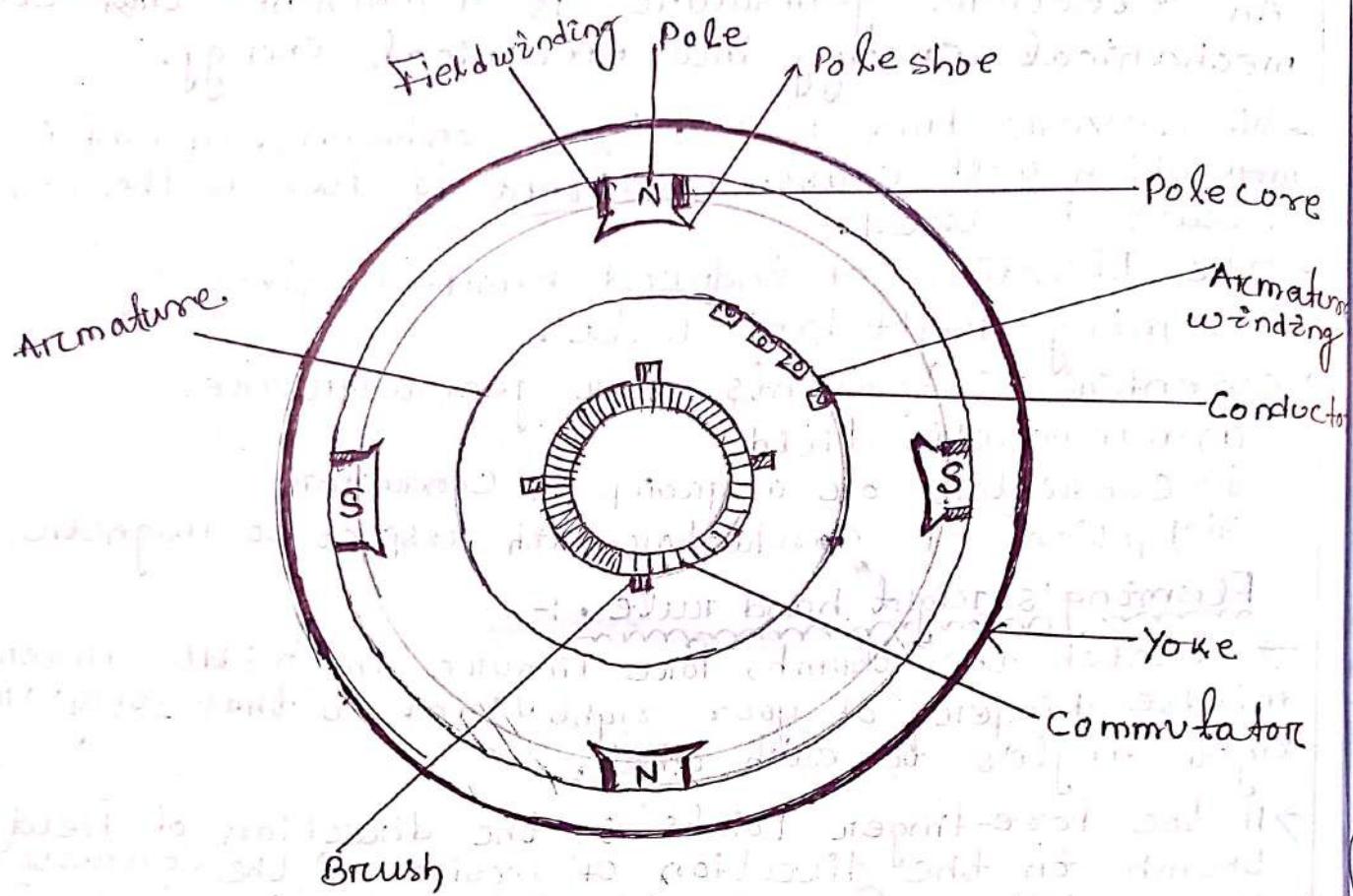
- All d.c. machines have principal components are :-  
(i) field system (ii) armature core (iii) armature winding  
(iv) commutator (v) brushes.

#### (i) Field System :-

- The function of the field system is to produce uniform magnetic field within which the armature rotates.
- Number of salient poles bolted to the inside of circular frame (generally called Yoke)
- The yoke is usually made of solid cast steel whereas the pole pieces are composed of stacked laminations.
- Field coils are mounted on the poles and carry the d.c exciting current.

### (iii) Armature Core :-

→ The armature core is keyed to the machine shaft and rotates between the field poles.



### (iv) Armature winding Conductors :-

→ The slots of the armature core hold insulated conductors that are connected in a suited manner. This is known as armature winding.

→ This is the winding which is working emf is induced.  
→ The armature conductors are connected in series so as to increase the voltage in parallel path so as to increase the current.

### (v) Commutator :-

→ A commutator is a mechanical rectifier, which converts the alternating voltage generated in the armature winding into direct voltage across the brushes.  
→ The commutator is made up copper segments insulated from each other by mica sheets.

### (v) ~~Brushes~~ Brushes.

→ The propose of brushes is to insure electrical connections between the rotating Commutator and stationary external load circuit.

→ The ~~brushes~~ brushes are made of carbon and rest on the Commutator. The brushes pressure is adjusted by means of adjustable springs.

### Types of Armature winding:

There are two types of simple drum winding.

1. Simple Wave winding.

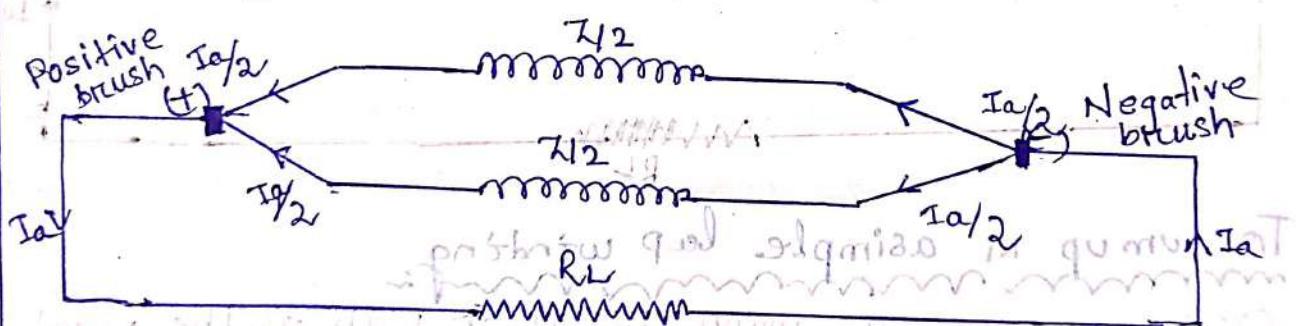
2. Simple Lap winding.

### Simple Wave Winding

→ In the arrangement the armature coil are connected in series through commutator segments in such a way that the armature winding is divided into two parallel paths.

→ If there are  $Z$  Armature conductor then  $Z/2$  conductor will be in series in each parallel path.

→ Each parallel path will carry a current  $I_a/2$  where  $I_a$  is the total armature current.



To sum up in a simple wave winding.

(a) There are two parallel path irrespective of number of poles of the machine.

