LECTURE NOTE

ON

ENGINEERING MECHANICS (TH-4)

1ST AND 2ND SEMESTER (DIPLOMA COURSE)



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FUNDAMENTALS OF ENGINEERING MECHANICS

Definitions of Mechanics -

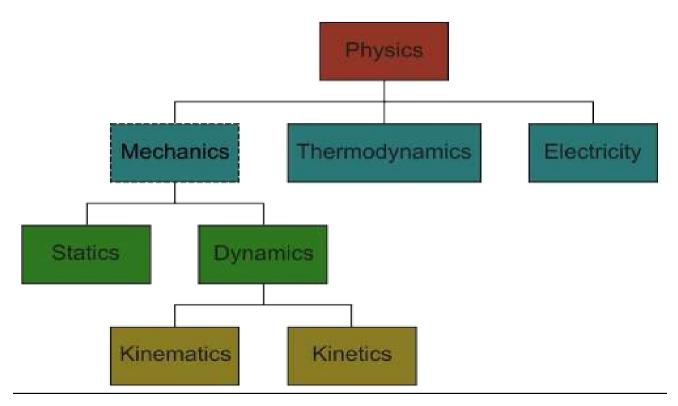
1. A branch of physical science that deals with energy and forces and their effect on bodies.

2. the practical application of **mechanics** to the design, construction, or operation of machines or tools

Definitions of engineering Mechanics

The subject engineering mechanics is the branch of applied science which deals with the laws and principles of mechanics, along with their applications to engineering problems .

Sub division of Engg. Mechanics



- 1. Particle: A particle is defined as an object that has a mass but no size.
- 2. Body: A body is defined as the matter limited in all directions. It has a finite volume and
- 3. Rigid Body: A body in which the particles do not change their relative positions under the
- action of any external force is called as Rigid Body. No body is perfectly rigid.
- 4. Deformable Body: A body in which the particles change their position under the action of any external force is called as Deformable body.
- 5. Mass: Mass of the body is the quantity of matter contained by the body.
- 6. Weight: The force with which the earth attracts any body to itself is called the weight of the body.



- 7. Space: The unlimited universe in which all the materials are located is known as space. It is a three dimensional region.
- 8. Statics: It is the branch of engineering mechanics which deals with the study of bodies at rest under the action of forces.
- 9. Dynamics: It is the branch of engineering mechanics which deals with the study of bodies
- 10. Kinetics: This branch of dynamics is the study of the behaviour of bodies in motion without considering the forces which causing the motion.
- 11. Kinematics: The kinematics studies the behaviour of bodies in motion by considering the
- 12. Force: It is the agent which changes or tends to change the state of rest or motion of a

Force

Defination -

Force is an external agent capable of changing the state of rest or motion of a particular body. It has a magnitude and a direction. The direction towards which the force is applied is known as the direction of the force and the application of force is the point where force is applied.

The Force can be measured using a spring balance. The SI unit of force is Newton(N).

Common symbols:	$F \rightarrow, F$
SI unit:	Newton
In SI base units:	kg·m/s ²

Other units:	dyne, poundal, pound-force, kip, kilo pond
Derivations from other quantities:	$\mathbf{F} = \mathbf{m} \mathbf{a}$
Dimension:	LMT ⁻²

Classification of force system according to plane & line of action

System of Forces

When two, or more than two, forces act on a body, they are called to form a system of forces. Following systems of forces are important from the subject point of view :

- 1. Coplaner forces. The forces, whose lines of action lie on the same plane, are known as coplaner forces.
- 2. Collinear forces. The forces, whose lines of action lie on the same line, are known as collinear forces.
- Concurrent forces. The forces, which meet at one point, are known as concurrent forces. The concurrent forces may or may not be collinear.
- Coplaner concurrent forces. The forces, which meet at one point and their lines of action also lie on the same plane, are known as coplaner concurrent forces.
- Coplaner non-concurrent forces. The forces which do not meet at one point, but their lines of action lie on the same plane, are known as coplaner non-concurrent forces.
- Non-coplaner concurrent forces. The forces, which meet at one point, but their lines of action do not lie on the same plane, are known as non-coplaner concurrent forces.
- Non-coplaner non-concurrent forces. The forces, which do not meet at one point and their lines of action do not lie on the same plane, are called non-coplaner non-concurrent forces.

Effects of a Force

A force may produce the following effects in a body, on which it acts :

- 1. It may change the motion of the body, *i.e.* if a body is at rest, the force may set the body in motion, and if the body is already in motion, the force may accelerate it.
- 2. It may retard the motion of a body.
- 3. It may retard the forces, already acting on a body, thus bringing it to rest or in equilibrium. We shall study this effect in chapter 5 of this book.
- It may give rise to the internal stresses in the body, on which it acts. We shall study this effect in chapters 12 and 13 of this book.

Characteristics of a Force

In order to determine the effects of a force, acting on a body, we must know the following characteristics of a force :

- Magnitude of the force (i.e., 10 kgf, 20 tf, 50 N, 15 kN, etc.)
- The direction of the line, along which the force acts (i.e. along OX, OY or at 30° North or East etc.). It is also known as line of action of the force.
- Nature of the force (i.e., whether the force is push or pull). This is denoted by placing an arrow head on the line of action of the force.
- The point at which (or through which) the force acts on the body.

Principle of transmissibility

The state of rest or of motion of a rigid body is unaltered if a force acting on the body is replaced by another force of the same magnitude and direction but acting anywhere on the body along the line of action of the applied forces. In the following animation, two rigid blocks A and B are joined by a rigid rod. If the system is moving on a frictionless surface, the acceleration of the system in both the cases is given

by,

Acceleration=Applied force/total mass

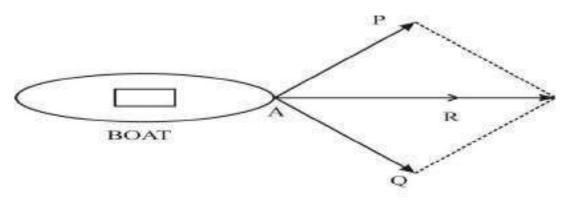
It is independent of the point of application



Principle of Superposition

This principle states that the combined effect of force system acting on a particle or a rigid body is the sum of effects of individual forces.

Consider two forces *P* and *Q* acting at *A* on a boat as shown in Fig.3.1. Let *R* be the resultant of these two forces *P* and *Q*. According to Newton's second law of motion, the boat will move in the direction of resultant force *R* with acceleration proportional to *R*. The same motion can be obtained when *P* and *Q* are applied simultaneously.



Principle of Superposition

Action & Reaction Forces

1. A force is a push or a pull that acts upon an object as a results of its interaction with another object.

2. Forces result from interactions but some forces result from contact interactions (normal, frictional, tensional, and applied forces are examples of contact forces) and other forces are the result of action-at-a-distance interactions (gravitational, electrical, and magnetic forces). According to Newton, whenever objects A and B interact with each other, they exert forces upon each other. When you sit in your chair, your body exerts a downward force on the chair and the chair exerts an upward force on your body. There are two forces resulting from this interaction - a force on the chair and a force on your body. These two forces are called action and reaction forces and are the subject of Newton's third law of motion. Formally stated, Newton's third law is:

For every action, there is an equal and opposite reaction.

The statement means that in every interaction, there is a pair of forces acting on the two interacting objects. The size of the forces on the first object <u>equals</u> the size of the force on the second object. The direction of the force on the first object is <u>opposite</u> to the direction of the force on the second object. Forces <u>always</u> come in pairs - equal and opposite action-reaction force pairs.

Concept of Free Body Diagram

Free-body Diagrams. To investigate the equilibrium of a constrained body, we shall always imagine that we remove the supports and replace them by the *reactions* which they exert on the body. Thus,

3.1. Free Body

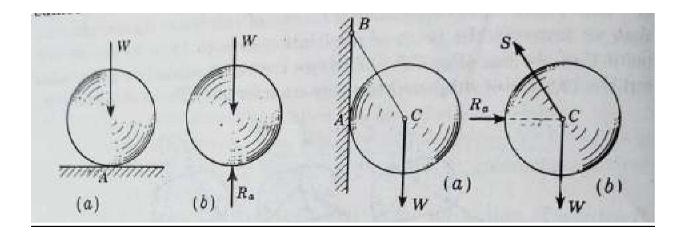
A body is said to be free body if it is isolated from all other connected members,

3.2. Free Body Diagram

Free body diagram of a body is the diagram drawn by showing all the external forces and reactions on the body and by removing the contact surfaces.

Steps to be followed in drawing a free body diagram

- 1. Isolate the body from all other bodies.
- 2. Indicate the external forces on the free body. (The weight of the body should also be included. It should be applied at the centre of gravity of the body.)
- 3. The magnitude and direction of the known external forces should be mentioned.
- 4. The reactions exterted by the supports on the body should be clearly indicated.
- 5. Clearly mark the dimensions in the free body diagram.



Resolution of a Force

The process of splitting up the given force into a number of components, without changing its effect on the body is called resolution of a force. A force is, generally, resolved along two mutually perpendicular directions.

In fact, the resolution of a force is the reverse action of the addition of the component vectors.

2.13. Principle of Resolution

It states, "The algebraic sum of the resolved parts of a number of forces, in a given direction, is equal to the resolved part of their resultant in the same direction."

Proof

Now consider for simplicity, two forces P and Q; which are represented in magnitude and direction by the two adjacent sides OA and OB of a parallelogram OACB as shown in Fig. 2.2.

We know that the resultant (R) of these, two forces Pand Q will be represented, in magnitude and direction, by the diagonal OC of the parallelogram.

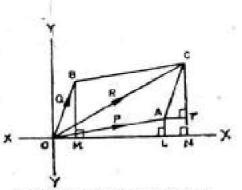


Fig. 2-2 Principle of resolution.

Let OX be the given direction, in which the forces are to be resolved. Now draw AL, BM, and CN perpendiculars from the points A, B and C on OX. Similarly, draw AT perpendicular from the point A on CN.

In the two triangles OBM and ACT, the two sides OB and AC are parallel and equal in magnitude. Moreover, the two sides OM and AT are also parallel.

$$OM = AT = LN$$

Now from the geometry of the figure, we find that

$$ON = OL + LN = OL + OM \dots (\dots LN = OM)$$

But ON is the resolved part of the resultant R, OL is the resolved part of the force P, and OM is the resolved part of the force Q.

Hence resolved part of R along OX

=Resolved part of P along OX

+Resolved part of Q along OX

Note: We have considered, for the sake of simplicity only, the two forces P and Q. But this principle may be extended for any number of forces.

2.14. Method of Resolution for the Resultant Force

The resultant force, of a given system of forces, may be found out by the method of resolution as discussed below :

1. Resolve all the forces vertically and find the algebraic sum of all the vertical components (i.e., ΣV).

2. Resolve all the forces horizontally and find the algebraic sum of all the horizontal components (i.e., ΣH).

3. The resultant R of the given forces will be given by the equation :

$$R = \sqrt{(\Sigma V)^2 + (\Sigma H)^2}$$

4. The resultant force will be inclined at an angle θ , with the horizontal, such that

$$\tan\,\theta\,=\,\frac{\Sigma V}{\Sigma H}$$

Note: The values of the angle θ will vary depending upon the values of ΣV and ΣH as discussed below :

- 1. When ΣV is +ve, the resultant makes an angle between 0° and 180°. But when ΣV is -ve, the resultant makes an angle between 180° and 360°.
- 2. When ΣH is +ve, the resultant makes an angle between 0° and 90° and 270° to 360°. But when ΣH is -ve, the resultant makes an angle between 90° to 270°.

Example 2.3. A triangle ABC has its sides AB = 40 mm along positive x-axis and sides BC = 30 along positive y-axis. Three forces of 40 kgf, 50 kgf and 30 kgf act along the sides AB, BC and CA respectively. Determine the resultant of such a system of forces.

(Osmania University, 1985)

Solution.

The system of the given forces is shown in Fig. 2.3. From the geometry of the figure, we find that the triangle ABCis a right angled triangle in which the *side AC = 50 mm. Moreover.

