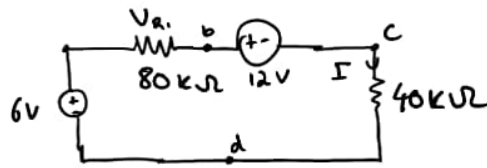


KCL AND KVL EXAMPLE

3

- Find I and V_{bd} in the following circuit?



Using Ohm's law

We find

$$I = \frac{V_T}{R_T}, \text{ where } V_T = (12 - 6)$$

taking ' I ' going out of src as +ve.

$$R_T = 80k + 40k = 120k\Omega$$

$$I = \frac{-6}{120k} = -0.05mA$$

Now Using KVL to the loop.

$$V_{bd} = 6 + V_{R1}$$

$$= 6 + 80k(0.05mA) = \underline{\underline{10V}}$$

Using KCL we know that only 1 current I flows in the loop.

Then we apply Ohm's law to find the current I .

Lastly, we use KVL in the single loop to evaluate the voltage V_{bd} .

We therefore see how KCL and KVL can be used as simple analysis tools.

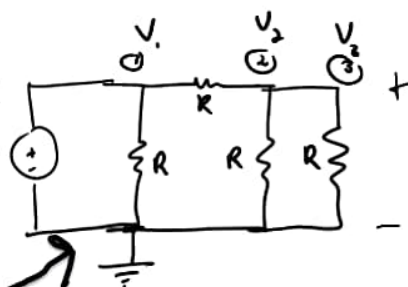
4

NODAL ANALYSIS

- Nodal Analysis of electronic circuits is based on assigning Nodal voltages at various nodes of the circuit with respect to a reference and then finding these nodal voltages to analyze the circuit.

Simple representation of Nodal Voltages shown below:

As shown in Figure, a *node* is a point in a circuit where two or more wires meet. At these nodes one can assign a nodal voltage with respect to the reference ground shown.



5

NODAL ANALYSIS: INDEPENDENT SOURCES ONLY

Using KCL:

write nodal Equations for nodes ① & ②

Assume current Reading out of node as +ve.

In this example we write the KCL equations at the nodes as Shown, then solve them to find The respected nodal voltages.

$$-1m + \frac{V_1}{12k} + \frac{V_1 - V_2}{6k} = 0 \quad \text{--- ①} \quad \left. \begin{array}{l} \text{--- ①} \\ \text{--- ②} \end{array} \right\} \text{KCL Eqn.}$$

7

$$4m + \frac{V_2 - V_1}{6k} + \frac{V_2}{6k} = 0 \quad \text{--- ②}$$

Solving for V_1 & V_2

$$-12 + V_1 + 2V_1 - 2V_2 = 0 \quad \text{--- ①a}$$

$$3V_1 - 2V_2 = 12$$

$$24 + 2V_2 - V_1 = 0 \quad \text{--- ②a}$$

Equation 1a & 2a

$$V_1 = 24 + 2V_2 \quad \& \quad 3V_1 - 2V_2 = 12$$

So

$$3(24) + 6V_2 - 2V_2 = 12$$

$$4V_2 = -60$$

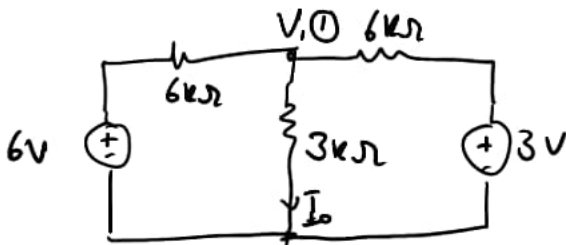
$$V_2 = -15V$$

$$\text{So } V_1 = 24 - 30 = -6V$$

7

NODAL ANALYSIS: INDEPENDENT SOURCES ONLY

Example 2 (Ind. Voltage Sources Only):



$$\frac{V_1 - 6}{6k} + \frac{V_1}{3k} + \frac{V_1 - 3}{6k} = 0$$

$$V_1 - 6 + 2V_1 + V_1 - 3 = 0$$

$$4V_1 = 9$$

$$V_1 = \frac{9}{4} V$$

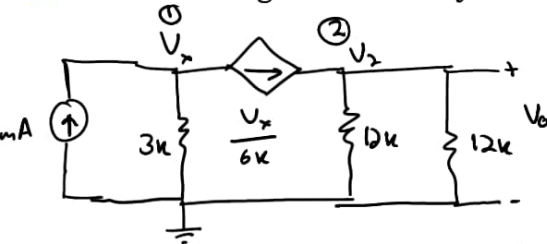
So Now

$$I_0 = \frac{V_1}{3k} = \frac{3 \frac{9}{4}}{3k} = \frac{3}{4} mA$$

8

NODAL ANALYSIS: DEPENDENT SOURCES

- Find V_o using Nodal Analysis?