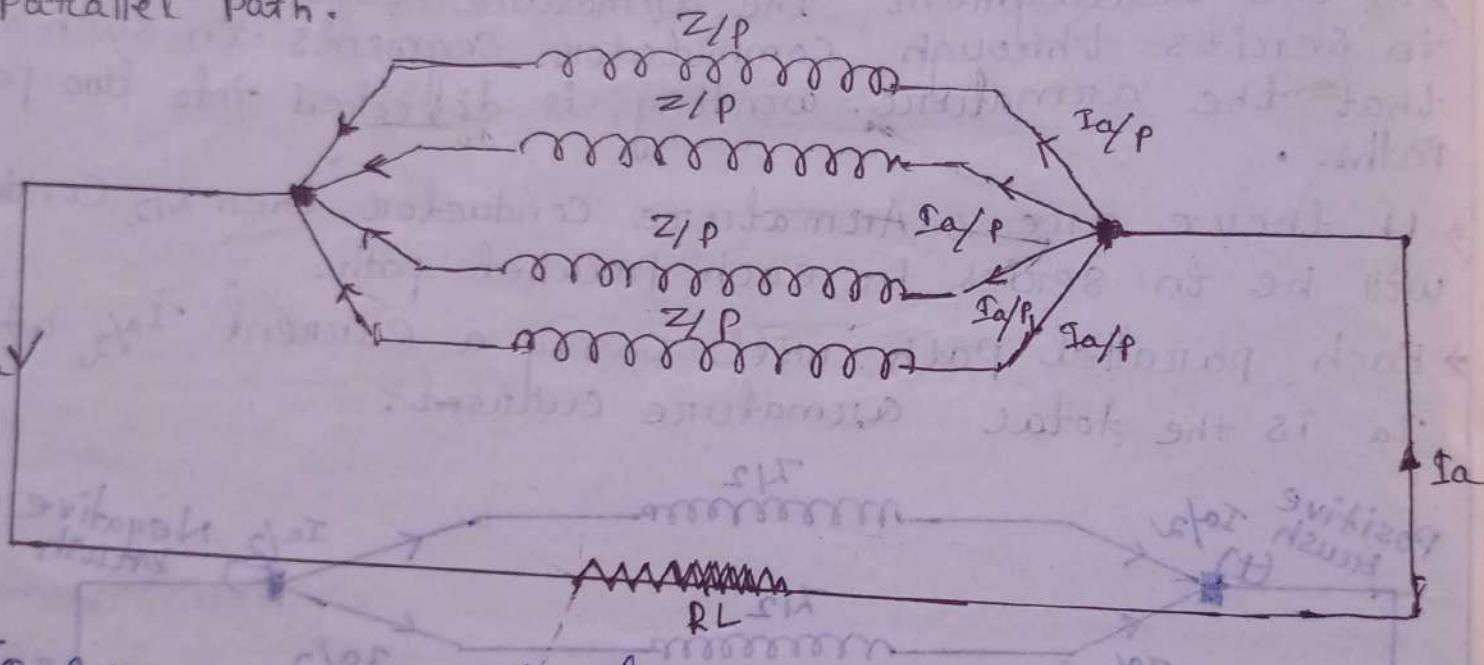
(b) Each parallel path has  $Z/2$  conductor in series.  $Z$  being total armature winding.

(c) EMF Generated =  $\frac{EMF}{\text{Number of parallel path}}$ .

(d) Total armature current  $I_a = 2 \times \text{Current/parallel path}$ .

## Simple lap winding.

- In this arrangement coils are connected in series through commutator segments in such a way that the armature winding is divided into as many parallel paths as the number of poles of the machine.
- If the  $Z$  conductors and  $P$  poles than there will be parallel path each containing  $Z/p$  conductors in series.
- Each path will carry a current of  $I_a/p$  where  $I_a$  is the total armature current.
- Here it is assumed that  $P=4$  so that there are 4 parallel path.



To sum up in a simple lap winding

- There are as many parallel path as the number of poles of the machine.
- Each parallel path has  $Z/p$  conductors in series where  $Z$  and  $p$  are the total number of armature conductors and poles respectively.
- Emf generated =  $\frac{\text{Emf}}{\text{Parallel path}}$
- Total current  $I_a = P \times \text{current/parallel path}$

~~choice of Armature windings~~

1. Pole pitch :-

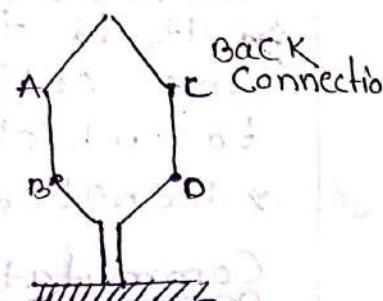
1. Pole pitch is the peripheral distance between two adjacent poles. It is measured in terms of armature slots or conductors.

2. It can be also defined as the number of armature conductors per pole.

$$e.g. \text{Conductor} = 48$$

$$\text{pole} = 4$$

$$\text{Pole pitch} = \frac{48}{4} = 12$$



### coil pitch

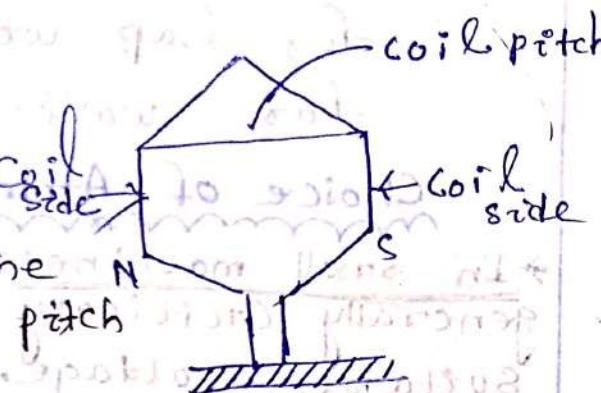
1. It is the angular distance between 2 sides of coil, measured in the term of armature slots per pole.

$$e.g. \text{slots} = 36$$

$$\text{pole} = 4$$

$$\text{coil pitch} = \frac{36}{4} = 9$$

2. If the coil pitch is equal to the pole pitch then it is called full pitch coil.



3. For full pitch coil each coil side lies under the opposite pole i.e. the coil spans 180° electrical.

4. If the coil pitch less than the pole pitch then it is said to be short pitch coil or fractional pitch coil.

### winding pitch :-

It is defined as the distance between two successive conductors which are directly connected together around the armature.

It is the beginning of two successive coil sides & is denoted by  $y_w$ .

### Back pitch

1. Denoted by  $y_b$  & defined as the distance between the 1st & last conductors of a coil.

### Front pitch

- It is the distance between the 2nd conductor of one coil & the first conductor of the next coil.
- Both the coils should be connected to the same commutator segment & on the front end by  $y_f$ .

### Resultant pitch :-

- It is the distance between the beginning of one coil & the beginning of the next coil to which is connected.
- Denoted by  $y_r$

### Commutator pitch :-

- Distance between the commutator segments to which the two ends of coil are connected  
for lap winding  $y_c = y_b - y_f$   
for wave winding  $y_c = y_b + y_f$

### Choice of Armature winding

- In small machines:- the current carrying is not generally critically therefore in order to obtain suitable voltage.
- Wave winding are often used.
- In large machines:- suitable voltage are easily obtained because of the relatively large number of armature conductors available.
- Current capacity is more critical.
- Large machines generally used lap winding.
- In some cases, neither simple lap winding nor simple wave winding provides a satisfactory solution. In such cases we use more complicated type of armature winding.

## E.M.F Equation of a D.C generator

We shall now derive an expression for the emf generated in a dc generator.

$$\Phi = \text{flux/pole} \text{ web / flux per pole}$$

Z = total number of armature conductor

P = Number of poles

A = number of parallel paths for wave winding  
& for lap winding

N = speed of armature in r.p.m

$$E_g = \text{emf of the generator} = \frac{\text{emf}}{\text{parallel path}}$$

flux cut by one conductor in one revolution of the armature  $d\Phi = P\Phi$  webers.

Time taken to complete one revolution

$$dt = 60^\circ / N \text{ second}$$

$$\text{e.m.f generated/conductor} = \frac{d\Phi}{dt} = \frac{P\Phi}{60/N} = \frac{P\Phi N}{60} \text{ Volt}$$

$$\text{emf of generator } E_g = \text{emf per parallel path} \\ = (\text{emf/conductor}) \times \text{no of Conductor}$$

in series in parallel path

$$E_g = \frac{P\Phi Z N}{60 A} \quad (\text{for wave winding})$$

where  $A = \text{area of one conductor}$  (for lap winding)

Armature Resistance: To terminals

The resistance offered by the armature circuit is known as armature resistance ( $R_a$ ) and it includes

- Resistance of armature winding.
- Resistance of Brushes.

The Armature Resistance depends upon the construction of the Machine. Except for small Machines. Its value is generally less than 1Ω.

### Question-01

An 8 pole 250V wave wound generator has 400 conductors if the generator is to be lap wound the number of conductors is?