 $\sin \theta = \frac{30}{50} = 0.6$ $\cos \theta = \frac{40}{50} = 0.8$

50 kg1 30 30 4 30 4 50 kg1 30 30 30 4 50 kg1 30 30 4 50 kg1 30 50 kg1 50

and

Resolving all the forces horizontally (i.e. along AB)

$$\Sigma H = 40 - 30 \cos \theta = 40 - 30 \times 0.8 = 16 \, \text{kgf}$$
 (i

and now resolving all the forces vertically (i.e. along BC),

$$\Sigma V = 50 - 30 \sin \theta = 50 - 30 \times 0.6 = 32 \text{ kef}$$
 ...

We know that the magnitude of the resultant force,

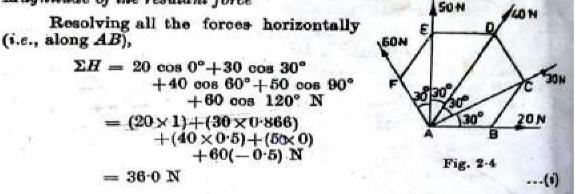
$$R = \sqrt{(\Sigma H)^{3} + (\Sigma V)^{3}} = \sqrt{(16)^{2} + (32)^{2}} \quad \text{kgf}$$

= 35.8 kgf Ans.

Example 2.4. The forces 20 N, 30 N, 40 N, 50 N and 60 N are acting on one of the angular points of a regular hexagon, towards the other five angular points, taken in order. Find the magnitude and direction of the resultant force. (Cambridge University)

Solution.

The system of the given forces is shown in Fig. 2.4. Magnitude of the resulant force



and now resolving the all forces vertically (i.e. at right angles to AB)

 $\Sigma V = 20 \sin 0^{\circ} + 30 \sin 30^{\circ} + 40 \sin 60^{\circ}$ +50 sin 90° + 60 sin 120° N = (20×0) + (30) + (0.5) + (40×0.866) + (50×1) + (60×0.866) N = 151.6 N

We know that magnitude of the resulant force.

$$R = \sqrt{(\Sigma H)^2 + (\Sigma V)^2} = \sqrt{(36 \cdot 0)^2 + (151 \cdot 6)^2} N$$

= 155.8 N Ans.

Direction of the resultant force

ta

...

Let θ = Angle, which the resultant makes with the horizontal (i.e., AB).

$$\frac{n}{2} \theta = \frac{\Sigma r}{\Sigma H} = \frac{151 \cdot 6}{36 \cdot 0} = 4 \cdot 211$$

$$\theta = 76^{\circ} 39' \text{ Ans.}$$

OF

...(ii)

Resultant Force

If a number of forces, P, Q, R, \dots etc. are acting simultaneously on a particle, it is possible to find out a single force which could replace them i.e. which would produce the same effect as produced by all the given forces. This single force is called *resultant* force, and the given forces P, Q, R, \dots etc. are called component forces.

Composition of Forces

The process of finding out the resoltant force of a number of given forces is called *composition of forces* or compounding of forces.

Methods for the Resultant Force

Though there are many methods for finding out the resultant force of a number of given forces, yet the following are important from the subject point of view :

1. Analytical method, 2. Graphical method.

Analytical Method for Resultant Force

The resultant force, of a given system of forces, may be found out analytically by the following methods :

1. Parallelogram law of forces, 2. Method of resolution.

Parallelogram Law of Forces

It states "If two forces, acting simultaneously on a particle, be represented in magnitude and direction by the two adjacent sides of a parallelogram : their resultant may be represented in magnitude and direction by the diagonal of the parallelogram, which passes through their point of intersection." Mathematically, resultant force,

$$R = \sqrt{P^2 + Q^2 + 2PQ} \cos \theta$$

and

$$= \frac{Q \sin \theta}{P + Q \cos \theta}$$

where P and Q = Forces whose resultant is required to be found

out,

- θ Angle between the forces P and Q, and
- α Angle which the resultant force makes with one of the forces (say P).

COM^B

Note. If the angle (α) which the resultant force makes with the other force Q, then

$$\tan x = \frac{P \sin \theta}{Q + P \cos \theta}$$

tars or -

Cor.

1. If $\theta = 0$ i.e., when the forces act along the same line, then R = P + Q ...(since cos $\theta^{n} = I$)

2. If $\theta = 90^{\circ}$ i.e., when the forces at at right angle, then $R = \sqrt{P^2 + Q^2}$...(since cos $20^{\circ} = 0$)

3. If $\theta = 180^{\circ}$ i.e., when the forces act along the same straight line but in opposite direction then

4. If the two forces are equal i.e. when
$$P = Q$$

4P8 cos2 - = 2P cos

then
$$R = \sqrt{P^2 + P^2 + 2P^2 \cos \theta} = \sqrt{2P^2 (1 + \cos \theta)}$$

= $\sqrt{2P^2 \times 2 \cos^2 \frac{\theta}{2}}$... $(\because 1 + \cos \theta = 2$

Example 2.1. Two forces act at an angle of 120°. The bigger force is of 40 N and the resultant is perpendicular to the smaller one. Find the smaller force.

Solution Given: P = 40 N; $\angle AOO = 120$; $\angle BOO = 90^{\circ}$ $\therefore \angle AOB$, $\alpha = 120^{\circ} - 90^{\circ}$ $= 30^{\circ}$ Let $\cdot Q$ = Smaller force, Fig. 2-1 We know that

$$\tan \alpha = \frac{Q \sin \theta}{P+Q \cos \theta}$$

$$\tan 30^{\circ} = \frac{Q \sin 120^{\circ}}{40+Q \cos 120^{\circ}} = \frac{Q \sin 60^{\circ}}{40+Q (-\cos 60^{\circ})}$$

$$0.577 = \frac{Q \times 0.866}{40-Q \times 0.5} = \frac{0.866}{40-0.5} \frac{Q}{Q}$$

$$40 - 0.5 Q = \frac{0.866}{0.577} = 1.5 Q$$

$$2Q = 40 - \text{ or } Q = 20 \text{ N} \text{ Ans.}$$

• Example 2.2. Find the magnitude of the two forces, such that if they act at right angles, their resultant is $\sqrt{10}$ N. But if they act at 60°, their resultant is $\sqrt{13}$ N. (Bihar University, 1986)

Solution

 $\leq T_{\rm c}$

10

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Let P and Q = Two given forces.

First of all, consider the two forces acting at right angles. We know that when the angle between the two given forces is 90°, then the resultant force (R)

$$\sqrt{10} = \sqrt{P^2 + Q^2}$$

10 = P^2 + Q^4(Squaring both sides)

Similarly, when the angle between the two forces is 60° , then the resultant force (R)

$$\begin{array}{rcl} & \sqrt{13} &= \sqrt{P^{2} + Q^{2} + 2PQ} \cos 60^{\circ} \\ & \ddots & 13 = P^{2} + Q^{2} + 2PQ \times 0.5 & \dots & \text{Squaring both sides}) \\ &= 10 + PQ & \dots & (\text{Substituting } P^{2} + Q^{2} = 10) \\ PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 13 - 10 = 3 \\ \hline PQ &= 10 + 6 = 16 \\ \hline PQ &= 10 + 10 \\ \hline PQ &= 10 +$$

General Laws for the Resultant Force

The resultant force, of a given system of forces, may also be found out by the following general laws :

1. Triangle law of forces. 2. Polygon law of forces.

Triangle Law of Forces

It states, "If two forces acting simultaneously on a particle, be represented in magnitude and direction by the two sides of a triangle, taken in order-; their resultant may be represented in magnitude and direction by the third side of the triangle, taken in opposite order."

Polygon Law of Forces

Solution.

It is an extension of Triangle Law of Forces for more than two forces, which states, "If a number of forces acting simultaneously on a particle, be represented in magnitude and direction, by the sides of a polygon taken in order; then the resultant of all these forces may be represented, in magnitude and direction, by the closing side of the polygon, taken in opposite order."

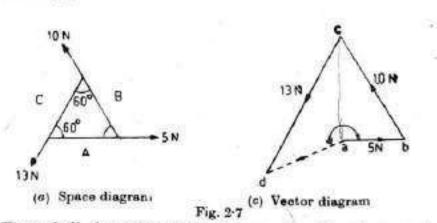
Graphical (Vector) Method for the Resultant Force

This is another name given to the method of finding out, graphically, magnitude and direction of the resultant force by the polygon law of forces. It is done as discussed below :

- Construction of space diagram (position diagram). It means the construction of a diagram showing the various forces (or loads) alongwith their magnitude and lines of action.
- Use of Bow's notations. All the forces in the space diagram are named by using the Bow's notations. It is a convenient method in which every force (or load) is named by two capital letters, placed on its either 'side in the space diagram.
- Construction of vector diagram (force diagram). It means the construction of a diagram starting from a convenient point and then go on adding all the forces vectorially one by one (keeping in view the directions of all the forces) to some suitable scale.

Now the closing side of the polygon, taken in opposite order, will give the magnitude of the resultant force (to the scale) and its direction.

Example 2.7. A particle is acted upon by three forces equal to 5 N, 10 N and 13 N, along the three sides of an equilateral triangle, taken in order. Find graphically the magnitude and direction of the resultant forces. (Madurai University, 1985)



First of all, draw the space diagram for the given system of forces (acting along the sides of an equilateral triangle) and name the forces according to Bow's notations as shown in Fig. 2.7 (c). The 5 N force is named as AB, 10 N force as BC and 13 N force as CD.

Now draw the vector diagram for the given system of forces as shown in Fig. 2.7 (b) and as discussed below :

- 1. Select some suitable point a and draw ab equal to 5 N to some suitable scale and parallel to the force AB of the space diagram.
- 2. Through b, draw bc equal to 10 N to the scale and parallel to the force BC of the space diagram.
- 3. Similarly, through c, draw cd equal to 13 N to the scale and parallel to the force CD of the space diagram.
- 4. Join ad, which gives the magnitude as well as direction of the resultant force.
- 5. By measurement, we find the magnitude of the resultant force is equal to 7 N and acting at an angle of 200° with ab. Ans.

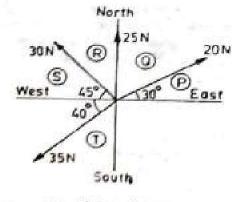
Example 2.8. The following forces act at a point :

(i) 20 N inclined at 30° towards North of East.

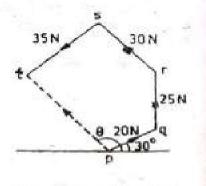
- (ii) 25 N towards North.
- (iii) 30 N towards North West, and
- (iv) 35 N inclined at 40° towards South of West.

Find the magnitude and direction of the resultant force. (Jiwaji University, 1986)

*Solution



(a) Space diagram



(c) Vector diagram

Fig. 2-8

First of all, draw the space diagram for the given ays. In of forces (acting at point O) and name the forces according to Be W^{*} notations as shown in Fig. 2.8 (a). The 20 N force is named as PV the 25 N force as QR, 30 N force as RS and 35 N force as ST. Now draw the vector diagram for the given system of forces as shown in Fig. 2.8 (b) and as discussed below :

- Select some suitable point p and draw pg equal to 20 N to some suitable scale and parallel to the force PQ.
- Through g, draw gr equal to 25 N to the scale and parallel to the force QR of the space diagram.
- 3. Now through r, draw rs equal to 30 N to the scale and parallel to the force RS of the space diagram.
- Similarly, through s, draw st equal to 35 N to the scale and parallel to the force ST of the space diagram.
- Join pt, which gives the magnitude as well as direction of the resultant force.
- By measurement, we find that the magnitude of the resultant force is equal to 45.6 N and acting at an angle of 132° with the horizontal *i.e.* East-West line. Ans.

2.19. Relation Between Mass and Weight

(The term 'mass' is defined as the matter contained in a body,) whereas the term weight' is defined as the force with which a body is attracted towards the centre of the earth? From the above mentioned two definitions, it is clear that the units of mass are kg, tonnes etc.) whereas the units of weight are N, kN and kgf etc.)