For this Circuit, We need to Overlook the node with dependent Source and form equations round it. We use KCL at Nodes 1 and 2 and derive the equations based Current flow.

At Node 2 taking passive sign convention

$$\text{KCL Eqn} \quad -2m + \frac{V_x}{3k} + \frac{V_2}{10k} + \frac{V_2}{12k} = 0 \quad \text{--- (1)}$$

At node 2

$$\frac{V_2}{12k} + \frac{V_2}{12k} - 2m + \frac{V_x}{3k} = 0 \quad \text{--- (2)}$$

NODAL ANALYSIS: DEPENDENT SOURCES

Controlling Equation at Node 1

$$2m = \frac{V_y}{6k} + \frac{V_x}{3k} \quad \text{--- (3)}$$

$$12 = V_x + 2V_y \quad V_x = 4V \quad \text{For the nodal voltages.}$$

Now put in Eqn (2)

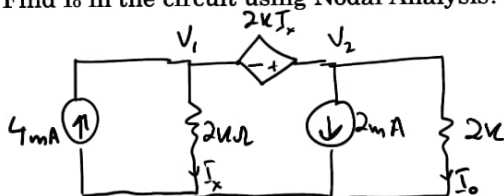
$$\frac{V_2}{12k} + \frac{V_2}{12k} - 2m + \frac{4}{3k} = 0$$

$$V_2 - 12 + 8 = 0$$

$$V_2 = 4V \quad \text{As } V_o = V_2 = 4V$$

NODAL ANALYSIS: DEPENDENT SOURCES

Find I_o in the circuit using Nodal Analysis?



forming KCL Eqn at node 2

$$\frac{V_2}{2k} + 2m + \frac{V_1}{2k} - 4m = 0 \quad \text{--- (1)}$$

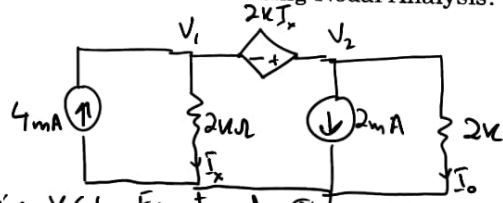
Controlling Eqn

$$V_1 + 2kI_x = V_2 \quad \text{--- (2)}$$

Using KCL at nodes 2 and Forming a controlling equation At node 1 we can simplify the Problem into simple equation Current entering the node is Summed at the node to form The equations.

NODAL ANALYSIS: DEPENDENT SOURCES

Find I_o in the circuit using Nodal Analysis?



Using KCL at nodes 2 and Forming a controlling equation. At node 1 we can simplify the problem into simple equations. Current entering the node is summed at the node to form the equations.

Forming KCL Eqn at node ②

$$\frac{V_2}{2k} + 2m + \frac{V_1}{2k} - 4m = 0 \quad \text{--- ①}$$

Controlling Eqn

$$V_1 + 2kI_x = V_2 \quad \text{--- ②}$$

$$I_x = \frac{V_1}{2k} \quad \text{--- ③}$$

$$V_1 + 2k\left(\frac{V_1}{2k}\right) = V_2 \quad \therefore \boxed{2V_1 = V_2} \quad \text{--- ④}$$

NODAL ANALYSIS: DEPENDENT SOURCES

Put ④ in ①

Simplify the circuit to Obtain nodal voltage.