Soln: given that no. of conductors  $A = 2$   
Number of poles ( $p$ ) = 8, for wave wound  $\Rightarrow A = 2$

$$\text{Number of Conductors } (Z) = 400$$

The wave wound generator (EMF) = 250V

$$\text{EMF} = \frac{PQZN}{60A} = \frac{8 \times 2 \times 400 \times N}{60 \times 2} \quad (i)$$

(for wave wound)

$$\text{EMF} = \frac{PQZN}{60A} = \frac{8 \times 2 \times Z \times N}{60 \times 8} \quad (ii) \quad (\text{for lap wound})$$

By equating eq (i) & (ii),

$$\Rightarrow \frac{400 \times 8 \times N}{60 \times 2} = \frac{8 \times Z \times Q \times N}{60 \times 8}$$

$$\Rightarrow \frac{400 \times 8}{2} = \frac{8Z}{8} \Rightarrow \frac{400 \times 8 \times 8}{2} = 1600$$

The lap wound generator the number of conductors is 1600.

### Question-02

A 6 pole lap wound generator has 300 conductors. The emf induced per conductor being 5V then the generated voltage of generator?

Soln given that:

A lap wound generator.

$$\text{Number of conductors } (Z) = 300$$

EMF induced per conductor = 5V

$$\text{No. of poles } (p) = 6$$

$$\text{Total EMF} = 300 \times 5 = 1500 \text{ V}$$

then generated emf,  $E_g = \frac{\text{Total EMF}}{\text{Parallel path/pole}}$  (for lap wound)

$$E_g = \frac{1500}{6} = 250 \text{ V (ans)}$$

so that the output voltage of generator is 250V.

Q.3 A. 4 Pole generators having wave wound armature winding has 51 slots each slot containing 20 conductors what will be the voltage generated in the machine when driven 1500 rpm, assuming flux per pole to be 7 mwb.

Solution Given that

$$\text{No of poles} (p) = 4$$

$$\text{slot} = 51 \text{ & per slot conductors} = 20$$

Wave wound armature winding ( $A$ ) = 2

$$(z) \text{ Total Conductors} = 51 \times 20 = 1020$$

$$N = 1500 \text{ rpm}$$

$$Q = 7.0 \text{ mw b} = 7.0 \times 10^{-3} = 0.007 \text{ wb}$$

$$\text{Then } \text{Emf} = \frac{P \& N}{60} \times Z = \frac{4 \times 0.007 \times 1500 \times 1020}{60 \times 2} = \frac{42840}{120} = 357 \text{ v}$$

The generated voltage of the machine 357 v

Types of D.c generators.

→ The magnetic field in d.c generator is normally produced by electromagnets rather than permanent magnet.

→ Generators D.c generators are divided into 2 types.

1. Separately excited d.c generator

2. Self-excited d.c. generators.

→ The behaviour of a d.c generator on load depends upon the method of field excitation adopted.

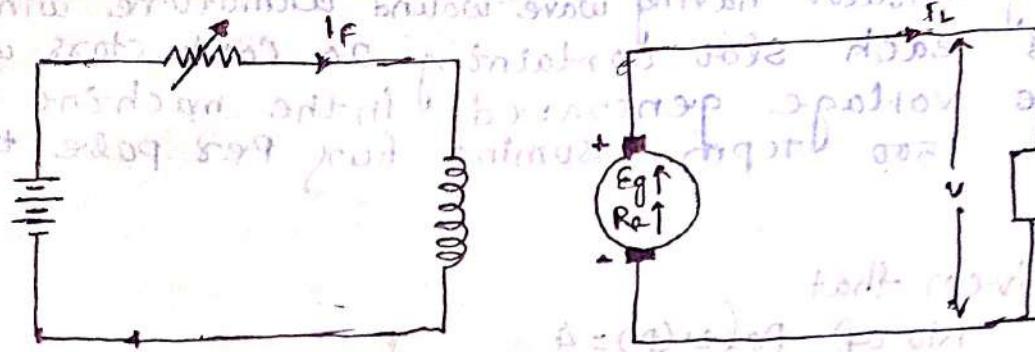
Separately excited generator.

→ A d.c generator whose field magnet winding is supplied from an independent external d.c source is called a separately excited generator.

→ The voltage output depends upon the speed of rotation of armature and the field current.

→ The greater the speed and field current, greater is the generated emf. It may be noted that separately excited d.c generators are rarely used in practice.

→ D.c generators are normally self-excited type.



$$\text{Armature current } I_a = I_L$$

$$\text{Terminal voltage } V = E_g - I_a R_a$$

$$\text{Electric power developed} = E_g I_a$$

$$\text{Power delivered to load} = E_g I_a - I_a^2 R_a = I_a(E_g - I_a R_a)$$

Self-excited generators :-

A d.c. generators whose field magnet winding is supplied current from the output of the generator is called self-excited generators.

→ Self-excited generators depending upon the manner in which the field winding is connected to armature.

→ Self-excited generators are three types.

1. Series generator.

2. Shunt generator.

3. Compound generator.

1. Series generator :-

→ In series-wound generator, the field winding is connected in series with armature winding.

→ So that whole armature current flows through the field winding as well as load.

→ Field winding carries the whole of load current.

It has a few turns of thick wire having low resistance.

→ Series generators are used in boosters.

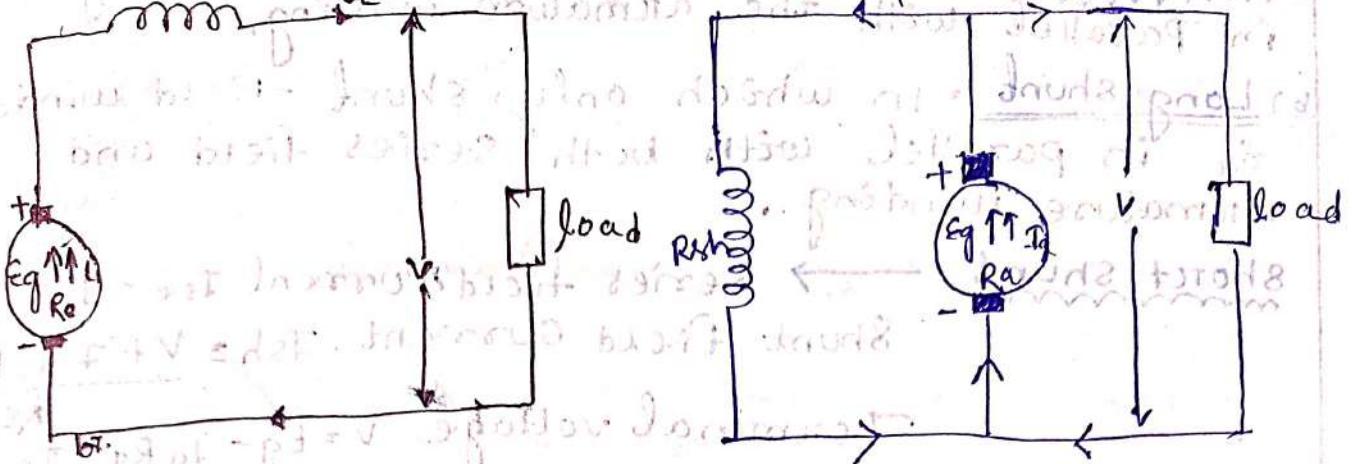
$$\text{Armature current } I_a = I_{se} = I_L = 1$$

$$\text{Terminal voltage } V = E_g - I_a(R_a + R_{se})$$

$$\text{Power developed in armature} = E_g I_a$$

$$\text{Power delivered to load} = E_g I_a - I_a^2(R_a + R_{se})$$

$$= I_a(E_g - I_a(R_a + R_{se})) = V I_a \text{ or } V^2$$



### (ii) Shunt generator:

- In a shunt generator, the field winding is connected in parallel with the armature winding, so that terminal voltage of the generator is applied across it.
- The shunt winding has many turns of fine wire having high resistance.
- The connection of a shunt-wound generator.