It will be interesting to know that there is an important relation between the mass and weight of a body, which will be discussed in detail in chapter 23 of this book. But for the time being, it may be taken as

$$M = m q = 9.8 \text{ m}$$

 $P = \text{Weight of the body in newtons}$

... (g = 9.8)

where

m = Mass of the body in kg, and

9 Gravitational acceleration whose value is taken as 9.8 m/sec².

Example 2.9. A machine shaft BC 1.5 m long and of mass 100 kg is supported by two ropes AB and CD as shown in Fig. 2.9 given below :

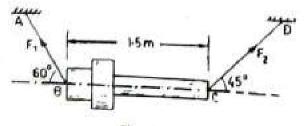


Fig. 2-9

Calculate the tensions F1 and F2 in the rope AB and CD.

(London University)

Solution. Given : Mass of shaft = 100 kg

We know that weight of the mass

 $= m.g = 100 \times 9.8 = 980$ N

Resolving the forces horizontally (i.e. along BC) and equating the same,

 $F_1 \cos 60^\circ = F_2 \cos 45^\circ$

:
$$F_1 = \frac{\cos 45^\circ}{\cos 60^\circ} \times F_2 = \frac{0.707}{0.5} \times F_2 = 1.414 F_2 \dots (i)$$

and now resolving the forces vertically,

$$F_{1} \sin 60^{\circ} + F_{2} \sin 45^{\circ} = 980$$

$$(1 \cdot 414 \ F_{1}) \ 0 \cdot 866 + F_{2} \times 0 \cdot 707 = 980$$

$$1 \cdot 93 \ F_{2} = 980$$

$$\therefore F_{3} = 980/1 \cdot 93 = 507 \cdot 8 \ \text{M Ans.}$$

$$F_{2} = 1 \cdot 414 \times 507 \cdot 8 = 718 \ \text{M Ans.}$$

and

Moment of a Force

It is the turning effect produced by a force, on the body, on which it acts.¹ The moment of a force is equal to the product of the force and the perpendicular distance of the point, about which the moment is required, and the line of action of the force. Mathematically, moment,

$$M = P \times l$$

where

P = Force acting on the body, and

l = Perpendicular distance between the point, about which the moment is required and the line of action of the force.

Graphical Representation of Moment

Consider a force P represented, in magnitude and direction, by the line AB. Let O be a point, about which the moment of this force is required to be found out, as showing in Fig. 3-1.

From O, draw OC perpendicular to AB. Join OA and OB.

Now moment of the force P about O

 $= P \times O\hat{C} = AB \times OC$

But $AB \times OC$ is equal to twice the area of the triangle ABO.

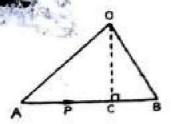


Fig. 3.1

Thus the moment of a force, about Representation of moment any point, is geometrically equal to twice the area of the triangle, whose base is the line representing the force and whose vertex is the point, about which the moment is taken.

Units of Moment

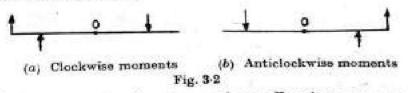
Since the moment, of a force, is the product of force and distance, therefore the units of the moment will depend upon the units of force and distance. Thus, if the force is in Newton and the distance is in metres, therefore the units of moment will be Newtonmetre (briefly written as N-m). Similarly, the units of moment may be kN-m (i.e. kN×m), N-mm (i.e. N×mm) kgf-m (kgf×m) etc

Types of Moments

Broadly speaking, the moments are of the following two types :

1. Clockwise moments. 2. Anticlockwise moments.

Clockwise Moment



It is the moment of a force, whose effect is to turn or rotate the body, in the same direction in which the hands of a clock move, as shown in Fig. 3.2 (a).

Anticlockwise Moment

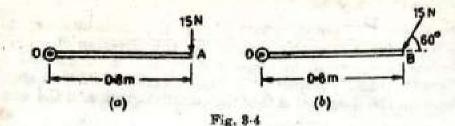
It is the moment of a force, whose effect is to turn or rotate the bady, in the opposite direction in which the hands of a clock move, as shown in Fig. 3.2 (b).

Note. The general convention is to 'take clockwise moment as possitive and applelockwise moment as negative.

Varignon's Principle of Moments (or Law of Moments)

It states, "If a number of coplanar forces are acting simultaneously on a particle, the algebraic sum of the moments of all the forces about any point is equal to the moment of their resultant force about the same point."

Example 3.1. A force of 15 N is applied perpendicular to the edge of a door 0.8 m wide as shown in Fig. 3.4 (a). Find the moment of the force about the hinge.



If this force is applied at an angle of 60° to the edge of the same door, as shown in Fig. 3.4 (b), find the moment of this force. (Gujarat University, 1984)

Solution. Given : P = 15 N ; l = 0.8 m

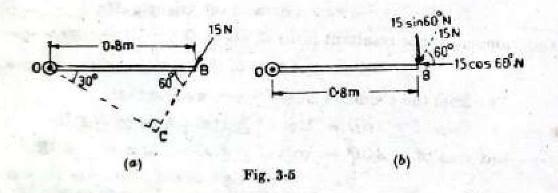
Moment when the force acts perpendicular to the door

We know that the moment of the force about the hinge,

$$= P \times l = 15 \times 0.8 = 12.0$$
 N-m Ans.

Moment when the force acts at an angle of 60° to the door

This part of the example may be solved either by finding out the perpendicular distance between the hinge and the line of action of the force as shown in Fig. 3.5 (a) or by finding out the vertical component of the force as shown in Fig. 3.4 (b).



From the geometry of Fig. 3.5 (a), we find that the perpendicular distance between the line of action of the force and hinge,

 $OC = OB \sin 60^\circ = 0.8 \times 0.866 = 0.693 \text{ m}$

Moment = 15×0.693 = 10.4 N Ans.

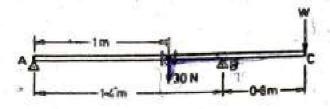
In the second case, we know that the vertical component of the force

. .

 $= 15 \sin 60^{\circ} = 15 \times 0.866 = 13.0 \text{ N}$

Moment = 13×0.8 = 10.4 N Ans.

Example 3.2. A uniform plank ABC of weight 30 N and 2 m long is supported at one end A and at a point B 1.4 m from A as shown in Fig. 3.6.



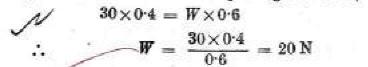


Find the maximum weight W, that can be placed at C, so that the plank does not topple. (Patna University, 1986)

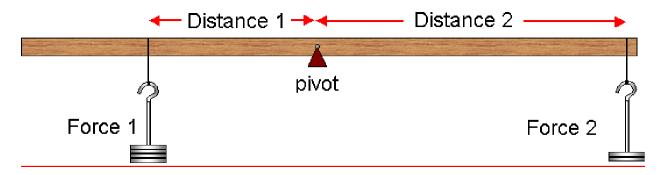
Solution. Given : W = 30 N; Length ABC = 2 m

We know that weight of the plank (30 N) will act at its midpoint, as it is of uniform section. This point is at a distance of 1 m from A or 0.4 m from B.

We also know that if the plank is not to topple, then the reaction at A should be zero for the maximum weight at C. Now taking moments about B and equating the same.



Law of moments



When an object is balanced (in equilibrium) the sum of the clockwise moments is equal to the sum of the anticlockwise moments.

Force 1 x its distance from pivot = Force 2 x distance from the pivot

 $F_1 d_1 = F_2 d_2$

COUPLE

Definition – Couple, in mechanics, pair of equal parallel forces that are opposite in direction. The only effect of a couple is to produce or prevent the turning of a body.

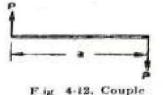
- The turning effect, or moment, of a couple is measured by the product of the magnitude of either force and the perpendicular distance between the action lines of the forces.

Arm of a Couple

The perpendicular distance (a), between the lines of action of the two equal and opposite parallel forces, is known as arm of the couple as shown in Fig. 4.12.

Moment of a Couple

The moment of a couple is the product of the force (*i.e.* one of the forces of the two equal and opposite parallel forces) and the arm of the couple. Mathematically :



Moment of a couple $= P \times p_{\sim}$

where

$$P = Force, and$$

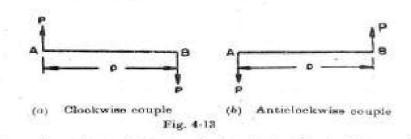
a = Arm of the couple.

Classification of Couples

The couples may be, broadly, classified into the following two categories, depending upon their direction, in which the couple tends to rotate the body, on which they act :

1. Clockwise couple, and 2. Anticlockwise couple.

Clockwise Couple



A couple, whose tendency is to rotate the body, on which it acts, in a clockwise direction, is known as a clockwise couple as shown in Fig. 4-13 (a). Such a couple is also called *positive* couple.

Anticlockwise Couple

A couple, whose tendency is to rotate the body, on which it acts, in an *anticlockwise direction*, is known as an anticlockwise couple as shown in Fig. 4.13 (b). Such a couple is also called a *negative* couple.

Characteristics of a Couple

A couple (whether clockwise or anticlockwise) has the following characteristics :

 The algebraic sum of the forces, constituting the couple, in zero.

1240

- 2. The algebraic sum of the moments of the forces, constituting the couple, about any point is the same, and equal to the moment of the couple itself.
- 3. A couple cannot be balanced by a single force, but can be balanced only by a couple ; but of opposite sense.
- 4. Any number of coplaner couples can be reduced to a single couple, whose magnitude will be equal to the algebraic sum of the moments of all the couples.

Example 46. A square ABCD has forces acting along its sides as shown in Fig. 4.14. Find the values of P and Q, if the system reduces to a couple. Also find magnitude of the couple, if the side of the square is 1 m. (Allahabad University, 1985)

Solution. Given : Length of square = 1 m

Values of P and Q

We know that if the system reduces to a couple, the resultant force in horizontal and vertical directions is zero. Therefore resolving the forces

 $100 - 100 \cos 45^{\circ} - P = 0$

:. $P = 100 - 100 \cos 45^{\circ} N$ = $100 - 100 \times 0.70 N$ = 29.3 N Ans.

Now resolving the forces vertically,

 $200 - 100 \sin 45^{\circ} - Q = 0$

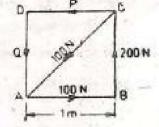
 $Q = 200 - 100 \times 0.707 = 129.3$ N Ans.

Magnitude of the Couple

We know that moment of the couple is equal to the algebraic sum of the moments about any corner. Therefore moment of the couple (taking moments about A)

 $= (-200 \times 1) + (-P \times 1) = -200 - 29.3 \times 1$ N-m

= -229 3 N-m Ans.(Minus sign due to anticlockwise)





CHAPTER-02 EQUILIBRIUM OFFORCES

of a system of forces acting simulteneously on a body produces no change in the state of rest on the state of notion of the body, the system of forces is said to be in equillm.

A system of forces an be in equeil " under two situations.

Ist of the resultant of a numbers of forces arting at a peint is xerco.

Ly when the resultant of a system of forces applied on a particle has a non-zero value, then the particle will reamain at rest by applying a force equal in magnitude but opposite in dirin of the resultant.

Principles of Equilibrium

Two - force principle

When a body is orched upon by tues, equal opposite collinear forces, the norultant force to zuco. The system of forces is easily to be in equilibrium.

Three non-parallel forces will be in equility when Three force primiple they lie in one plane, intercent of one peint and there free vertons form a closed prisargle.