$$\frac{V_2}{2k} + 2m + \frac{V_2/2}{2k} - 4m = 0$$

$$2V_2 + 8 + V_2 - 16 = 0$$

$$3V_2 = 8$$

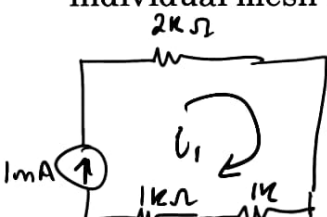
$$\boxed{V_2 = \frac{8}{3} \text{ V}}$$

So

$$I_o = \frac{V_2}{2k} = \frac{8/3}{2k} = \boxed{\frac{4}{3} \text{ mA}}$$

MESH ANALYSIS

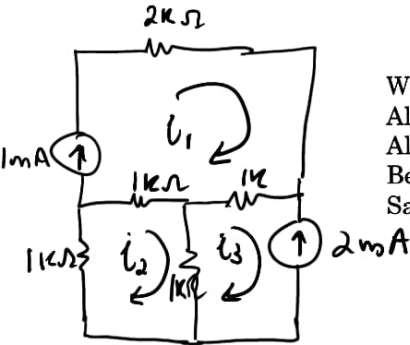
- Mesh Analysis involves solving electronic circuits via finding mesh or loop currents of the circuit. This is done by forming KVL equations for respected loops and solving the equations to find individual mesh currents.



We simply assume clockwise current flow in All the loops and find them to analyze the circuit. Also any independent current source in a loop becomes the loop current as current in series is same.

MESH ANALYSIS

- Mesh Analysis involves solving electronic circuits via finding mesh or loop currents of the circuit. This is done by forming KVL equations for respected loops and solving the equations to find individual mesh currents.

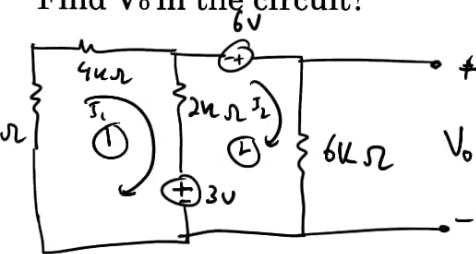


We simply assume clockwise current flow in All the loops and find them to analyze the circuit. Also any independent current source in a loop Becomes the loop current as current in series is Same.

13

MESH ANALYSIS: INDEPENDENT SOURCES

Find V_o in the circuit?



Using KVL at loops 1 and 2, we form KVL equations using the current and Components in the loops in terms of The loop currents. Important thing to look at it the Subtraction of the opposing loop Current in the shared section of the Loop.

Loop ①

$$6kI_1 + (I_1 - I_2)2k + 3 = 0 \quad \text{--- ①}$$

Loop / Mesh ②

$$-6 + 6kI_2 + (I_2 - I_1)2k - 3 = 0 \quad \text{--- ②}$$

14

MESH ANALYSIS: INDEPENDENT SOURCES

Simplifying

$$\begin{aligned} -2kI_2 + 8kI_1 &= -3 \\ 4k(8kI_2 - 2kI_1) &= 9 \end{aligned}$$

$$\frac{30kI_2}{30k} = \frac{33}{30}$$

$$I_2 = \frac{11}{10} \text{ mA}$$

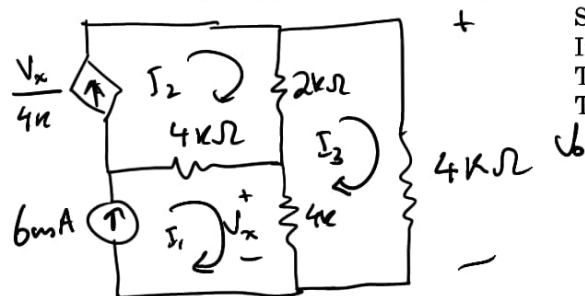
Now once we found I_2

$$V_o = 6k \times I_2 = 6k \times \frac{11}{10} \text{ mA} = \frac{33}{5} \text{ V}$$

15

MESH ANALYSIS: DEPENDENT SOURCES

Find V_o in the circuit using Mesh Analysis?



Simplify the circuit using the Independent sources by assigning them to the mesh currents for the specific loop.

$$I_1 = 6 \text{ mA} \quad (\text{primary current in loop 1}) \quad \text{--- (1)}$$

$$I_2 = \frac{V_x}{4k} \quad \text{where} \quad \text{--- (2)}$$

$$V_x = 4k(I_1 - I_2) \quad \text{--- (3)}$$

16

MESH ANALYSIS: DEPENDENT SOURCES

Obj: Find I_3 using Mesh Analysis

then $V_o = 4k(I_3)$ --- (4)

Form KVL in Main loop 3

$$\text{KVL: } 4k(I_3) + 4k(I_3 - 6\text{mA}) + 2k(I_3 - I_2) = 0 \quad \text{--- (5)}$$

$$\text{So } I_2 = \frac{4k}{4k} (I_1 - I_3) \quad \text{--- (6)}$$

Simplify Using V_x and I_2 .