$$\text{Shunt field current } I_{sh} = V/R_{sh}$$

$$\text{Armature current, } I_a = I_L + I_{sh}$$

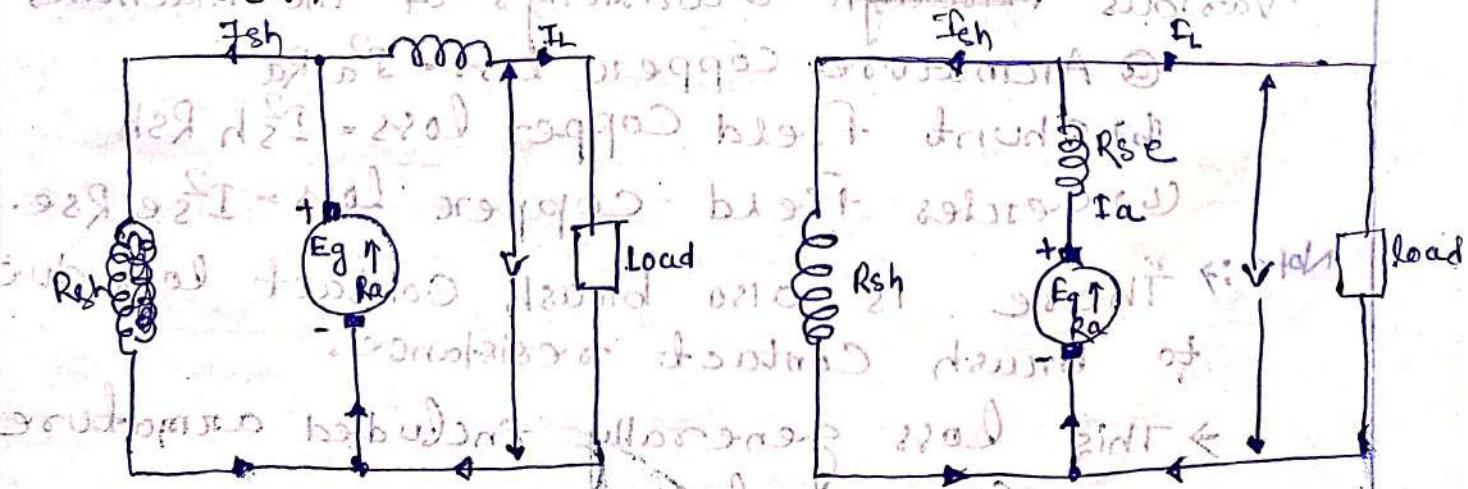
$$\text{Terminal Current, } V = E_g - I_{sh} R_a$$

$$\text{Power developed in armature} = E_g I_a$$

$$\text{Power delivered to load} = V I_L$$

### (iii) Compound generator:

- In a compound-wound generator, there are two sets of field windings on each pole.
- \* One is in series and the other in parallel with armature.



(Compound generator)

- a) short shunt := In which only shunt field winding is in parallel with the armature winding.
- b) Long shunt := In which only shunt field winding is in parallel with both series field and armature winding.

short shunt  $\rightarrow$  series field current  $I_{se} = I_a$

shunt field current  $I_{sh} = \frac{V + I_{se} R_{se}}{R_{sh}}$

Terminal voltage  $V = E_g - I_a R_a - I_{se} R_{se}$

Power developed in armature =  $E_g I_a$

Power delivered to load =  $V I_L$

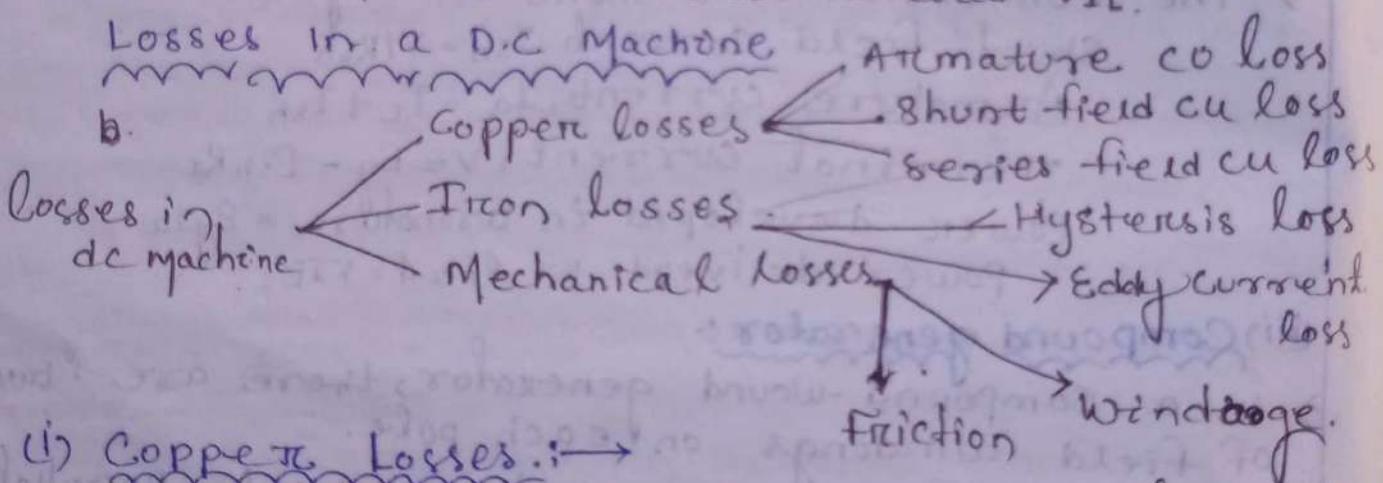
long shunt  $\rightarrow$  Series field current,  $I_{se} = I_a = I_L + I_{sh}$

shunt field current,  $I_{sh} = V / R_{sh}$

terminal voltage  $\therefore V = E_g - I_a (R_a + R_{sh})$

Power developed in armature =  $E_g I_a$

Power delivered to load =  $V I_L$ .



(i) Copper Losses  $\rightarrow$  These losses occur due to currents in the various ~~through~~ & windings of the machine.

(a) Armature copper loss =  $I_a^2 R_a$

(b) Shunt field copper loss =  $I_{sh}^2 R_{sh}$

(c) Series field copper loss =  $I_{se}^2 R_{se}$ .

Note: There is also brush contact loss due to brush contact resistance.

$\rightarrow$  This loss generally included armature copper loss.

(rotor with brushes)

### (ii) Iron Losses:-

- These losses occur in the armature of a DC machine and are due to the rotation of armature in the magnetic field of the fixed poles.
- Hysteresis loss.
- The phenomenon of lagging of magnetization or induction flux density behind the magnetizing force is known as hysteresis loss.
- The loss due to hysteresis is called hysteresis loss.
- Hysteresis loss occurs in the armature of the DC machine.
- Hysteresis loss  $P_h = \mu_0 n B_{max}^2 f V$  watts.
- $B_{max}$  = maximum flux density in armature.
- $f$  = frequency of magnetic reversals.

$$= NP / 120 \text{ where } N \text{ is in r.p.m.}$$

$V$  = Volume of armature in  $m^3$

$n$  = Stomets hysteresis coefficient.

### Eddy Current Loss.

- When armature rotates in the magnetic field of the pole an emf is induced in it which circulates eddy currents in the armature cores.

The power losses due to this eddy current called

$$\text{Eddy current loss } P_e = K_e B_{max}^2 f^2 t^2 V \text{ watt}$$

$K_e$  = Constant

$B_{max}$  = maximum flux density in the core.

$f$  = frequency of magnetic reversal

$t$  = thickness of lamination.

$V$  = Volume of core in  $m^3$ .

## Mechanical losses :-

→ These losses are due to friction and windage  
 @ friction loss e.g. bearing friction, brush friction.

(b) Windage loss e.g. air friction of a rotating armature. The losses depend upon the speed of the machine.

## Constant and variable losses :-

Constant losses :- These losses in a dc generator which remain constant at all loads are known as constant losses.

The Constant losses in a dc generator

- Iron losses
- Mechanical losses
- Shunt field losses.

Variable losses :- Those losses in a dc generator which vary with load are called variable losses.