Laneze Theorem of three coplanners concurrent forces are acting on a bedy hapt in equilibrium, then each forces is propertion to the line angle between other trees forces and the const. of propertionality is the same. = con 0.P sinja Sinn P. R. R seting at point 0. het force gince p. q, k are in equilibrium the triangle of forces shell be a closed one. (vertor diagram) Draw as line AB 1 to forcer. Premend A dreaw a live 11 top. name of AC. prem's' drew alone 11+0 p. It will intervient the line Ats at B. 2A 2 T-9 49 = T-B LC ZT-V Applying sine reale to the BABC. Sin(T- a) sin(#-p) sin(T-n) sens SUNN

A the elastic lamp usergheig 201 is supersted from a point a supersted by 2 wine to 2 BC. The point A.B are at some level. Ac makes an angle 60° and BC makes 45° to horizontal as sheven in fig. Determine the tension in the straing AC 2 BC.

self w at c = 20 * A250 TAC - tension in AC TBC = " " BC. SON sinar' sinp sinv

20 = TBC AC AC sin 135 . sin 150; 150 TAC = 20x 20135 = 14.14 = 14.95 AN Sinto TBC = <u>ao n sin 300</u> Sin75°

(2) Boby weighing 10N is expendended from a forred paint by astrong 15cm long & is upt at rest by a transit force p at a distance of 9 cm from the vertical line dreven through the paint of cuspension. What are the train of the string & the value of P?

Let terrier T beveloped in the drining AB. The point B is in equil , moler the three forcies to TAB. 2P. 2 cm les 2 480 = 0-W= ION Applying Lamile theorem P TAB 2 10 Sin (90+0) Sin90 Sen (180-0)

 $\frac{1}{\cos 2} = \frac{T}{1} = \frac{10}{\sin 2}$

From DABC

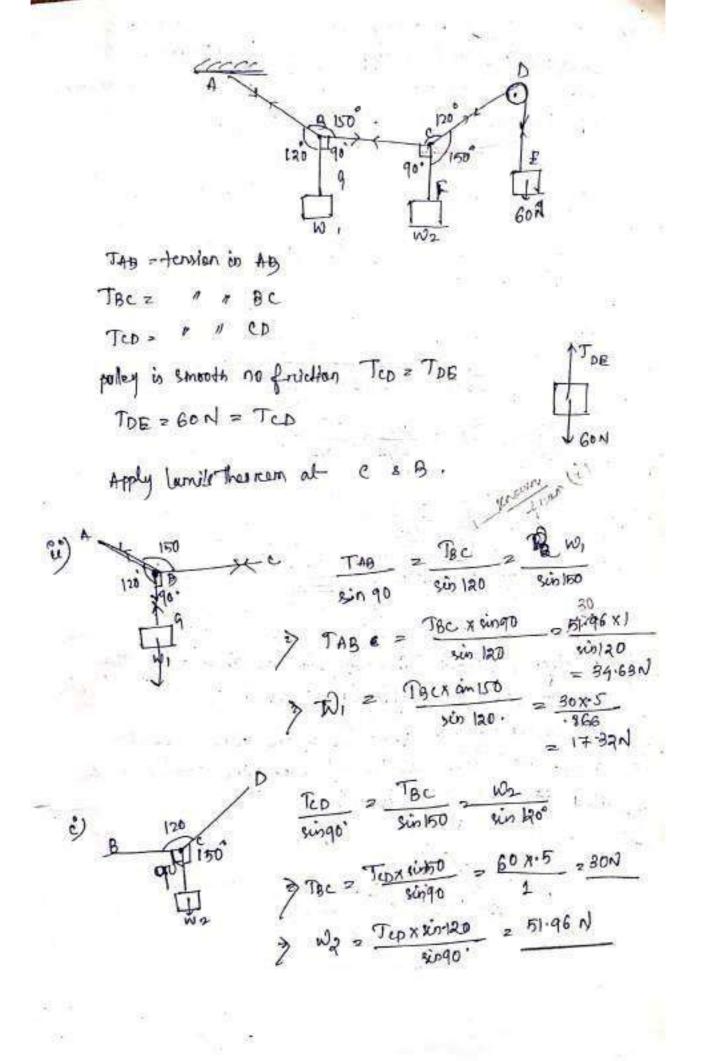
 $ABR = Ac^{2} + Bc^{2}$ $Ac^{2} = AB^{2} - Bc^{2}$ $= B^{2} - g^{2}$ = 2as - 81 $Ac = \sqrt{144}$ = 1204ny

1 2

 $\frac{8in\Theta}{AB} = \frac{AC}{AB} = \frac{12}{15} = 2.0.8$ $\frac{P}{AB} = \frac{12}{15} = 2.0.6$ $\frac{P}{AB} = \frac{9}{15} = 2.0.6$ $\frac{F}{AB} = \frac{10}{15} = 2.0.6$

) T = 10 = 12.5 A A

A. fine light officing ABCDE with one end A fixed, for weeights Wi & W2 attached to it at B and c. The string parses tround as smoothing ulley D canning we born at freezend E as showen in fig. If the position of equ?, BC is honizental with AB & CD makes an angle 150° & 120° with BC. Dind
Pension in pention AB, BC, DE.
Magnitude of W1 & W2



Twee equal and heavy sphered of 40 mm reading and in equell must in a cyp of reading 120 rom. Show 2 that the reambers the cup & one sphere is doubly ap-that begin the twee spheres. As sherren in the sin 120 $= \frac{W}{V^3/a} = \frac{P}{Va}$ R= F = 2PV A writerom wheel 600 mm den neeighing 5 km rust aganist a riegid reichargulare black of momm heigh as showen in the fig. Lind the mins force greep. to tures the wheel over the covener A & rener" on the block, Soomm

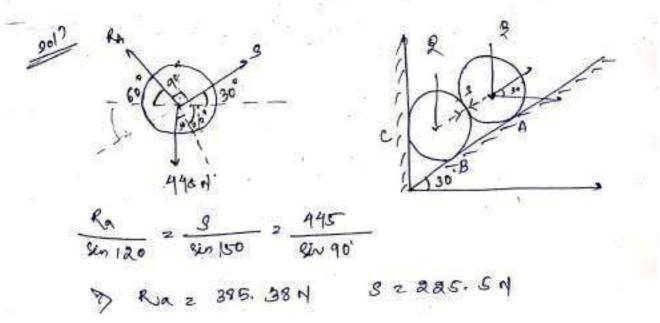
160 120 5 UN 3000 (A sigo Rin120 1in 150 4.33 KM 1330N P = 2 2500 N 87 2.5 KA Two spheres with center A& B. lying is equally, in sup with outers of , had the a sphere contact at ptc. and sphere A heith cup @ 2 sphere & with cup E - grean at DIE p - ren at c. = 120-40 from geometry. OD = 120 mm AD = 40 mm 280. similarly OB= 80. AB = AC+CB 240+40 280 OAB becomes equilateral Δ. R W Zinko qui R= 13/2 = 1/2 R= 2P

2) A smooth circular cylinder of scordius 1.5 meter is laying en triangular greeve, are side if which makes 15° angle 2 other 40° angle, weith horizental. Find the scenefions at the surface of content. If there is no friction & the cylindon weight 100N. RA: 40 100 N RA - ROOL of A Ro - Real of B sin (180-15) sin (15+45' sin(180 - 40) = 78.54 R3 ~ 31.61 A string. ABCD altached to fined peinds AD has two equal veeights of 1000 N alforshed to BIC. This weight ref with the pontions AB & cD inclined angle as shown in for 60 670N 1000N Eind the tension in AB, BC & CD

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Sot free body diagram. 1000. 1000 TAB sin (180-30) sin 150 1732 1 748 z = 1000 N TOD TBC 1000 TOP 120 1000 N

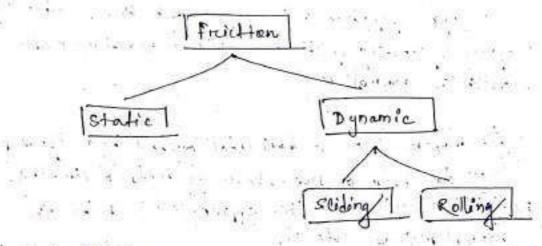
Two identical rollers each of weight &= 445 N are Supported by an inclined place and a vertical wall as showen in the fig. A examing smooth surface, Pind the greations induced at pt pt A, B, C



Pp Rb 10 530 Resolving vertically 60 fy 20 21 Rb cos 30 = 945 + S son 30' 3 690003 Rb 2/ Roolining horisentally Sa 20 Rb sin 30 + 5 6330 = Rc Re z N $\pm x$ Scanned by CamScanner

CHAPTER > 03 FRICTION

8.1 When a bedy slides an tends to slide even another chanface on appoing force; called as force of fruitian. It acts tangent to the surface and apposite to the direction the body is moving ex fords to more.



Listatic Privilian

It is experienced by a bady when it is at next ore when the body is fendito move.

Leiding Procesion It is experienced when a bedy slids once arother

body.

4 Rolling Preiction

It is experienced when a body scalls are anothere body.

1.464 1.1.1

Liemiting Freiclion

Which comes in to play, when a bealy) with begins to Relide over another bedy , known as limiting friction.

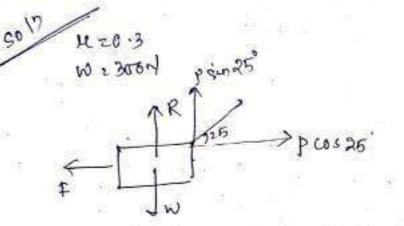
If the applied forces is less than the limiting fristion, the body runains at rust a the fristions is called static friction, which may have any value beto zero to limiting friction. Angle of froition Engle of friction is the angle which the resultant of foreve of limiting friction & normal reaction makes with the normal real. - Let mass m kept on howizertal. pulled by a fare p. when the body is Just about to slide a limiting (F) frittion well act on the apposite ride. R be the normal ream of who w. Let oc is the renaultant bet R & F., makes an angle of with R. $+an \phi = \frac{BC}{B0} = \frac{+}{R}$ A OBC Coefficient of friction of in the realist of friction to the riormal scenetion betn a bodies denoted by u " u= E= "tan " > F= UR

Angle of report

consider the block of weight w nuting an an inclined plane which makes an angle a with horizental. To When a is very small the block will suf on the plane of a micriaries gradually ; a stage is reached at which the black will. starts to click . That angle it salled as angle of rapose. waso-W. COS B AT =0 F= WSOND W sind = F. tono = F ton op = tan 8-7 9-0

Laws of frostions agaa ayaa 🎯 Ly have of static fristion g an Meri II - Meri The force of friction already out opposite on the linec? of applied force. 200 M A A The magnifuide of force of fridian is exactly equal to the applied force, which tend to many the body . -. The magnitude of the liming friction bears a const ratio to normal reaction bet the tree surface. F/R = consf. -> The force of friction is independent of the area of contact betn & surface : -> The force of friction depends yoon the surface roughness. -> Lower of Dynamic friction $\alpha \in [n^{2}]$ → the forces of friction always act in a direction opposite in which the bedy is moving. -> For moderate speed the force of friction ecomains court, but it decreases with increase of the speed. e al e que of a least the Scanned by CamScanner

2) A bedy of veright 300N is lying on a naugh ponisental plane having a co-efficient of friction 0.3. Find the magnitude of the force, which can move the bedy, while acting at an angle of 25° Dith the porisental.



- 2420 => pcosa5° = F > F = 0.9063P
 - Deynew that F = 4R
 - > 0.9063p = & [W-px.4226] > 0.9063p = 0.3[300 - .4226] > 0.9063p = 90- .1268p > 0.9063p = 90- .1268p

87.1 N.

A body nufing on a neugh horizental plane requer of a pull of 180 M molined at 30°, to the plane to to more it. I was found that that a push to more it. I was found that that a push of 200 N inclined at 30° to the plane Joyt m of 200 N inclined at 30° to the plane Joyt m the trady determine the weight of the body the trady determine the weight.