Now put (6) in (5)

$$4k(I_3) + 4k(I_3 - 6\text{mA}) + 2k(I_3 + I_3 - I_1) = 0$$

$$12kI_3 - 24 - 2k(6\text{mA}) = 0$$

$$12kI_3 = 36$$

$$I_3 = \underline{3 \text{ mA}}$$

$$\text{Hence } V_o = 4k \times 3 \text{ mA} = \underline{12 \text{ V}}$$

17

PRACTICE PROBLEMS

Find V_o in the circuit in Fig. P3.28 using nodal analysis.

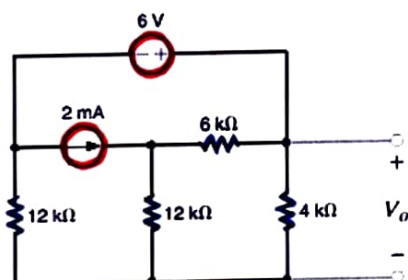


Figure P3.28

PRACTICE PROBLEMS

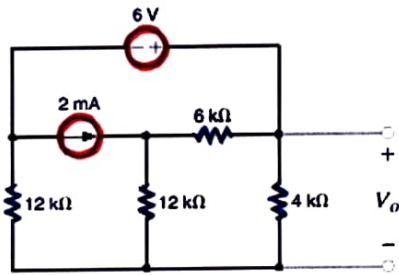
Find V_o in the circuit in Fig. P3.28 using nodal analysis.

Figure P3.28

18

PRACTICE PROBLEMS

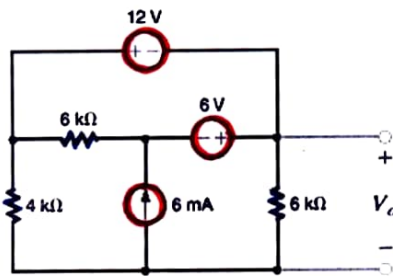
Use nodal analysis to find V_o in the circuit in Fig. P3.29.

Figure P3.29

19

PRACTICE PROBLEMS

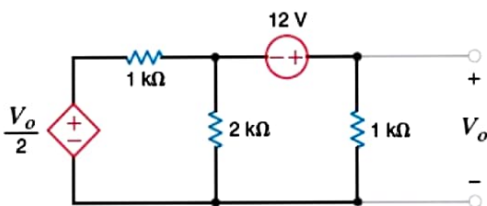
Find V_o in the circuit in Fig. P3.36 using nodal analysis.

Figure P3.36

20

PRACTICE PROBLEMS

Use nodal analysis to find V_1 , V_2 , V_3 , and V_4 in the circuit in Fig. P3.44.

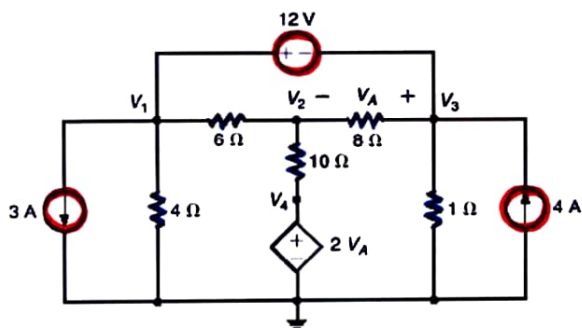


Figure P3.44

PRACTICE PROBLEMS

Use mesh analysis to find V_o in the circuit in Fig. P3.47.

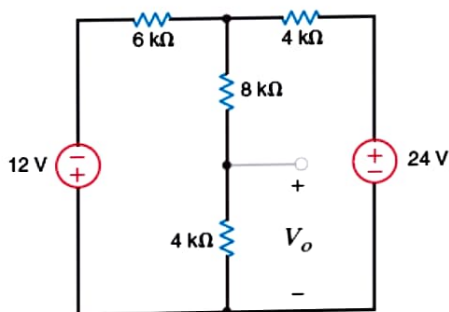


Figure P3.47

PRACTICE PROBLEMS

Use mesh analysis to find V_o in the circuit in Fig. P3.84.