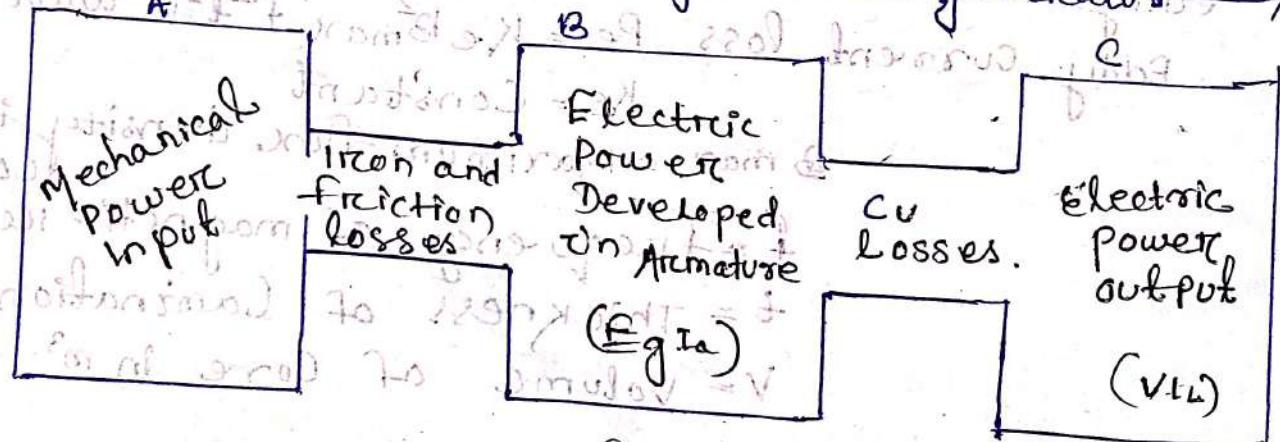
→ The variable losses in a dc generator

- Copper loss in armature winding ( $I_a^2 R_a$ )
- Copper loss in series field winding ( $I_s^2 R_s$ )

Total losses = Constant losses + Variable losses.

## Power stages.

The various power stages in dc generator →



$$A - B = \text{Iron and friction losses}$$

$$B - C = \text{Copper losses}$$

i) Mechanical efficiency :  $\eta_m = \frac{B}{A} = \frac{E_g I_a}{\text{Mechanical power input}}$

ii) Electrical efficiency :  $\eta_e = \frac{C}{B} = \frac{V I_L}{E_g I_a}$

iii) Commercial or overall efficiency :  $\eta_c = \frac{C}{A} = \frac{V I_L}{\text{Mechanical power input}}$

clearly,

Unless otherwise stated, Commercial efficiency is always understood.

Now, Commercial efficiency,  $\eta_c = \frac{C}{A} = \frac{\text{Output}}{\text{Input}} - \text{input-losses}$

Conditions for Maximum efficiency

The efficiency of a DC generator is not constant but varies with load. Consider a shunt generator delivering a load current  $I_L$  at a terminal voltage  $V_L$ .

General output :  $V_L$

General Input : Output + losses.

=  $V I_L + \text{variable losses} + \text{constant losses}$

=  $V I_L + I^2 L R_a + w_c$

$\therefore \text{losses} = (V I_L + C I_L + I_s h)^2 R_a + w_c$

The shunt field current  $I_{sh}$  is generally small as compared to  $I_L$  and therefore can be neglected.

Generator Input =  $V I_L + I^2 L R_a + w_c$

$$\eta = \frac{\text{Output}}{\text{Input}} = \frac{V I_L}{V I_L + I^2 L R_a + w_c} = \frac{1}{1 + \left( \frac{I^2 L R_a + w_c}{V I_L} \right)}$$

$$\Rightarrow \frac{d\eta}{dR_a} \left( \frac{I^2 L R_a + w_c}{V I_L} \right) = 0$$

$$\Rightarrow \frac{R_a}{V} - \frac{w_c}{V I_L^2} = 0 \Rightarrow R_a = \frac{w_c}{V I_L^2}$$

$$I^2 L R_a = w_c \quad (\text{Variable loss} = \text{constant loss})$$

The load current corresponding to maximum efficiency is given by  $I_L = \sqrt{\frac{w_c}{R_a}}$

Hence the efficiency of a dc generator will be maximum when the load current is such that the variable loss is equal to the constant loss.

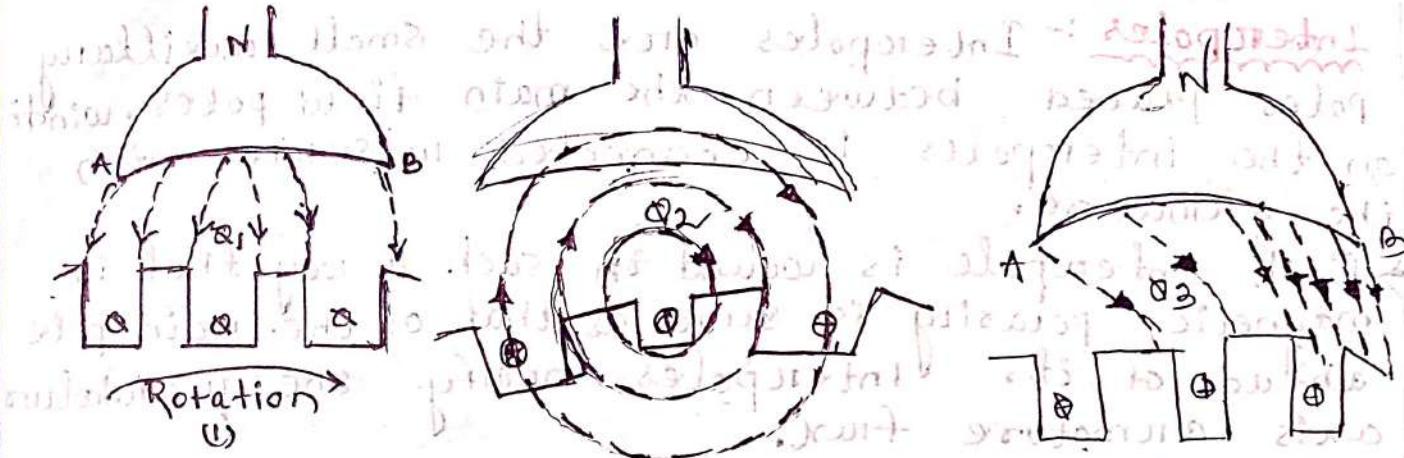
## Armature Reaction

Dt : 39-4-2022

- So far we have assumed that the only flux acting in a dc machine is that due to the main poles called main flux.
- However, current flowing through the armature conductor also creates a magnetic flux called armature flux that distorts and weakens the flux coming from the poles.
- The action of armature flux on the main flux is known as armature reaction.
- When the generator is on no-load a small current flowing in the armature does not appreciably affect the main flux  $\Phi_1$ .
- i) Coming from the top pole when the generator is loaded the current flowing through armature conductors sets up flux  $\Phi_2$ . Coming from the pole when the generator is loaded, the current flowing through armature
- ii) shows flux due to armature current alone by superimposing  $\Phi_1$  and  $\Phi_2$ , we obtain the resulting flux  $\Phi_3$  as shown in fig.
- iii) It is clear that flux density at the trailing pole tip (point O) is increased.

while at the leading pole tip (point A) it is decreased. This unequal field distribution produces the following two effects:

- The main flux is distorted.



Due to Higher flux density at pole tip B, saturation sets in. Consequently, the increase in flux at pole tip B is less than the decrease in flux under pole tip A. Flux  $\phi_2$  at full load is, therefore, less than flux  $\phi_1$  at no load.

### How to Reduce Armature Reaction:

Usually no special efforts are taken for small machines to reduce the armature reaction. But for large DC Machines Compensating Winding and interpoles are used to get rid of the ill effects of armature reaction.

**Compensating winding:** Now we know that the armature reaction is due to the presence of armature flux. Armature flux is produced due to the current flowing in armature conductors. Now if we place another winding in close proximity of the armature winding and if it carries the same current but in opposite direction. Then this will nullify the armature field, such an additional winding is called as Compensating winding.

→ It is placed on the pole faces. Compensating winding is connected in series with the armature winding in such a way that it carries the current in the opposite direction.