80 30 FBD 50 10330 5420 F = 190 COS 30 2V 20 w + 220 sin 30 EV 20 = W- 180 m 30 10+110 190,52 = le (W+110) F, = -90) 155.88 equnO (2) Adding Substant , 130' 220 · 2 FOD 220-LA BO' 気れこり 190.52N

105.88 = WW -90 4 190.52 = 9LW + 110ML 6 9 + 34.64 = + 200k > W = 01732 Ary puting nature of all is equal O ver get 155.88 = 0.1732 (W-90). W = 991.68N 2) if co. efficient - but " the & blocks is 0.3. find force p key to move the block . WAZ 1KM WB = aRN Tain 90 (verisically) RI + T sin 30' = 1 km) 7/18/18/7 TSin 30' 2-2-R 1 Horeizonfally TU1300 = FI PT COSSO' = MRI > Tues 30' = 0.3 R, Daviding equator & D $\frac{T \sin 30'}{T \cos 30'} = \frac{1 - R_1}{0.3 R_1} \xrightarrow{>} \tan 30' = \frac{1 - R_1}{0.3 R_1}$

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0.5774 = 1-R1 1.14 0-3 R1 0.5774×0.3R1= 1-R1 0.173 R, = 1-R1 3 R1 2 0.85 KN 2) F= AR1 = 0.3 ×0.85 255KN WB+R1 RazztRi 2 0.85 ta = 2.85 KA Fa = PLRa 2 0.03 x 2.85 = .855W P z-F1+F2 • 255 + 855 = 1.11 KM 10.2

A bedy of net 500 N is lying on a reaugh plane. inclined at an angle of 250. supported by Aborizental force pas cheven in feg Defermine p for both upward e downward motion. $p_1 = W \sin(\alpha - \varphi)$ = 464 N Cos p. 376·2 N PR = Wsin (++) = 600 2> Andined plane as shown in fig is used to unload abedy of ut 400N. from a height 12m It = 0.3. (State useathere it is necessary to push the body daven the plane are hold it back from silving dever, what minim force is gueg. parallel for this purpose) And (P) 25 $- \frac{1.8}{2.4} = 0.5$ 5019 ·2m m = 26.5° 400 2 normal scene Rz ideoson z 400× 103 28.5 = 357.9N FFRR A sin os + SLR = P = 400 X 301 265 + 0.3 X 357.9

Equilibrium of a bedy on a rough inclined plane
Subjected to a force atting huriduately
Consider a body lying on a rough inclined plane
aubjected to a force acting hornerholdy.
Is Nimum force (P1) which will usep the body in
equil^(m), when it is at the point of Riding decomband

$$F = 9RR$$

 $AH = 0$
 $P \cos n + F = W \sin n$
 $P \cos n + W \sin n - KR = O(: F = LR)$
 $SV = 0$
 $Rv = W \cos n + P ingr = O$
 $P (\cos n + RP ingr = O)$
 $P (\cos n + RP ingr = W \sin n - L (W (\cos n + P) inn))$
 $P (\cos n + RP isingr = W sin n - L (W (\cos n + P) inn))$
 $P (\cos n + RP isingr = W sin n - L (W (\cos n + P) inn))$
 $P (\cos n + RP isingr = W sin n - L (W (\cos n + P) inn))$
 $P (\cos n + RP isingr = W sin n - L (W (\cos n + P) inn))$
 $P (\cos n + RP isingr = W sin n - L (So in - L (So inn)))$
 $P (\cos n + RP isingr = W sin n - L (W (\cos n + P) inn))$
 $P (\cos n + RP isingr = W sin n - L (So inn))$
 $(\cos n + 4mq cos n)$
 $(\cos n + 4mq cos n)$
 $(\cos n + 4mq cos n)$
 $(w (sin - singr cos n))$
 $(w (sin + singr) = W (sin n - R (cos n))$
 $(w (sin + singr singr))$
 $= W (sin - singr cos n)$
 $(w (sin + singr singr))$
 $= W (sin - singr singr)$
 $= W (sin - singr singr)$
 $= W (sin - singr singr)$

P₁ =
$$W \frac{\sin(w-\varphi)}{(\omega \in w-\varphi)}$$

 $V = W \frac{\sin(w+\varphi)}{(\omega \in (w+\varphi))}$
Pore force (P₁), when the body is moving upward.
P₁ = $W \frac{\sin(w+\varphi)}{(\omega \in (w+\varphi))}$
 $P_1 = W \frac{\sin(w+\varphi)}{(\omega \in (w+\varphi))}$
 $P_1 = W \frac{\sin(w+\varphi)}{(\omega \in (w+\varphi))}$
 $P_1 = W \tan(w+\varphi)$
 $P_1 = W \tan(w+\varphi)$
 Q_2
 Q_2
 Q_2
 Q_2
 Q_2
 Q_3
 Q_4
 Q_4

 $\phi_1 = \omega \frac{\sin(\alpha - \phi)}{\cos(\alpha - \phi)}$ *LEXESSADD PI= W ten (or-q) Force forces (P), when the bealty is moving upweared. $W = \frac{\sin(a^{2} + \phi)}{\cos(a^{2} + \phi)}$ P, = $P_i = W + an(\alpha + \varphi)$ Find the total force is in (2013) el? acon 300 (0.330 100 ->Ptoses 300 05 30 21=0 300 WS30 z R+ 200 vin 30 R = 300 cos30'-200 xin30' 24 20 -200 00530 + 300 singo'z F pr R = 200 cos 30' + 300 sin 30' Minimum force (p), keepthe bedy in equility when sliding downwood No sin (m - q) P1 2 Cos (0+ 4' Prime = Pa = Wain (a+4) LOS (0-9)

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In effort of such is requeired such to move certain bedy up an included plane at an angle 15° the focus acting I to plare. If angle spice " is 20°, then the effect very is found to be abon. Find needyhol of the boly . & in, fa = agenl piz 2ml a 221° on 2 15° \$F420 FH-10sing, = 20 22050 POLR 1+ REPORTING 15 = 2 PD > H W WS or + ala inis 2200 > MODON (H WEAT + MSing) = 200 Av 20 RIZW COSM 254 20 P= W Sq120 +F > ur + ws1920 = 230 0 10520 , & w cos 20 + w sageo = 230 > M(H W320 + 90920) 2230 SAV2 0 RR Z W COSRO' selios 20 + Sporo 230 H cos 15 + cints W Q cq10 H = 0.25 -> w (-259)x cos 15 + sin 15) 29m 0 (N2 392 N

I hand of torne withing an an inclined reaugh plane, can be moved up to plane by a face of and applied horizentally & by a face of 1.25 kN applied 11 to the place. Find engle of inclination s th P COS of vessor ew cases pun Q ۵ p= w sim(r+q) p= wtan (at p) 050 25 = 15 en(53.1) $an(\alpha + \varphi)$ 610 r+9 = 63. .96 = (220) a = 53.1-16.3 36.8 ye ztar \$ = tan x 16.3° .292 R/ Find the force trag to more a lead soon upon rough plane the force outing being " to the place. The inclination of the plane is such that when the same lood is kept on a perfectly smooth plane inclined at angle , of facue bar applied at an inclination of 30° to the plane, heip the same fead in equil19. et = 0.3. w Rangh. Smooth 12.3 mobth H=0.: \$ 20 310 cital on 210 Ces 30" Pzw Sin (ont P) Ac 0.3 AcRemas 140.71 PE w sin Pz 216.7

µ= 0.35 Deference value of p. 2 ZOON 3000 consider the pulley is friction les. Storing 80 sd FIDENSO 2000 P = MR0 + 800 0030 F +800 cos 30' > 5 2000 = Ro + 800 pin30 > Rn = 2000 - 8-10, 20130. > putting value of RM. P= Hx (2000- 800 Gin30) + 800 LOS30' = (1252.52) ~ Application of friction LADER PRICTION A balero is a denice for climbing on wells. 3.3 - As upper and of the ladder tends to IB slip deven reard, fordetton (Pw) is upwarcol. - As the lower end trobes to slip away from weall of 0 ATRY pruction (Fy) is towards the wealt. - Since the system is is equil?, thurafore the algebraic sum of heatrental & vertical componends of the forces must also be equal to zero.

Winform hadder of length 3.25m and neighing 250 N placed aganist a smooth vertical reall. 3)'s linear end 1.15 m from the wall. The co-effi cient of friction bell ladder & floor is 0.3. Determine a booth frictional free acting on ladden at point of contact bet ? ladder & floor. 00 SV20 Rf 2 250 N freem geometry BC2 = Ag2 - Ac2 125 30m Taking moment about 0. Rfx 1.25 - 250×(1.25) = Ff x3 Rt = 521. N A holder & meter long red on or horizental geound and leans against a smooth vertical reall at an angle 70° with horizontal. The weight of ladder is good and acts at it's middle. The ladder is at the peint of sliding, when a man weighing 7501 Sards in a the ladder 1.5m from bottom. calulate esp.

55cn20 60/ 1, 5m oc = 70 500520 101 2 900 N Wa 2 750 N Q= 900 +750 = 1650 N 4× Rf 7 Hf × 1650 N ... RA50570-900 x2.50570. Wing memery about B +60×3.5 0570 = 54 × 500 70. Rfx15 xin20° = \$ 900 x 2.5 Rin20 - 750× 3.5 Sin20° = Ffx5 Usao" . put the value of Ff \$ x 5 sinao - 900x 25 sinao - 750x3 5 sinao = 44x1650x 10:20' 1650 × 5 sin 20' 2 (4 f × 1650× 5001 20') + 975 t = 0.15 AN Duo identical blacks of weight ware supported a need inclined at 45° with horizenfal, as sheren in fig. of both the bleeves are limiting equilibrium, Find the orefficiend of Friction. (100 (4). ascaming it to be same W floor annellas at wall. Ff

902 Rooling forces verdically. > urwtry = 2W _____ New resolving the forces horizotally. RN = Ft > Rozurg-@ Substituting Rev in equin O. re(ref.) + Rf = 2W > H Rg + Rf = 2 W $\geqslant Rq = \frac{2W}{(1+H^2)}$ (9) potting nature of Rf is equi? @ $RW = \frac{41 \times \frac{2W}{\mu^2 + 1}}{\mu^2 + 1}$ Taking moment if the forces about black A Rux les 45° + Fux les 45°= Wallos 45°. RW +FW = W ZRW + HRW2W 3 RW (1+4) = W putting value of RN M Xaw (HH)=W 117+1 => &U(HH)= H2+1 2H +242 = H2+) 42+2H -1=0 l = -3+ (2) + 4 = 0.414 AS

NEDGE ERICTION I wedge is usually, of a triangular is cross-section , g is, genercally, used for slight adjustments in the position of a body in for tightening fits in keys for shafts. Dometimes, a medge is also used for lifting hearry weight. It is made of up reveal on metal. Wedge ABC, used to lift the body DEFG. N = neight of the body DEFG p =. Fonce leag. to lift the body horizent re = co-efficient of froitiens = tanp novement are ges vertical Whedge - Not considered. lift in upweared When forces pirapplied in . The body will direction Pole RI-resultant of fruictional fonce & normal kent bet floor energy. FI ERN Re -> angle of RN2-snownal rece? at AG froition. 8 frictional force Fa. The next scientifiel of both is Rz. onalding an angle \$2. 802

27 A wiform ladder of 9m kergth rusts aganst a vertical well with which it makes an anaple. of 95°. The control of freither bet lodder & well of & that bet? ladder & roadt floor well of & that bet? ladder & roadt floor as if a man whose weight is one-half of that ladder accesseds it. how high itwell be when the hadder slips?

50 a, distance bet A & the man neight of man = 12 =.50

Fro 2. Hur Rio 2 0.9 RW

RW = R+ = 0.5Rf Ryf = RRW

Resolving ventically RJ+FW = W+5.5W 2RW + 0.9. RW = 15W RW = 115W = 0.625W

Fw= 14 x. 629W 5.6.42 National manager about A. W X2 0545 + . 5WX 2 COS 45) = RW x 4 Sin 43 + FW X 604 COS 45

put value of RWS Fir

x = 30 3.0 m.

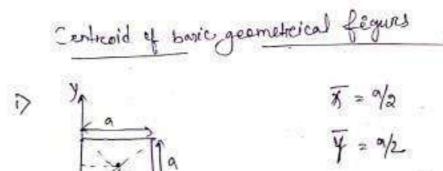
CHAPTER > 04 Centre of Gravety

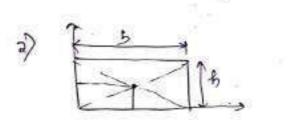
Centre of granity can be defined as a point through which the whole neight of the body acts, Ennespect of A's position. It may be noted that every body has one and only one contre of granity.