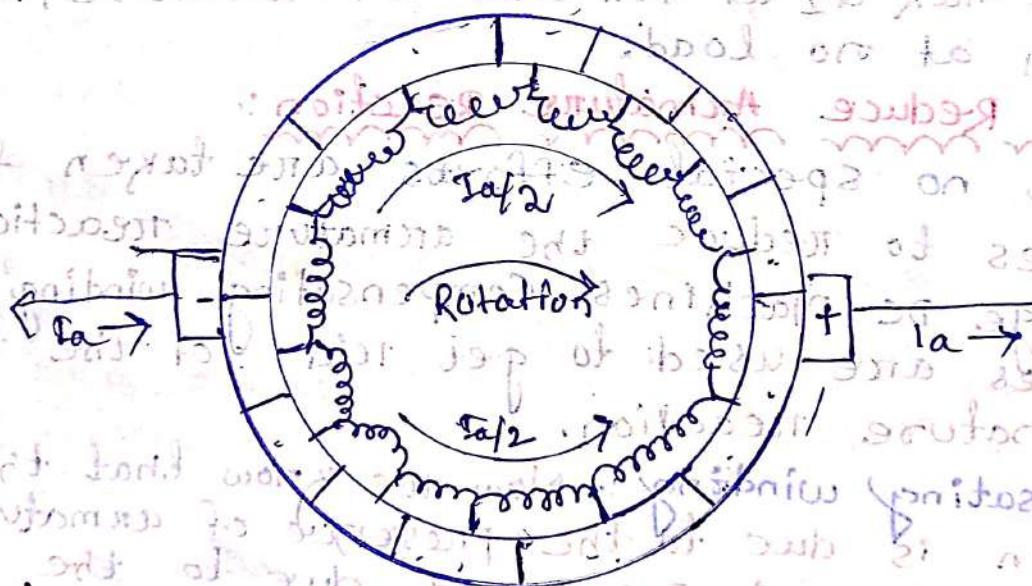
Interpoles :- Interpoles are the small auxiliary poles placed between the main field poles. Winding on the interpoles is connected in series with the armature.

→ Each interpole is wound in such a way that its magnetic polarity is same as that of the main pole ahead of it. Interpoles nullify the quadrature axis armature flux.

### Commutation

In fig shows the schematic diagram of a 2-pole lap wound generator. There are two parallel paths between the brushes.

Therefore, each coil of the winding carries one-half of the total current ( $I_a$ ) entering or leaving the armature circuit.



Note that the current in the coils connected to a brush are either all towards the brush or all directed away from the brush.

Therefore, current in the coil will reverse as the coil passes a brush. This reversal of current in the coil passes a brush is called commutation.

→ The complete reversal of current in a coil at a uniform rate as the coil passes the brush is called ideal commutation.

### Illustration :-

→ Let us illustrate the phenomenon of Commutation in one coil in the armature winding shown in fig. For this purpose, we consider the coil A. Suppose the width of the brush is equal to the width of the commutator segment and total armature current is  $40\text{ A}$ .

→ Since there are two parallel paths, each coil carries a current of  $20\text{ A}$ .

(i) In fig (i) the brush is in contact with only segment 1 of the commutator. The commutator segment 1 conducts a current  $40\text{ A}$  to the brush,  $20\text{ A}$  from coil A and  $20\text{ A}$  from the adjacent coil as shown. The coil A has yet to undergo commutation.

(ii) As the armature rotates, the brush will make contact with segment 2 and thus short-circuits the coil A as shown in fig.

→ There are now two parallel paths into the brush as long as short-circuit of coil A exists.

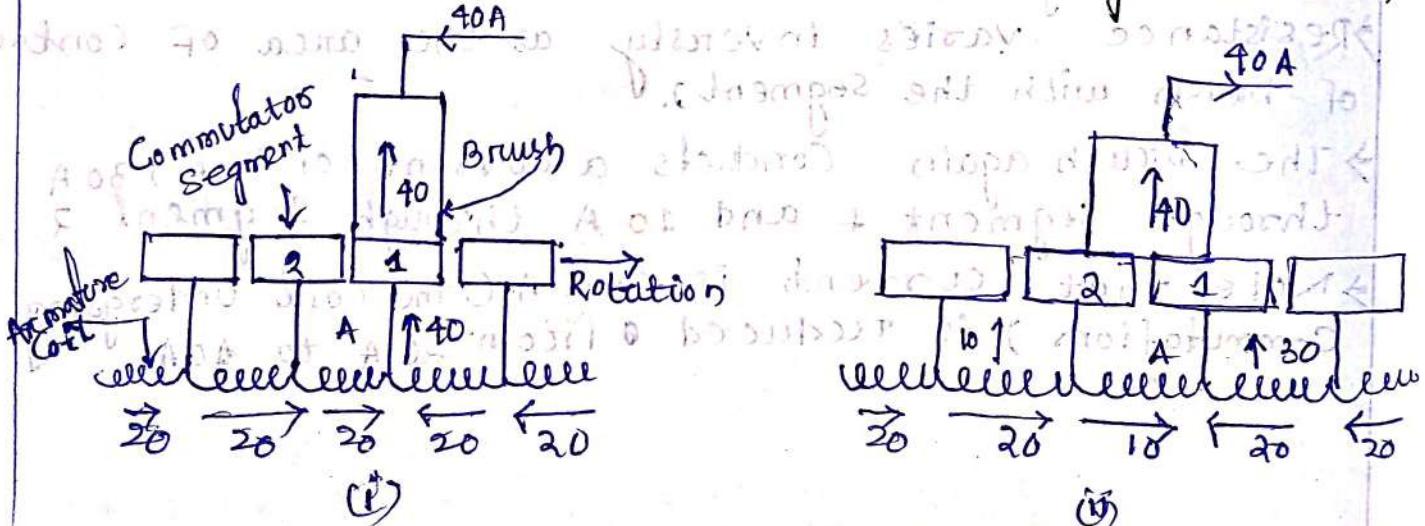
→ Shows the instant when the brush is one-fourth on segment 2 and three-fourth on segment 1. For this condition, the resistance of the path through segment 2 is three times the resistance of the path through segment 1.

→ Resistance varies inversely as the area of contact of brush with the segment).

→ The brush again conducts a current of  $40\text{ A}$ ,  $30\text{ A}$  through segment 1 and  $10\text{ A}$  through segment 2.

→ Note that current in coil A (the coil undergoing commutation) is reduced from  $20\text{ A}$  to  $10\text{ A}$ .

- (iii) Shows the instant when the brush is one-half on Segment 2 and one-half on Segment 1.
- The brush again conducts  $40A - 20A$  through segment 1 and  $20A$  through segment 2. (∴ now resistances of the two parallel paths are equal)
- Note that current in coil A is zero.
- (iv) The fig. shows the instant when the brush is three-fourth on segment 2 and one-fourth on segment 1.
- The brush conducts a current of  $40A - 30A$  through segment 2 and  $10A$  through segment 1.
- Note that current in coil A is  $10A$  but in the reverse direction to that before the start of commutation. The reader may note the action of commutator in reversing current in a coil as the coil passes a brush.
- (v) The fig. shows the instant when the brush is contact only with segment 2. The brush again conducts  $40A - 20A$  from coil A and  $20A$  from the adjacent coil.
- Note that now current in coil A is  $20A$  but in the reverse direction.
- Thus the coil A has undergone commutation. Note that now current in coil A is  $20A$  but in the reverse direction. Thus the coil A has undergone commutation.
- Note that during commutations, the coil under consideration remains short-circuited by the brush.



### charlie path

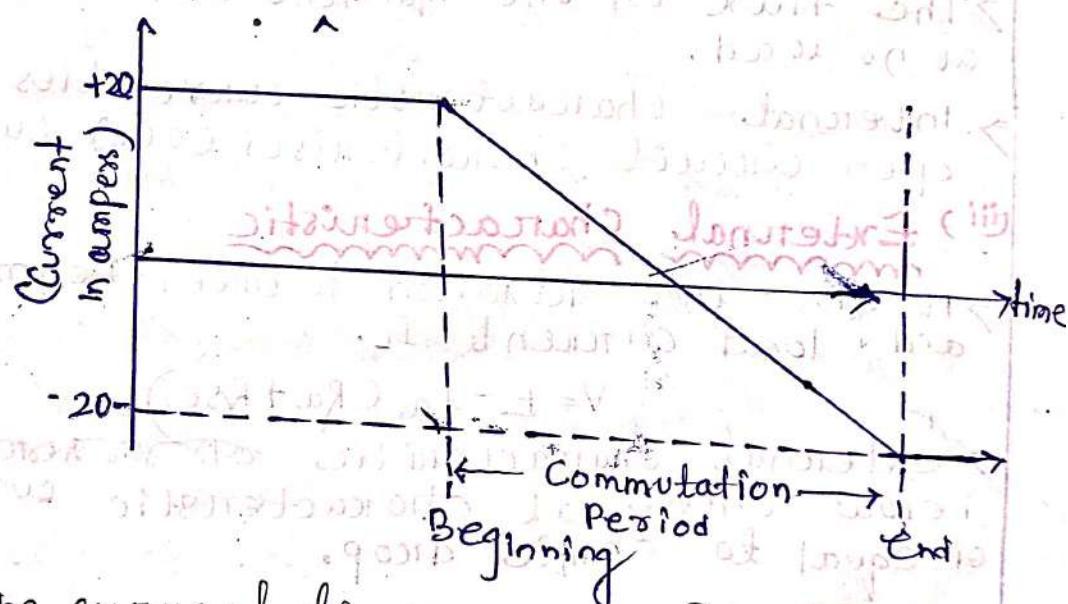
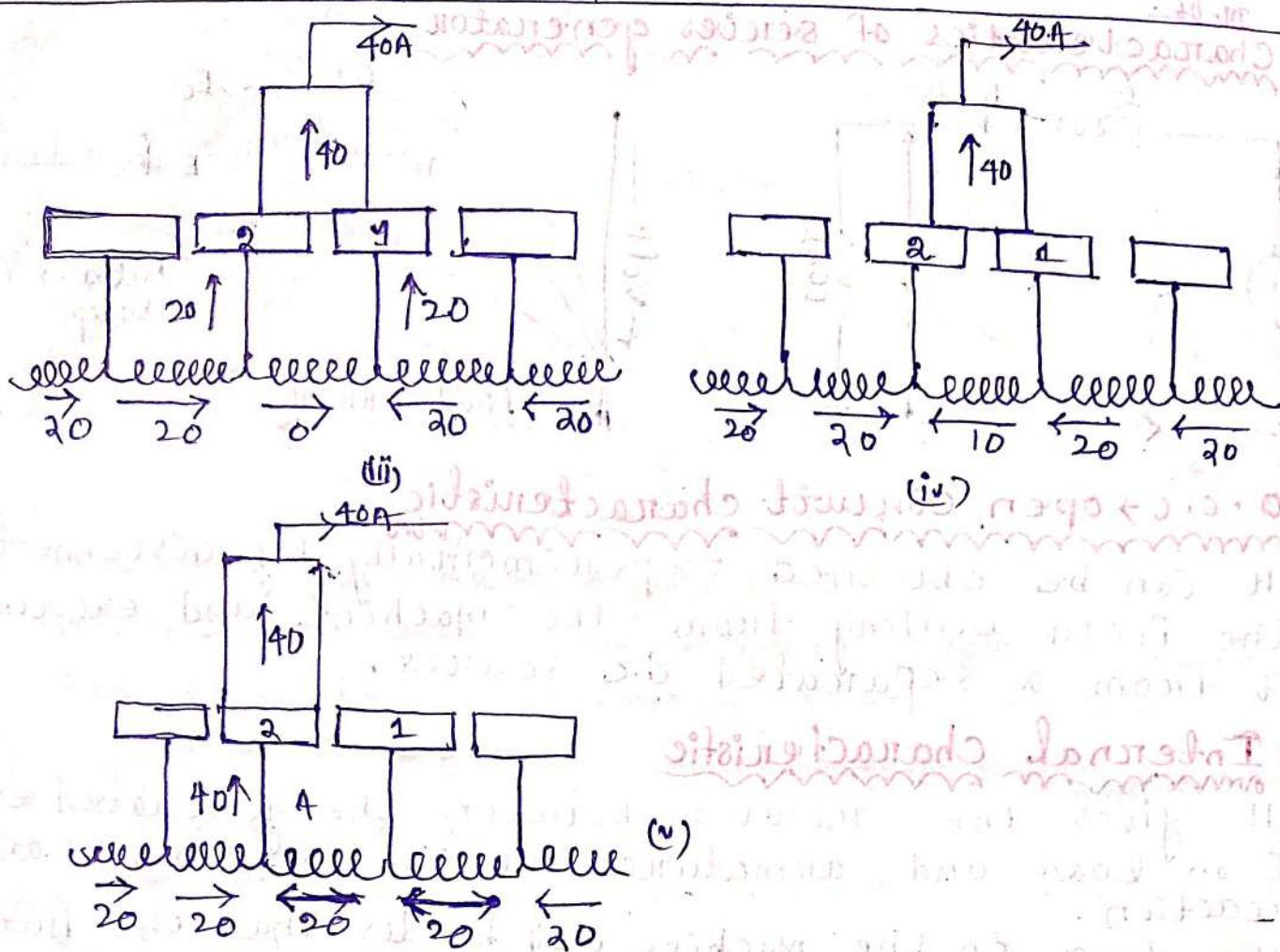
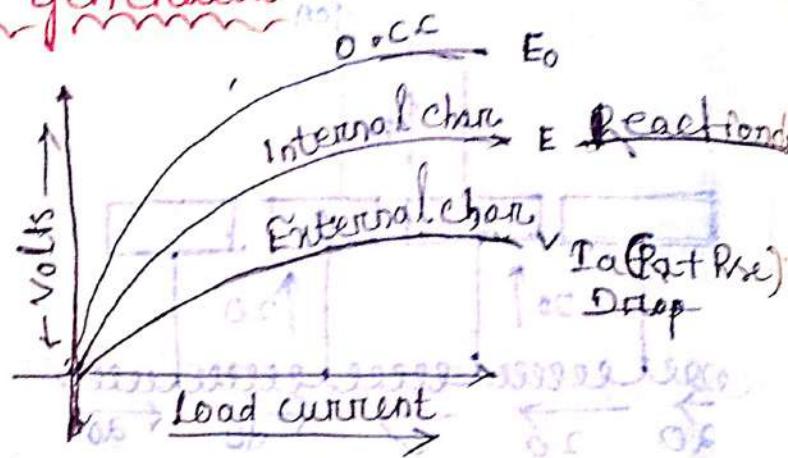
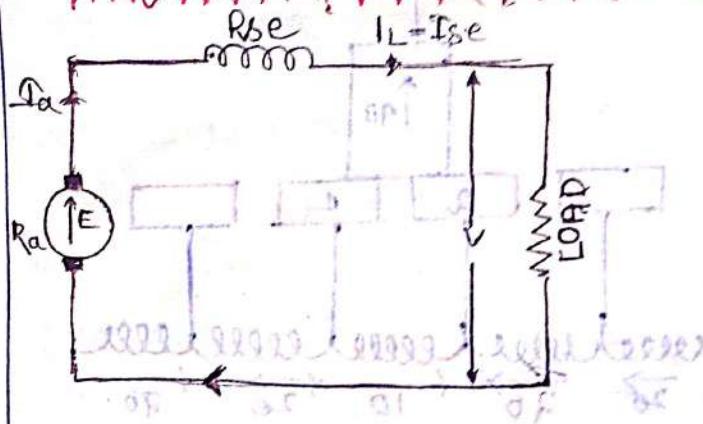


Fig shows the current-time graph for coil A during ideal commutation note that current reversal in coil A is uniform.

Q1-Q4

## Characteristics of series generator



### (i) O.C.C → open circuit characteristic

→ It can be obtained experimentally by disconnecting the field winding from the machine and exciting it from a separated d.c source.

### (ii) Internal characteristic

→ It gives the relation between the generated emf  $E$  on load and armature current due to armature reaction.

→ The flux in the machine will be less than the flux at no load.

→ Internal characteristic curve lies below the open circuit characteristic (O.C.C) curve.