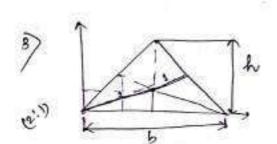
4.1 Centrooid

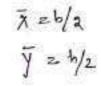
The plane figures like trisangle, rectangle, inche et a have only area, but no move. The contra of area of such fig is known as contraid.

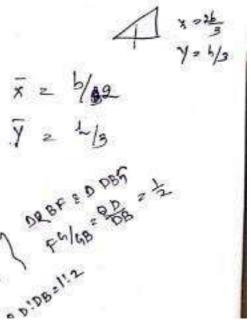
(12)



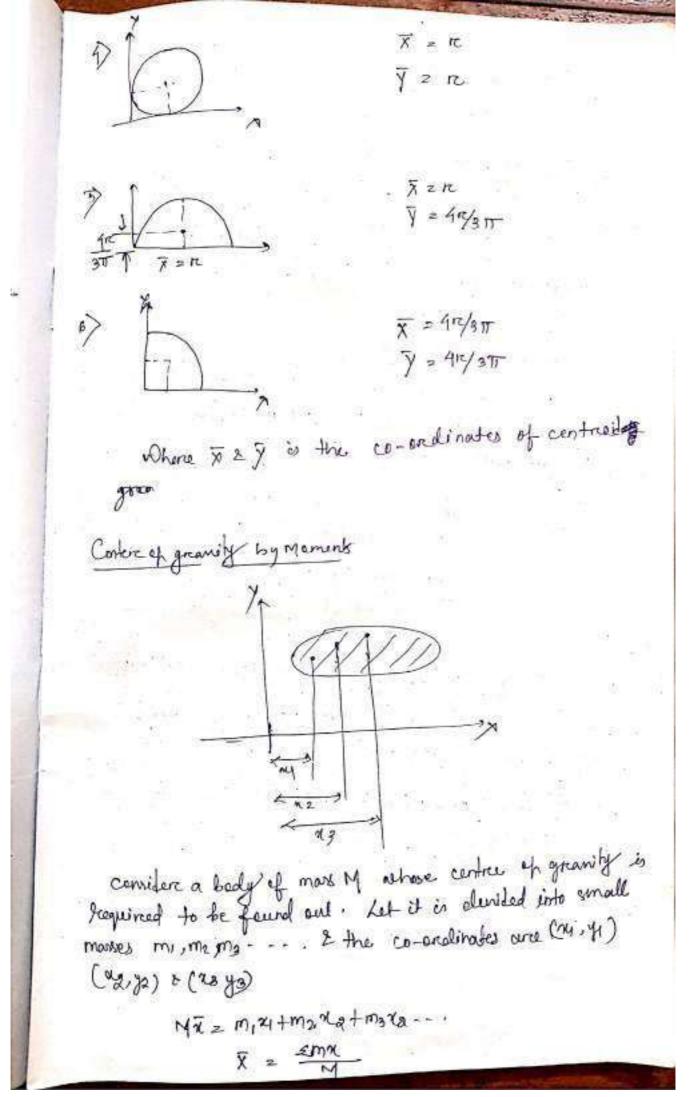








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y = xmy M= mitmet mat

Aris of Reference The centre of gravity of a bedy is alwears calculated with reference to g one assumed axis alculated with reference to g one assumed axis analytical with reference to g one assumed axis of neuerons axis of reference, called as aris of negerine from where F 2 y is calculated.

Centere of granify of plane figure The plane geometrical sections such as T, T, L Sections only have area but no mass. For there the centroid & centre of granity is same.

$$\overline{x} = \frac{a_1n_1 + a_2x_2 + a_3x_3 + \cdots}{a_1 + a_2 + a_3 + \cdots}$$

$$\overline{y} = \frac{a_1y_1 + a_2y_2 + a_3y_3 + \cdots}{a_1 + a_2 + a_3 + \cdots}$$

Center of granity of Symmetrical Sections - If the given section is sympetrical about X-X axis then use have to find X. - If it is symmetrical to Y-Y axis then we have Pofind X & y.

2) End the centre of gravity of 100 non x 100 nm x 30 nm of
T. subien
3) The section of is symmulated about
$$\frac{1}{100 \text{ mm} \times 30 \text{ mm}} = \frac{1}{2}$$
 and
 $y - y$ and $y - y$ and
 $y - y$ and $y - y$

$$\overline{a} = \underbrace{\alpha_{1}x_{1} + \alpha_{2}x_{2} + \alpha_{3}x_{3}}_{a_{1}+\alpha_{2}+\alpha_{3}}$$

$$= \frac{1}{4\pi}\sum_{n}\sum_{k=1}^{n}\sum_$$

$$\overline{x} = \frac{\alpha_1 \alpha_1 + \alpha_2 \alpha_2}{\alpha_1 + \alpha_2} = \alpha_{57000}$$

$$\overline{y} = \frac{\alpha_1 \alpha_1 + \alpha_2 \alpha_1}{\alpha_1 + \alpha_2} = 357000$$

$$\overline{y} \wedge uniform laminer is shawn in fry Octomine the CG of the laminer is shawn in fry Octomine the CG of the laminer is an end of the laminer is shawn in fry of the laminer is shawn if the laminer is shawn in the lamin$$

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MOMENT OF INERJIA 4-2 Moment of force = FX I distance. 11st memory of force. of FAIndistance X Ire distance (2nd memerit of focus) are moment smaneral M. M. O.F/Decend marmend of of focue) Sometime free & mans can be found out by above metheole. Balso known as Moment- of merchia (M. M. O. A 9 M.M. D. M Janes Tyy = Eda. x (m. I about = 5 24 . 2.2 Jyy 2 EdA. x2] - M2 abent X Dyy = Idana? In = [dA.y.2] - M.I about na ancis Moment of inentia - Parene X (porperdicular distance with = N m2 Moments of inertia of a sectorgular. Section considere a nastangalare Section 3 - Width sh-the section ABCD . d -> depth of the section Considere a small strip B2 of thickness dy/11 to X->0 abs' at a distance of from the centre gois.

Anca of mall strip = dA = bx dy Ł M.O.I of strop about x-x ancis Z Arua Xya = dA. y2 = bxdy. of2 $I x - \lambda = \int dA \cdot q'$ $- d/2 \frac{3}{2} \frac{3}{2} \frac{3}{2} \frac{1}{2} \frac$ 6 49 [(d/2)3 <u>d3/8</u> - (-d3/8) Ferchellew = b[<u>x/2</u>3.] Iny = bdg - b1d1) db3/12 - di 613/12 Dar = bd3/1a. = 263 circular section M.I of a - consider a vircle ABCD with cuntree 0. consider a riving of reading of and thickness ofter. area épôtre rieng d'a = arros. d'ac MOI about XX only = durea X distance anio - arra. dr. x x2 or xyy e alla³ da. Now MIL about the central asis tel it be I

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It 2 pring. da 2 or Jag don BUDA 2 2 2 x + 1" = Int = I d (r = da) for helles - (" In = Tyy = Jec = = Td4 Theorem of perpendicular Anis Don = = = [09-d9] = . I state that of I've & Igg be the memory of enortia of a plane section about 2. perpendicula - ancis melting at 0, The mement of inertia about Izz about the the aris perependicular to the plane and parsing thriangh intersection of X-X & Y-Y is given by Izz = Ixx + Iyy considerca laminas 100 of , area do howing exarchinates. nc sy on shopportion along ox 2 oy oncis og showenes for 1. considerca plane or I tooxe oy. Let re bette distance of Caminar p from 22 ares. op = re from geometry re?= 22+y2-M.I. abent XX . Inx 2 day2 Zyy 2 da. 22. YY

TAX , da. nº = da (n2+y2) ~ dane+da.y2 JAZZ INA + Tyy

Theorem of parallel ares

If states that of the M.Z of a plane area about an ancis through it's centre of granity is denoted by Iq, then moment of inscritin of the areas about any other areas AB, parallel to the 1st, and soladistance h from the cig is given by

IAB = Ig + ah2-

IAS -> M.I. of the area about ancis AB

Ig -> M.I - - about cig

a - a near of section

h - distance bet c.g i see"AB

convider a striep of a vin ale, where M.I. required to be found out let Sa = area in theip y = distances of striep from. A C.G. h sclisterer of C.G. From arcis AB

M.I of while heation about an aris paring through Up = Sa.y?

IG = ESa. y2' MI of whole see paning through C.G.

M'I of section about AB Ing = & sa (hty)? 2 & Sar (h2+ y2+2hy) " ({h2 da) + (zy2. sa) + (z 2 hy sa) Ing = aha+Iq. Shigh = shigum of moments 2y2 Ja = Iq M.I of a triangulary Section consider, a triangular section ABC whose not M.I in required to be found out. b - base hr > height (BC = base = b) Consider a small see" pg o thickness doc at a distance freem variass A. for DAPR, DABC PR = R > P? = BC. 2 = b.2 Smallarceai of the pg 2 bir xdx MI of strip about BC = Area x (destance)? $= \frac{bx}{du} \cdot du \times (h-u)^2$ = bx (h-2)2. dre M.I. of vehale southing a can be found out by integrating the above from 0 toh

 $I_{RC} = \int_{-\frac{bn}{b}}^{\frac{n}{b}} (b-x)^2 dx$ = = fm. (h2+n2-2hx) dx $= \frac{b}{h} \int (nh^2 + n^3 - 2hn^2) dx$ $z = \frac{b}{b} \left[\frac{x^2}{a} + \frac{x^2}{4} - \frac{abx^3}{3} \right]_a^b$ $z \frac{b}{h} \left[\frac{h^{4}}{a} + \frac{h^{4}}{4} - \frac{2h^{4}}{3} \right] = \frac{b}{h} \left[\frac{2h^{4} + h^{4}}{24} - \frac{2h^{4}}{3} \right]$ $2 \frac{b}{h} \left[\frac{3h^{4}}{4} - \frac{2h^{9}}{2} \right] = \frac{b}{h} \left[\frac{qh^{4} - 8h^{4}}{12} \right] = \frac{bh^{3}}{12}$ M.I. of thingular certion through aris of it's centre of gravity, parallel to X-aris Ig IBC + ad 2 <u>bb3</u> <u>bb3</u> <u>bby (b)</u> d= 1/3 IBC , IG+ ah2 $I_q = \frac{bh^3}{36}$ Moment of Inertia of a composite Section Steps Lo 1st aplit up the given section into plane arens. Ly Dind M.I of these areas about their rupective C.G. La Apply parendlel aris theorem. La Obtains the M.I.

Cirol 4.2 about axis kk Ø 120 > 10 0 0 splitup the seen into O 2(2) for seen O. IGI = M.I. about c.G about the ancis Ki-K. $T_{G_1} = \frac{db^3}{12} = \frac{120 \times 40^3}{12} = 640 \times 10^3 \text{ mm}^4$ W1 = 100+40 = 120 mm. Cdistance bet n C.G of seen () & axis K-K) M. I of seel aris K-K. Ing IGI + ashi -[640x103)+(120x40)x(120)?] = 69.76×106 mm Similarly M. I of section @ above . it's cog e parcellel to aris w. K. $IG_2 = \frac{db^3}{12} = 46.08 \times 10^6 mm^4$ ha = 100 + 240 = 220 mm Igz + ozha? =[(46.08×10))+(240×40)×(20)]; = 510.72×10 mm $IKK = 69.76 \times 10^{6} + 510.72 \times 10^{6}$ = 580.48×106 mm 4

2) Find the MII of a J-section with as 150 mmx comm and useb 150 mm x50 mm about x-X & y-y axis through the centre of gravity of the section. 150mm gol Reefongle O -50mm) 0 Q1 = 150 × 50 = 7500 mm? 1 = 150 + 50 = 175mm. 150 000 0 Rechargle (2) ag = 150 × 50 = 4500 mm2 ->1 1 K yz = 150 = 75 mm $\overline{y} = \underbrace{a_{4}y_{1}+a_{2}y_{2}}_{a_{4}+a_{2}} \underbrace{(\text{From x 175}) + (\text{From x75})}_{a_{4}+a_{2}} \underbrace{(\text{From x 175}) + (\text{From x75})}_{a_{5}+a_{5}$ y-sdistance from c.g. WI = 190+50 - 125 = 50mm M. I about x-x and Ig1 + a1 hi2 = 1.5525×10 + 7500×(50)2. = 20-3125 ×106mm Similarly 1-2 of @ about X-X aris $Iq_2 = \frac{bd^3}{1a} = \frac{50 \times (150)^3}{1a}$ 14.06 × 10⁶ mm⁴ ha = 125 - 150 = 50 mm M.Jabers KX aris Igztazh2 = 14.06 × 106 + 7500 × 502. = 32.9125 X10⁶ mm⁴ Txx = 20.3125 ×106 +32.8125 ×106 = 53-125 X 10 6 mm 4 AM

 $P_{G_1} = \frac{bd^3}{12} = \frac{60 \times a0^3}{12} = 40 \times 10^3 \text{ mm}^4$ WI = 81-8 = 130-60.8 = 69.2mm M.I. of rectangle. O about X-X IGI+ ahi2 = 40×103.+ [1200× (9.2)] = 5786×103mm1 for @ _ bd3 = 20×108 = 1666.7×103mm4 ha = ga-y = 70-60.8 = 9.2 mm Txx2, 2 IG2+a2h2 = 1896×103 mm1. for @ IG3 = 100 x203 = 66.7×108mm 4 he = ŷ-y== 60.9-10 = 50.9-mm. JANE = IGataghat = 5228 NOSmmt Dax = 55 (5-7 86 × 10) + (1836×10) + (5 229 × 10) = 12850 × 103 mm4

Sind the M.2 about the centredal . X-X 2 Y-Y axis of the angle section. got ovis. Section is not symmetrical about x ory_ 100 Rocelargle () = 100 X Q 0 = 2000 mm2-JI = 100/2 = 50 mm 2) az = 80x20 2 16 00 mm2 $y_2 = \frac{20}{2} = 10 \text{ mm}$ $y_{z} = \frac{a_1y_1 + a_2y_2}{a_1 + a_2} = \frac{2000 \times 50}{2000 \times 10} = \frac{2500}{2000} = \frac{2500}{2000}$ 2000 + 1600 M. I of O abeut X-X axis. $T_{G_1} = \frac{633}{12} = \frac{20 \times 100^3}{12} = 1.667 \times 10^6 \text{ mm}^4$ tu = y1- y = 50-95 = 15mm Ixa() = 241 + 44 h12 = 1-667×10 + 2000×(15)2 2 2.117×18 mm 9 M. I of @ about X-X-aris IGaz baz z 200x 203 = 0.04x 10 mm 4 haz yo- ga = 35-10 = 25mm 2xx(2) = 2G1 + agh22 = 0.79×108 mm 4

$$I_{X-X} = 2\pi u + 2\pi x_{2} = 2 \cdot 9 \cdot 9 \cdot 4 \times 10^{6} \text{ mm}^{3}$$

$$R_{Y} = 2y_{2}^{2} = 10 \text{ mm}$$

$$R_{Y} = 2 \cdot 60/2 = 50 \text{ mm}$$

$$\overline{u} = 2y_{2}^{2} = 20 \text{ mm}$$

$$\overline{u} = 2 \cdot 60/2 = 20 \text{ mm}$$

$$\overline{u} = 2 \cdot 60/2 = 20 \text{ mm}$$

$$\overline{u} = \frac{100^{2}}{04+00} = 20 \text{ mm}$$

$$\overline{u} = \frac{100^{2}}{04+00} = 100 \text{ mm}^{3}$$

$$D_{01} = \frac{10^{2}}{12} = \frac{100 \times 20^{3}}{12} = 0 \cdot 0.6 \times 10^{6} \text{ mm}^{3}$$

$$R_{1} = \frac{10^{2}}{12} = -24 = 85 - 10 = 15 \text{ mm}$$

$$2y_{Y} = 2y_{1} + \alpha_{1}h^{2} = 2 \cdot 0.6 \times 10^{6} \text{ mm}^{3}$$

$$\frac{1}{2} \cdot 9 \cdot 9 \times 10^{6} \text{ mm}^{3}$$

$$R_{1} = \frac{100}{12} = 201 \times 90^{3} = 0 \cdot 36 \times 10^{6} \text{ mm}^{3}$$

$$R_{1} = \frac{10^{2}}{12} = 201 \times 90^{3} = 0 \cdot 36 \times 10^{6} \text{ mm}^{3}$$

$$R_{1} = \frac{10^{2}}{12} = 201 \times 90^{3} = 0 \cdot 36 \times 10^{6} \text{ mm}^{3}$$

$$R_{1} = 2 \times 2^{-7} = 250 - 25 = 25 \text{ mm}$$

$$R_{2} = 2x_{2} + 0.2h^{2} = 1.11 \times 10^{6} \text{ mm}^{3}$$

$$R_{2} = 1 \cdot 6.27 \times 10^{6} \text{ mm}^{3}$$

23

i)

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CHAMER-05 Principle of Liffing Machinel.

5.1 La Machine :- I is an assembly of interconnected Componente arercanged to fransmit or modify force in ordors to perform weful more.

b. Sémple machine !- ?) is defined as a machine mehich helps to do some more a seme point when effort of ferre is applied to it.

La compound nuclime !- It can be defined as a device which consist of nor of simple machine which enable us to do some work at a faster speed weith loss effort as compare to comple machine

Lo Löffing Mouhine : - The nochine which are we to lift heavily land are called lifting mashine. In a lifting muchine a force on lead (w) applied at one point by means of another force called effort (D) applied at another point.

> Mechanical Advantage (M.A) M.A = neight lead lifted = W effort applied P $M \cdot A = \frac{W}{P}$

2) Velocity Ratio (V.R) V.R. = Wintance moved by effort = y Distance moved by lead

of Input :- it can be defined as workdore on the machine. If is measured by the preaduct of effect applied whe distance canned by the effort . i/p = pxy on effort x effort distance. output :- It is defined as the month dance by the machine, . 91 is the preduce of Leod Lifted & Listone returned by the land. Lead x lead sidence . output = WX2 " Efficiency (1) / Relation bet 7 1, M.A., V.R Ratioof where by the machine. Dorde dance on the m/c $= \frac{WXX}{PXY} = \frac{W}{P} \times \frac{Q}{Y} = \frac{M \cdot A}{V \cdot R} \times \frac{1}{V \cdot R}$ $= \frac{W}{P} \times \frac{1}{yX} = \frac{M \cdot A}{V \cdot R} \times \frac{1}{V \cdot R}$ $\boxed{y = \frac{M \cdot A}{V \cdot R}} \times 1.$ Ideal Machine 57 AV $\int = \frac{M \cdot A}{V \cdot R} = 100^{\circ} \int \cdot$ ie | 0/P = i/p. 2) macerifais weight lifting new a neight of that is lifted by an effort of 25 N. while wit mores by 100mm, the point of application of officet- mores by 8 m. InLMAINR 19. M == w/p = 40 NR = y/K = 80 M=MA/ve = 05 = 50 f. SHID W=1KN PRASN AL= 100 mm = 1 m 8 = 3

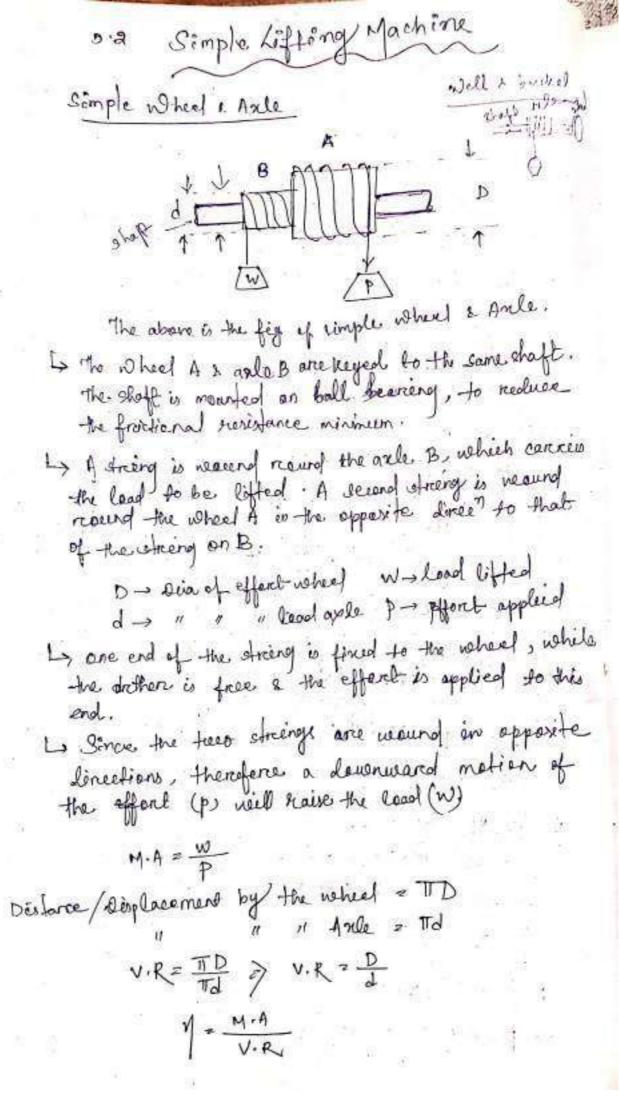
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Effort = 50 N (p) Lend (10) = 500 M effort distonce = (y) = A5 cm = @ .55m head distore = (21) = FEM = 0.05M VR = 4/2 = -155 = 11 N.A = 500 = 10 $\eta = \frac{10}{11} \equiv 0.9.1. = 90.1.$ \$ v.R = 50 Determin W & p= 60 1 2 70% VR = 8/2 1= MA MA = 12 30 F 7 MA2 35 > W z 2100 N. Renerosi bility of a Machine. daing l'espene nearch in the reversed direction, after effort is removed. Such a m/e is called a reversible m/c & unover of reversibility of machine. Centifier for Revensibility of angle N - load lifted by the m/e P - effort seen to lift the load y -> distance moved by effort his distance moved by looof.

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i/p = pky O/P Z WAX De unew that mk freition 2 i/p-0/p = pxy - wxx If the m/c is reversible then the o/p of the machine. sherld be more than friction. WHA > PXY-WXX M.A > % > awar > Pxy MA > 50%. MR > 50%. M > 50%. > WXM >12. > w/P > 1/2 So the condition is if the machine is reversible the efficiency is more than 501/. self locking m/c Some time a machine is not capeble. of deing any were wehen the effort is remared. Such machine is called as self lacking machine. Alere the efficiency sheuld not be more than 50.1. Low of Machine. Law of muchine may be defined as the relationship between effort applied & land lifted. Mathine Heally it is p- effect p2 mWtc . w - head lifted Elope)m-> conof configuration Pomo ideal N/c C - Another Lengt. seepennet mjr friction . ameunt > load of friction need to creations by the machine.