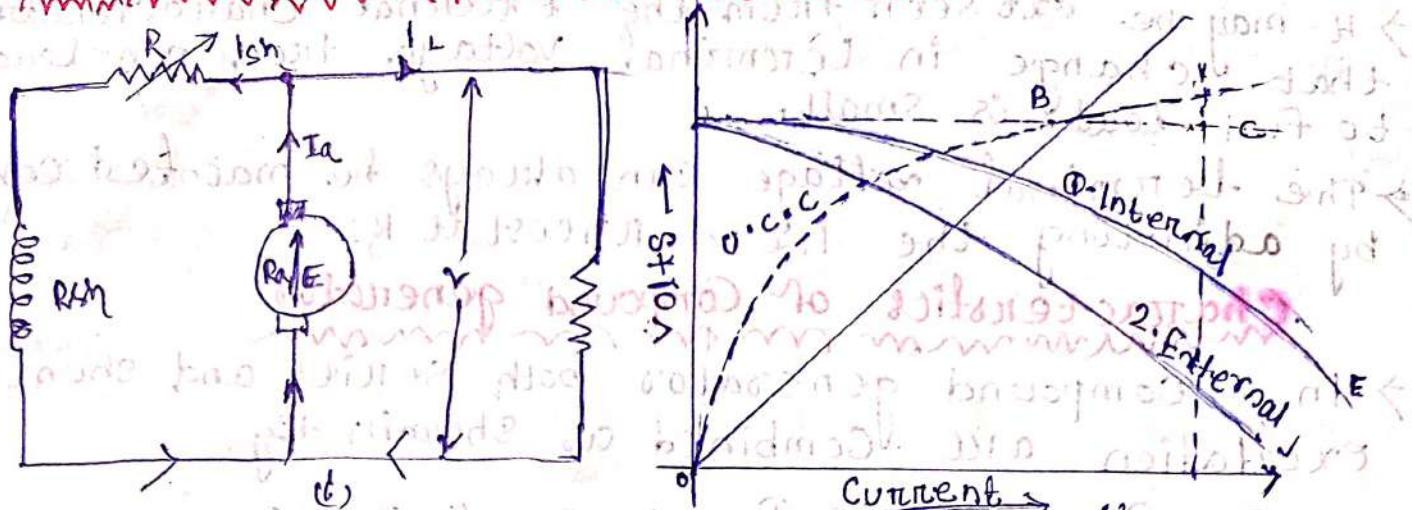
### (iii) External characteristic

→ It gives the relation between terminal voltage  $V$  and load current  $I_L$ .

$$V = E - I_a(R_a + R_{se})$$

→ External characteristic of series curve will lie below internal characteristic curve by an amount equal to ohmic drop.

## Characteristics of a shunt generator.



### O.C.C - Open circuit characteristics

- The O.C.C of a Shunt generator is similar in shape to that of a series generator as shown in fig (ii).
- The line OA represents the shunt field circuit resistance, when the generator is run at normal speed. It will build up a voltage  $o.m.$  at no-load.
- The terminal voltage  $V$  of the generator will be constant (represented by the horizontal dotted line MC).

### Internal characteristics.

- When the generator is loaded flux per pole is reduced due to armature reaction.
- Therefore, emf generated on load is less than the emf generated at no load as a result, the internal characteristic ( $E/I_a$ ) drops down slightly as shown in fig (i).

### External characteristics.

- Curve (ii) shows the external characteristic of a shunt generator. It gives the relation between terminal voltage  $V$  and load current  $I_L$ .
- $V = E - I_a R_a$
- $E = (I_a + I_{sh}) R_a$

- Therefore, external characteristic curve will lie below the internal characteristic curve by an amount equal to drop in the armature circuit.

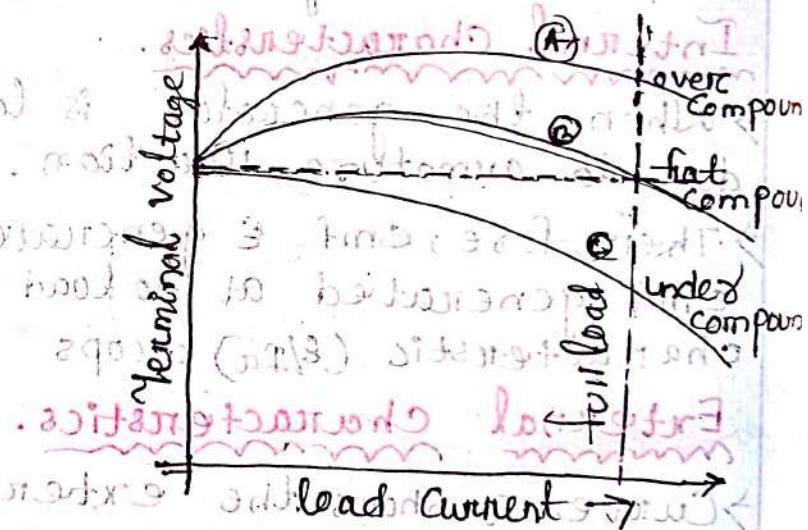
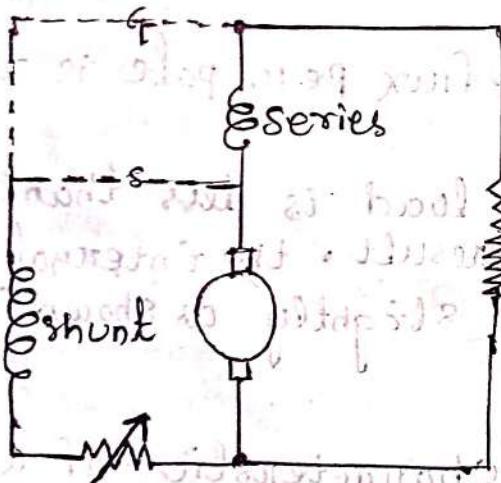
Graph of  $[E - (I_a + I_{sh}) R_a]$  as shown in fig (iii)

## Note

- It may be seen from the external characteristic that change in terminal voltage from no-load to full load is small.
- The terminal voltage can always be maintained constant by adjusting the field rheostat  $R_f$ .

### Characteristics of Compound generator

- In a compound generator both series and shunt excitation are combined as shown in fig.
- $I_a = I_L + I_{sh}$  As  $I_{sh}$  is small,  $I_a \approx I_L$
- Shunt winding can be connected either across the armature only (short-shunt connection) or across armature plus series (long-shunt connection).
- The compound generator can be cumulatively compounded or differentially compounded generator.
- External characteristics of long and shunt compound generators are almost identical.



### External characteristic

- The series winding turns are so adjusted that with the increase in load current the terminal voltage increases. It is called over-compounded generator.
- In such case as the load current increases, the series field m.m.f. increases and tends to increase the flux and hence the generated voltage.

The increase in generated voltage is greater than the I<sub>a</sub>R<sub>a</sub> drop. so that instead of decreasing

- The terminal voltage increases as shown by curve A in fig.
- (ii) The series winding turns are so adjusted that with the increase in load current, the terminal voltage remains constant. It is called flat-compounded generator.
  - The series winding of such a machine has lesser number of turns than the one in over-compounded machine, and does not increase the flux.
- The load current. Consequently, the full load voltage is nearly equal to the no-load voltage as indicated by curve B.
- (iii) The terminal voltage winding has lesser number of turns than for a flat-compounded machine, the terminal voltage falls with increase in load current as indicated by curve C in fig.

→ This machine is called under-compounded generator.

### Applications of series wound DC generator.

- These types of generators are restricted for the use of power supply.
- They are used for supplying field excitation current in DC locomotives for regenerative breaking.
- These type of generators are used as boosters to compensate the voltage drop in the feeders in various types of distribution system such as railway service.
- In series arc lighting this type of generators are mainly used.

### Applications of shunt Wound DC generator.

- They are used to supply power to apparatus situated very close to its position.
- These type of DC generators generally give constant terminal voltage for small distance operation with the help of field regulators from no load to full load.
- They are used for general lighting.
- They are used for charge battery because they can be made to give constant output voltage.

- They are used for giving the excitation to the alternator.
- They are also used for small power supply.
- Application of compound wound DC generators.
- The compound wound DC generators are most widely used because of its compensating property. Dependent upon number of series field turns.
- Comparatively compound generators may be over compounded, flat compounded, under compounded.
- They are used for lighting, power supply purposes and for heavy power services.
- They are mainly made over compounded.
- Comparative compound wound generator also used for driving a motor.
- Used for small distance operation. like power supply for hotels, offices, homes and lodges.

### Critical field Resistance of a shunt-generator.

- The voltage build up in a shunt-generator depends upon field circuit resistance.
  - field circuit resistance is  $R_1$ , then generator will build up  $V_m$ .
  - If the field ckt resistance is increased to  $R_2$  (line OB), the generated will build up a voltage  $V_L$ , slightly less than  $V_m$ . & slope of resistance line also increased.
  - The effect of residual magnetism has been neglected in drawing O.C.C.
  - Resistance = slope of line =  $\tan \alpha$
  - Here  $\alpha$  is the angle which the lines makes with x-axis, As  $\alpha$  increases.
  - The maximum field circuit resistance with which the shunt-generator would just excite is known as critical field resistance.
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