124 what lead can be lifted by an effect of 12011. if the vele. ratio is 18 2 1/2 60%. Determine the law of the machine, if it is observed that an effordof about is may to lift a load of 20000 & find the affent neg to run the mile at a lead of 3. MUN. 001 V.R 2 8/m= 18 Pzlab 12.6 $\frac{w/p}{y_R} = 16 \frac{w}{p} = 18 \times 6$ 2 93 10.9 3 W = 120× 9×9.10.9 = 1296N Laws of m/c p= 200 W= 2600 · Pzmw+c 120 = mx 1296 + y - 0 200 = MA2600+ (- 2) +80= + M 1304 7 m= 0.061 put the value of m is equi @ 120= 0.061X-1296+C 200= 0.061X2600+C 3-0-15 > C = 44 New effort seen. to supparent of 3,5th > 35×10 1 P = . 061x 3.5×103+44 P=25JN AM



worm A man D and drum. Lo of consist of a square threaded screw. S (knewer as searcon) & a terthed wheel (unever as searcon wheel) geared to each other ... Ly A wheel A is attached to the acorm, over uchich parties anope as sheven in fig. D- Ding of effort wheel te _ redues of the load brum. W- lead P -> Effect applied t → No. of teeth on the worr wheel. M.A = W Displace Distance moved by which = TD " " Load drum = amr V.R = TTD = DT = BOT -if the there is theread of n no. then V.R = DT OXAXIC 1) = M.A V.R

Simple. Screw. Jack It consist of a screw, fitted in a nut, which forms the body of the Jock. The principle, an which a screw ware s, is similar to that of an inclied plane. Ly The fig charas a rimple screw Jack . 17 L - leng the of effect and P -> effort-10 -> Lead p -> pitch of the served the distance moved by the effect it are revolution - att Distance moved by the Least 2 p V.R = ATT MA = W Single purchase Crabulinets In a single purchase enabusench, a repe is, fruit to the drum & is neound a few turns arrowed it.

The free end of the rope carries a load w. 1.4 toothed ushered 4 is nigidly mounted on the lead drawn L'Another toothid wheel B called pinion is geared with usheel & Ti - No. of texts in whell/gean A. 「ねー」 " " / " B. 1 - longth of handle He -> reading of load drum W -> Level p - effort . Distance moved by the affect in one recolution of hande = attl No. of scevel made by binien B = 1 A = T2 " Lead drewn = TA/TI distance moved by lead = attr xTa/TI Vir = attle = Tixl attrextops = Taxte MAZ P Ig 2 N.A Double purchase creats voinely

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If is the impressed version of single purchase weak and here there are a spun wheel & 2 pinion.

TI meshed with Ta (pinion) J3, , , J4 (pinion) L = length of the hadke . Tisty = No of teeth in span wheels Tably z " " peníon re = radius of drum W. - lead p 2 peffent Distance maned by effort in one tunolution of bardle = attl r lo. of scovols made by penson 9 - 1 , cour 3 = T4/T3 " poing = Ja/T3 " · epun 1 = 12 × 1/2 Distance mered by lead = atax To x Ty V.R = _ att 2m (12/11) (13/14)= + (1/2×14/13) M.F= W/P = M.A.

CHAPTER-06

DYNAMICS

6.2

Dynamics :- It is the study of motion of regid body and their relation with the forces causing them.

The enline system of dynamics is based on 3 laws of motion. Also known of marian law's of motion.

Newton's 1st law

It shakes that " Every bedy continues in its shake of rest are of uniform motion, in a straight line, when it is acted up on by some assternal force. It also called as have of inertia.

- Lo A bedy at rest- has a tendency to seemain at not called inertion of rest.
- Lo A body in uniform motion in a straightline has a tendency to prevenue its motion. Answer as inertial of motion. A I

Newton's 2nd Law

"The mate of change of momentum is lineably propentional to the impressed force and takes place, in the same dire" in which the force all?"

m = mass of a body U = gritial velo. of the booky V = Final velo of the bedy a = conf. acci" to a fime. is seconds sug. to change the velo Uto V. F = Forces sear to change velo from wto is ab tree.

gnifial mamenbugs mu final = mV Rate of change of momentum = mv-mv = m(v-v) 2 Ma Ace to and land Forma $\left(\begin{array}{c} \frac{v-v}{t} - q \right)$ > F= Kma n→ conist. For convenience, the will of fares adapted in which that it produces will ace!" in which mans. F2ma 2 massacel In s.I system unit of force is Newton -> N. A Newton may be defined as the force while acting upon a mans of 1 kg, produces an acel of 1 m/sd in the dire" of which it acts. Also known as have of dynamics. of all is due to greanity a 29.8 m/s2 = 1 kg. wt Fama (1 kg-wt = 9.8 N) > F = 9.8 1000000 N LL. Y.F = 9-8N) 2080800 = 1 kg.wb body has song mars on earth. Find a where g=9.84/62 by on moon g=1.7m/s= ≥u ever. g = 270 m/s2 F1 2 50 X 93 Fa 2-50 x 1-7 F3 - 50 K2 70

Konetic equations > V= Utat 's zub+'s al2 3 122UR+ 200 A particles of more nogen stands from nost & more under the influence of a const faces. I acquires a speed of om/s after 125. > And force on the particle ie) And speed at 1-212 a) First distance covered by the particle is fit ". , furing time 10.5. (v) Find interend 5 to 158. m = mans of the particle 250g = 0.05 kg UZO ¥ = 6 m/s t = 12, e > v = u + a + a\$620+ax12 Frma > a'z 6/12 = 0.5 m/s2 : Famxo 2 . 05 X.0.5 = 0.02 5 N ii) vzutat = 0 + (0.5 × 16.) = (80 m/s iii) sz v4.+ 1/2 al? 2 0+ + × 0.5×10 - 25m $S_{a}-S_{1} = \left(U_{a}^{+} \pm a d_{a}^{2} \right) - \left(U_{a}^{+} + \pm a d_{a}^{2} \right)$

Newton 3 red laws of Motion To every action there is an equal & epporite seen. Memorhum: - It is the pocoduct of mons with relocity. Prece :- Any extensional agent which presduce are tends to produce, destroys on tends to destroy the motion of any body. destroy the motion of any body. destroy or force. unit N. The prespecty which offers surisfance. The prespecty which offers surisfance to change state of next-or motion is benous as inerchia. FEmxa Inerchia! 斑 ... 28 AL

Newton and law for secoil of guin When bullet is fined from agun, the apposite scention of the bullet is known as scerail of que. M -> Mars ef gun. m -> Mans of Whet. V - velo. of gun v - neb if willet often being fined. memoritum before of the given = MV , bullef = mV MV = mv Law of conservation of Nomentum. D'alembert's preinciple A system of forces alling on a body eo motion is in dynamic equilin with cherchia farce of the body.

gnerefia -> Resist motion -s constat be at subt FR the renultant of S, Fa, F3 let bet a mans m. Fa of we nearly to bring the body preduces at rest, nee have to apply a force tooo is opposite dires TR. fiema whose value is equal to ma.

where main as investion force , to kning the body in thetic
where no investion force , to kning the body in thetic
upull?

$$FR = ma = 0$$

 $FR = ma = 0$
 $Fi = ma$
 $ma = s$ investion force $s = Pi + Also unsues as received
force.
 $Far = 0$
 $Far = 0$
 $From = 1$ force $received = 0$
 $From = 1$ force $received = 0$
 $From = 1$ force $received = 10^{-4}$ force.
 $W = F \cdot S$
 $M = F \cdot S$
 $= N - m = 1$ force $received = 10^{-4}$ force.
 $From = 0$
 $From = 1$ force $received = 10^{-4}$ force.
 $From = 0$
 $From = 1$ force $received = 10^{-4}$ force.
 $From = 1$ force $From = 1$ force $From = 1$ force $From = 10^{-4}$ force.
 $From = 10^{-4}$ $Fro$$

Energy I a the capacity to do work. Hereiste in many forms, yestanical electrical Chemical, heat, light etc. unit Came as neorth = Joules - in ycinetic = 1/2mv? Mechanical Energy potential = mgh Rinefic Energy Energy possed by a bedy, by vintue of its mans & velocity Energy powed by a hedy by wetue of its position. A truck of mans 15 tennes travelling at 1.6 m/s. Imp neith on spreng Low of concernation of Energy

I states that " Energy on neither be created nor destrayed. though it can transformed from one form to another form.

thansformation of energy . Considere a bedy of mans muchich is recleased from rest from hight to above the ground. m = manset the body h = height o Bringy at A since at A body has O velocity 40=0 pe = mgh total energy = petke = mgh energy af B y distance from A to B. 50 . The booky travelled · V 2. 1294 He at $B = \frac{mv^3}{2} \frac{2mx(xqy)^2}{2}$ P-E = mg Ch-y) = mgh -mgy total energy = kette = make + mghi - mgy = mghi thorque al c At a body has fallen a hight h. V = 1 2gh = mgh $ke = \frac{mva}{a} = \frac{m(2gw)^{3}}{a}$ ke the = mgh P8 = 0 to tal energy -

A range built in preloased from press from the top of som high huilding . good - too aborgo in p. 42 34 when it is also hight of lo from . to great ast" m = 100gm = 0.14g Wi = Rom PEF mgh, - " MG1 = 0 Impulse -> when a const forcer Facts and body for à time inferend. E. Known as groubre. I = FXt and N-3 Lineare momenting Kow it conservation of Linear momentum Ace to newton's and law, the metericinal face allong on a body is equal to reate of charge of linear momintum / mancentum. This leads to the law of conservation of lineare memeritur for abody which states that the linear momentum of a body leimade const. if the external force on a bedy is Zerco. 24 10 11

5.3 collision of Blastic Bedies

When tues bedies shalles weith each other with actain velocity it is known as callision.

to it (wall onfloor) also lenever as cellision.

Ly het any ball strikes to the floor, it rises certain height or rebounded.

Lo . This prependy of badies by viatue of which , they repounded after imposed is called elasticity.

Lo gut if a body does not exchand at all, after import called as inelastic collision.

Phenomenon of cellision

- The baddes, immediately after cellision, come memerilarily

- The twee bodies tend to compress each other, so long as they are compressed to the majoin value called as time of compression. (tc)

- The preserves of regioning of onegenal shape from the deformed shape of the badies called restitution. Time taken for those called as time of restitution (tr.)

Time of calisian = Time of comprovion + The of restitution

haw of concernation of Momentum of states that a the total momentum of two boolies remains conf. after their collision. . m101+ mava = m1v1+ m222 m1 = mons of 1st bealy maz " " and body UI, UR = emitial nelocity of mans mix ma scapping 11 m12 m2 1 Visva: final 11 Newtons haw ef collicion of elastic bodies I states " when two moving bodies callide with cash othere, their velo. of separation hears a const seatio to their velo. of appreach. (V2-V1) = e (U1-V2) where ui-va e = co-efficient of restitution UL U1 >U2 -> collision takes place. -s separation falcesplace. Va>VI -Koice Pypes of collision colision Direct -> Dudineet

Direct cellisions

The line of import of the two colliding bedies , is is the line Joining the untens of the 2 bodies, known as peind of contact or point of collivian. m101+ m202 = m2V1+m2V2. The nature of a is in bet " 0 to 1 if e=0 cillision is inclusfic 20110 222 " elastic. A bull of mans a up mening with a velocity am/see hit another ball of mass of kg at read , after imposed We sol ball comes to real. cal . velo, of the and ball after imposet. & certifie of rescritivition m1 = Rug 01 2.2 m/s ma = A way VI F = 0 (cemes densit V2 2 0 at rund $m_1 v_1 + m_2 v_2 = m_1 v_1 + m_2 v_3$ 2×2 = 4×V2 > Va = 1 m/s (v2-v1) = c. (V1-V2.) e = 1-0 = 1 = 2 0.5 An Theo balls of montres and & 3 kg are moving with 12015 velo am/s 2 3n/s treveards each other of e = 0.5. find prelacity of the tace balls offen collision. U12 8 U2 2 3

- V, ~? e - Va-Vi m1 A = Va-V1 - V2-V1 2-(-3) -Va. > were in set & fords. 2 = 2 V2-4 > V2+V1 = -5/2 6) > -Va-Vi = 5/2 -> V2 = -5/2 +V1 millitmald z minitmal put the value at > ax2 + 3 (-3) = av1 + (-3 v2) (equ" @ _0 21-3(-72-1)=5 2V1-3V2=-5 2 2V1+15/2+3V12-5 241-3422 -5 multiply 2 ineq (3×2) - 2×1- 2×2 = 5 > V1 2-255/3 -5V2 = .0 V2 = Omls Now V1 = - 7/2 = - 2.5 m/s Va = D " A ball is alsopped frameau height of som an a Smooth floor and it rebound to a hight of 570. Determine the coefficient of estilation between the ball & the floor & also determine the espected beight of the and seebound U - , vell before import V - 1 after h - high before " 10m " after 14 seebound 5m

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